

# Increasing Returns to Scale and Markups

Olga Shanks

George Mason University

*ostaradu@gmu.edu*

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# Motivation

- Increasing Returns to Scale can explain
  - Rising industry concentration
  - Decreasing share of labor in total output
  - Rising markups

Yet economists use the assumption of constant returns

- Autor et al. (2020) use CRS and require a change in consumer price sensitivity
  - Karabarbounis and Neiman (2014) use CRS and require the capital-labor elasticity of substitution to be greater than one
  - De Loecker et al. (2020) argue that markups cause industry concentration
- Estimation of Markups
    - De Loecker et al. (2020) argue that the aggregate markup of U.S. firms rose from 1.2 to 1.6 since 1980 to 2016
    - Inconsistent with profitability trends
    - Treatment of variable and fixed costs
    - Long vs. short horizons

# Data

- Compustat Fundamentals Annual database
- Publicly traded companies in the U.S. from 1980 to 2019

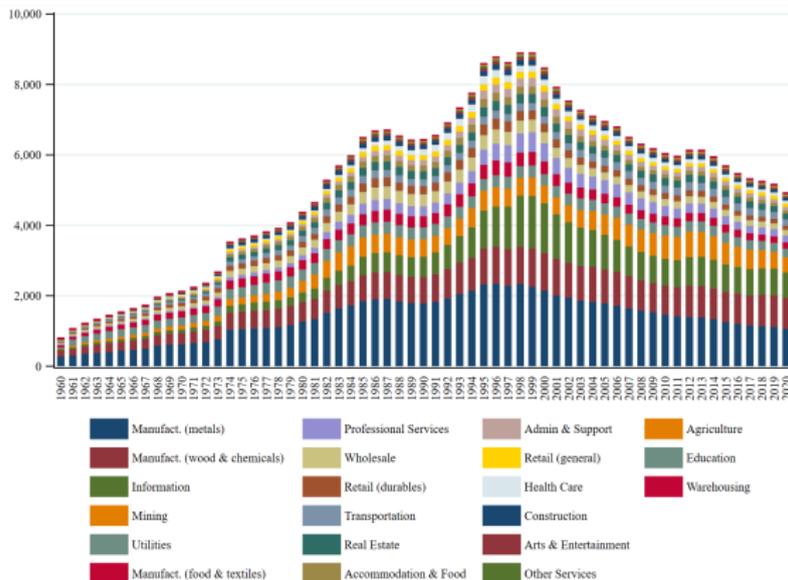
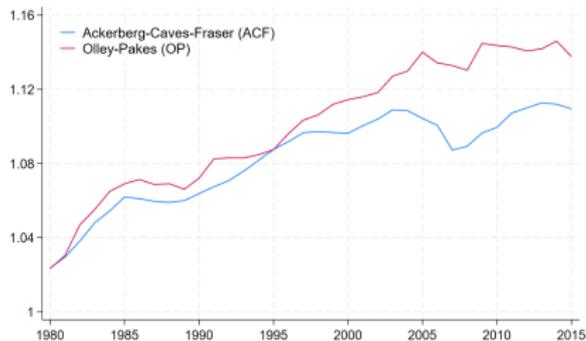


Figure: Number of firms in Compustat by year by industry

## Data (cont.)

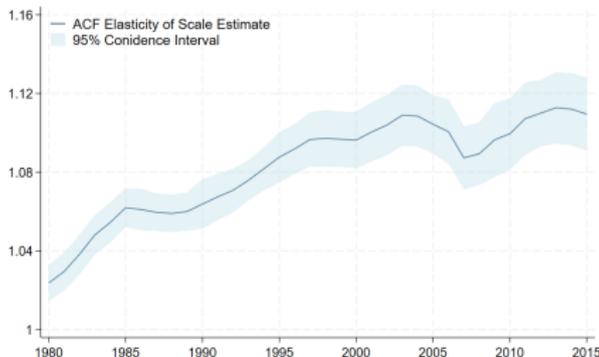
- Variable costs: Cost of Goods Sold (COGS) + Selling, General and Administrative (SG&A)
- Capital costs: Property, Plant and Equipment (PPE)  $\times$  user cost of capital
- User cost of capital is estimated:  $r_t = i_t - \pi_t + \delta_t$ 
  - $i_t$ : the Federal Funds rate
  - $\pi_t$ : FRED reported inflation rate, and
  - $\delta_t = 12\%$  for depreciation and risk premium
- Revenues and costs deflated by BEA chain-type price indexes by industry (2- or 3-digit NAICS level)
- Excluded Finance sector (NAICS code 52)
- 5-year rolling periods, e.g. 1980-1984, 1981-1985, etc.

## Results: Aggregate Returns to Scale



(a)

- Elasticity of scale is above 1
- Divergence after the Internet revolution
- OLS and Syverson's methods are biased
- Focus on ACF because:
  - Most conservative estimate
  - Allows estimation of standard errors
  - Variable costs are dynamic like capital



(b)

# Results: Industry-specific Elasticity of Scale

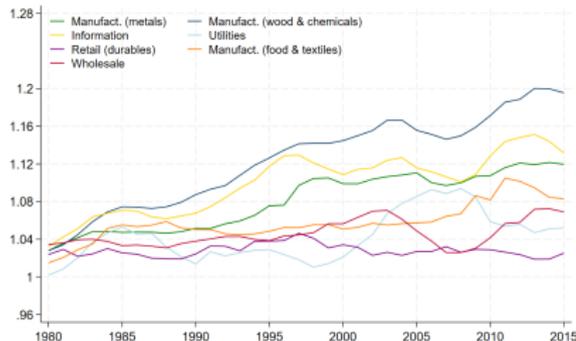


Figure: Top 7 industries

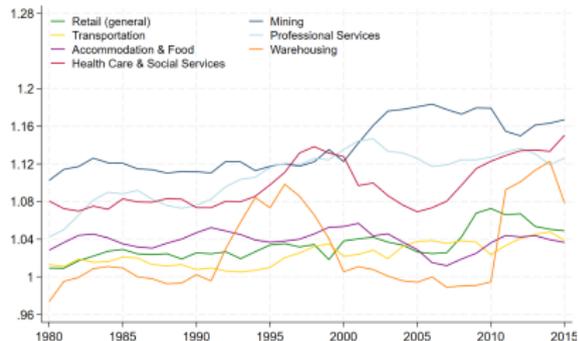


Figure: Middle 7 industries

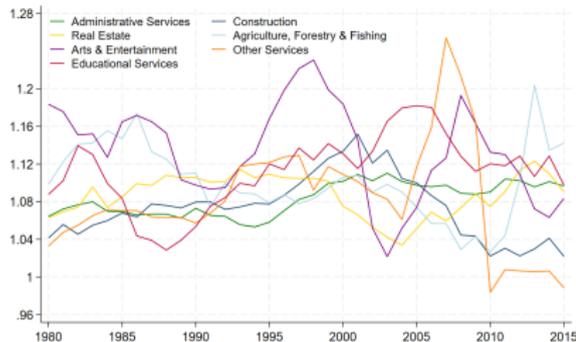


Figure: Bottom 7 industries

- Highest elasticity of scale
  - Manufacturing of wood and chemicals
  - Mining
  - Information
- Lowest elasticity of scale
  - Retail
  - Accommodation and Food
  - Transportation
- High volatility in the bottom 7 industries, likely due to the small number of observations

## Markup Estimation

- Cost-minimizing firm:

$$L(V, K, \lambda) = P^V V + rK - \lambda(Q(\Omega, V, K) - \bar{Q})$$

- Derive from FOCs:

$$\mu = e_V \frac{PQ}{P^V V}, \quad (1)$$

where  $\mu$  is markup and  $e_V$  is output elasticity of the variable input

- According to Varian (1992), Syverson (2019) and others,

$$\mu = \frac{P}{MC} = \frac{P}{MC} \frac{AC}{AC} \frac{Q}{Q} = \frac{AC}{MC} \frac{PQ}{AC \times Q} = e_{scale} \frac{PQ}{TC} \quad (2)$$

- De Loecker et al. (2020) use  $e_V$ :  $\mu = e_{COGS} \frac{Sales}{COGS}$

Traina (2018) uses  $e_V$ :  $\mu = e_{COGS+SG\&A} \frac{Sales}{COGS+SG\&A}$

Present research uses  $e_{scale}$ :  $\mu = e_{COGS+SG\&A+capex} \frac{Sales}{COGS+SG\&A+capex}$

## Variable Costs

Variable costs: COGS vs. COGS + SG&A?

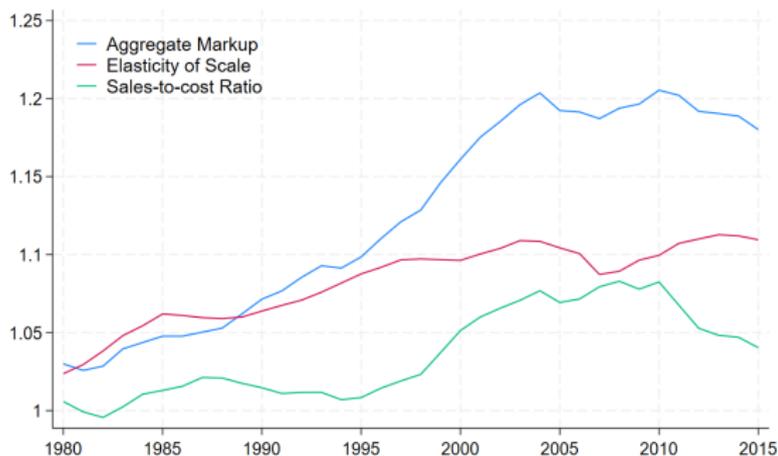
- COGS typically include:
  - raw materials
  - direct labor
  - manufacturing overhead
  - freight in
- SG&A typically include:
  - wages of sales and office staff
  - shipping of finished goods
  - rent & utilities
  - R&D
- COGS have been going down, while SG&A have been trending up: firms have been shifting costs from COGS to SG&A
- Firms have the incentive to improve Gross Margin (i.e. Revenues - COGS)
- Firms in the same industry may "decide" whether to record certain costs as COGS vs. SG&A
- Based on above: Variable costs = COGS + SG&A  
Traina (2018)'s  $\mu = 1.2$  vs. De Loecker et al. (2020)'s  $\mu = 1.6$

## Choice of Markup Formula

Markup formula:  $\mu = e_v \frac{PQ}{PVV}$  or  $\mu = e_{scale} \frac{PQ}{TC}$ ?

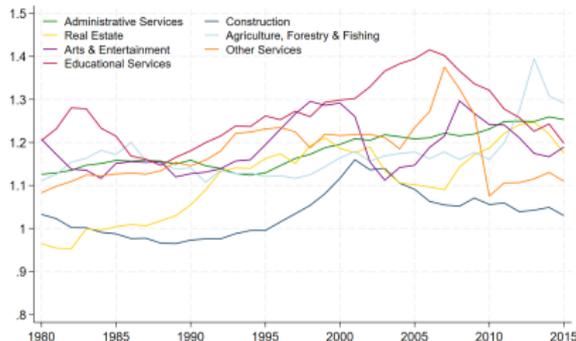
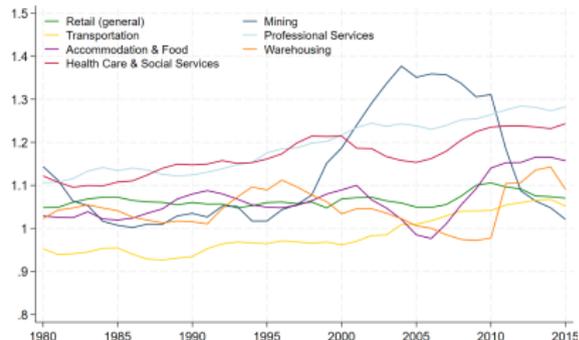
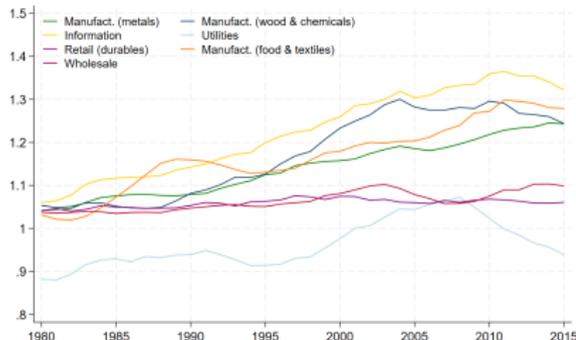
- $\mu = e_v \frac{PQ}{PVV}$  reflects a short-term view, where firms cannot adjust capital
- $\mu = e_{scale} \frac{PQ}{TC}$  reflects a long-term view, where all costs can change
- Long-term view is more appropriate for looking at data from 1980 to 2019
- Long-term view is more appropriate for large firms (most publicly traded firms)
- hardware refresh cycles have been shrinking from 10 to 5 to 3 years with fast-changing technology
- Renting vs. owning real estate will result in different classifications of costs for firms in the same industry (SG&A for renting and capital for owning)
- Based on above:  $\mu = e_{scale} \frac{PQ}{TC}$

# Results: Decomposition of the Aggregate Markup



**Figure:** Decomposition of the Aggregate Markup into Elasticity of Scale and Sales-to-cost Ratio.

# Results: Industry-specific Markups



- Highest markups
  - Information
  - Manufacturing of wood and chemicals
  - Manufacturing of food and textiles
- Lowest elasticity of scale
  - Utilities
  - Transportation
  - Construction
- High volatility in the bottom 7 industries, likely due to the small number of observations

# Macroeconomic Implications

## Constant Returns to Scale

$$Y_i = z_i K^\alpha L^{1-\alpha}$$

Firms with higher  $z_i$  are more productive and get bigger

**Implications:** break up a big firm  $\Rightarrow$  same high  $z_i$  across many small firms  $\Rightarrow$  increased competition and efficiency

## Increasing Returns to Scale

$$Y_i = z_i L^\alpha K^\beta, \alpha + \beta > 1$$

Firms of bigger size are more productive

**Implications:** break up a big firm  $\Rightarrow$  same high  $z_i$  across many small firms  $\Rightarrow$  increased competition, but destroys productivity

# Appendix

## Estimation Methods: OLS and Syverson's method

- OLS

$$Y = AK^\alpha V^\beta \quad (3)$$

$$y_{it} = a + \alpha k_{it} + \beta v_{it} + u_{it}, \quad (4)$$

so  $\alpha + \beta$  measures the elasticity of scale

- Syverson's method

$$Y = A(K^\alpha V^{1-\alpha})^\gamma \quad (5)$$

$$y_{it} = a + \gamma \ln(K_{it}^\alpha V_{it}^{1-\alpha}), \quad (6)$$

where  $\alpha$  is the share of capital in total costs, and  $\gamma$  is the elasticity of scale

Note: all regressions are run on data within 5-year rolling periods and include year fixed effects and sub-industry fixed effects

## Issues with Estimation: Omitted Price Bias

- Simple OLS in logs as a starting point:  $y_{it} = \beta_0 + \beta_k k_{it} + \beta_v v_{it} + u_{it}$
- Klette and Griliches (1996): output price is correlated with input choices
- Bond et al. (2021): deflating prices does not resolve the bias in the presence of market power and heterogeneous markups

$$r_{it} = y_{it} + p_{it} = \beta_0 + \beta_k k_{it} + \beta_v v_{it} + p_{it} + u_{it}, \quad (7)$$

where, in logs,  $r_{it}$  is revenue,  $y_{it}$  is output,  $p_{it}$  is price,  $k_{it}$  is capital,  $v_{it}$  is variable inputs, and  $u_{it}$  is the error term.

After deflating:

$$r_{it}^d = \beta_0 + \beta_k k_{it} + \beta_v v_{it} + (p_{it} - p_{t\_index}) + u_{it} \quad (8)$$

- Potential solution
  - add a proxy variable for  $(p_{it} - p_{t\_index})$
  - share in total industry costs,  $s$
  - $s$  reflects relative firm size; size affects the firm's residual demand, which in turn affects the price differential

## Issues with Estimation: Simultaneity and Selection

$$r_{it}^d = \beta_0 + \beta_k k_{it} + \beta_v v_{it} + s_{it} + u_{it} \quad (9)$$

- Simultaneity
  - $u_{it}$  contains productivity shock  $\Omega_{it}$
  - Productivity shock affects inputs
  - Productivity shock is observed by the firm but unobserved by the econometrician
- Selection
  - Firms may respond to a negative productivity shock by exiting the market altogether
- Olley and Pakes (1996) and Akerberg et al. (2015) resolve these biases

## Estimation Methods: Olley-Pakes

$$inv_{it} = inv_t(\Omega_{it}, k_{it}, s_{it}) \quad (10)$$

$$\Omega_{it} = h_t(inv_{it}, k_{it}, s_{it}) \quad (11)$$

$$r_{it}^d = \beta_0 + \beta_v v_{it} + \beta_k k_{it} + \beta_s s_{it} + h_t(inv_{it}, k_{it}, s_{it}) + e_{it} \quad (12)$$

$$\phi_{it} = \beta_k k_{it} + \beta_s s_{it} + h_t(inv_{it}, k_{it}, s_{it}) \quad (13)$$

- estimate (6) with OLS using a second-order polynomial for  $\phi_{it}$

$$\Omega_{it} = g_t(\Omega_{it-1}, P_{it}) + \varepsilon_{it} \quad (14)$$

$$P_{it} = p_t(inv_{it-1}, k_{it-1}, s_{it-1}) \quad (15)$$

$$r_{it}^d - \hat{\beta}_v v_{it} = \beta_0 + \beta_k k_{it} + \beta_s s_{it} + g_t(\hat{\phi}_{it-1} - \beta_k k_{it-1} - \beta_s s_{it-1}, \hat{P}_{it}) + \varepsilon_{it} + e_{it} \quad (16)$$

- estimate (9) with probit using a second-order polynomial for  $p_t$
- estimate (10) with nonlinear least squares using a second-order polynomial for  $g_t$
- all regressions are run on data within 5-year rolling periods and include year fixed effects and sub-industry fixed effects

## Estimation Methods: Akerberg-Caves-Frazer

$$\Omega_{it} = h_t(inv_{it}, v_{it}, k_{it}, s_{it}) \quad (17)$$

$$r_{it}^d = \beta_0 + \beta_v v_{it} + \beta_k k_{it} + \beta_s s_{it} + h_t(inv_{it}, v_{it}, k_{it}, s_{it}) + e_{it} \quad (18)$$

$$\phi_{it} = \beta_v v_{it} + \beta_k k_{it} + \beta_s s_{it} + h_t(inv_{it}, v_{it}, k_{it}, s_{it}) \quad (19)$$

- estimate (12) with OLS using a second-order polynomial for  $\phi_{it}$

$$E \left[ \begin{array}{l} y_{it} - \beta_0 - \beta_v v_{it} - \beta_k k_{it} - \beta_s s_{it} + \\ g_t(\hat{\phi}_{it-1} - \beta_v v_{it-1} - \beta_k k_{it-1} - \beta_s s_{it-1}, \hat{P}_{it}) \otimes \begin{pmatrix} v_{it} \\ k_{it} \\ s_{it-1} \\ \hat{P}_{it} \\ \hat{\phi}_{it-1} \end{pmatrix} \end{array} \right] = 0 \quad (20)$$

- estimate (14) with generalized method of moments using a second-order polynomial for  $g_t$
- all regressions are run on data within 5-year rolling periods and include year fixed effects and sub-industry fixed effects

# Results: Markups Using Different Cost Categories

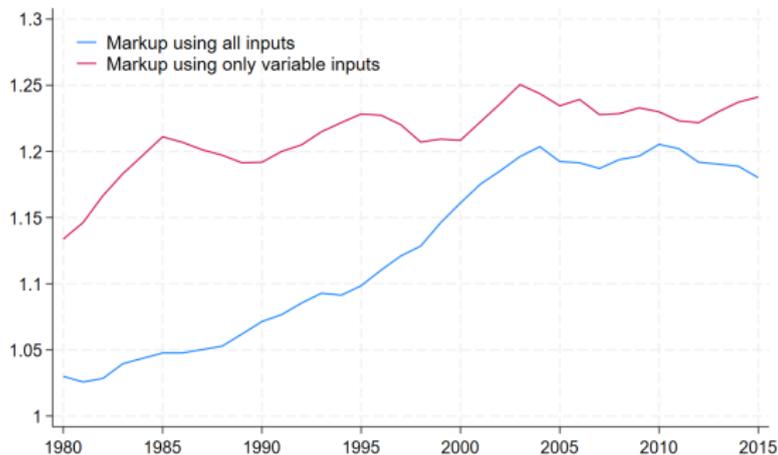


Figure: Markups Using Different Cost Categories

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