Resilience in Vertical Supply Chains

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- COVID-19, natural disasters, cyber-attacks...
- Public attention has focused on supply chain resilience
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- Firms: Private sector incentives
 - Visibility, Redundancy, Agility
- Policy-makers: Public Sector Strategies
 - Correct market failures resulting from externalities
 - Particularly important upstream

- What are the relevant externalities in a canonical model of vertical supply chains?
- What are the market distortions?
- How do optimal policies vary along the supply chain?
- How do first-best policies for resilience and network formation differ from second-best policies?

A Novel Model of Vertical Supply Chains

- Arbitrary number S + 1 of tiers: tier s firms purchase from tier s 1 suppliers (snake across tiers)
- Each firm has many suppliers (continuum) in tier above (spider within each tier)
- Each firm has many customers (continuum) in tier below
- Quantities and payments determined by bilateral bargaining
 - Bargaining sequential moving up the supply chain
 - Lead firms in tier S sign contracts with suppliers in S-1.
 - Firms in S-1 sign contracts with firms in S-2...
- All bargaining between firms in tiers s and s + 1 occurs simultaneously (Nash-in-Nash)
- Exogenous and independent risks of catastrophic supply chain disruptions
 - Endogenous networks (redundancy)
 - Endogenous resilience (agility)

Stages

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Firms choose supplier links \eta_s and investment in resilience r_s
   disruption shocks are realized
   surviving firms in tier S bargain with their surviving suppliers
   in tier S - 1 over \{m_{S-1}, t_{S-1}\}
   surviving firms in tier S - 1 bargain with their surviving suppliers
   in tier S - 2 over { m_{S-2}, t_{S-2} }
   surviving firms in tier 1 bargain with their surviving suppliers
   in tier 0 over \{m_0, t_0\}
   firms hire labor l<sub>s</sub>, manufacture intermediate inputs m<sub>s</sub>, and fulfill their
  contracts, for s = 0.1, \dots, S - 1
+ firms in tier S hire labor l_s, manufacture final output and sell to consumers x_s
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- Production technology in tier s: Cobb-Douglas across labor and bargained tier s - 1 intermediate inputs, CES across intermediate inputs
 - Tier 0: linear production function in labor
- **Demand**: derived from CES aggregate preferences over differentiated final goods
- Ex-ante investment in agility r_s leads to survival probability $\phi_s(r_s)$
- Ex-ante investment in link formation $\eta_s \rightarrow$ match with fraction η_s of surviving ex-ante formed links
- Labor market clearing: labor used for production of intermediate inputs, final goods, and for investments in agility and links.

Recursive Solution: we show that sequential Nash-in-Nash yields an intuitive and tractable solution for negotiated transfers and quantities

Markup factor: key result from recursive bargaining solution:

$$\mu_{s-1} = (1 - \beta_s) \frac{\sigma_s}{\sigma_s - 1} + \beta_s$$

- β_s : bargaining weight of tier *s* buyer
- σ_s : elasticity of subsitution of tier s buyer across tier s-1 inputs

First-Best Policies

Need 3 sets of policy instruments to decentralize first-best allocation:

- Taxes/subsidies on input transactions $\{\tau_s\}_{s=0}^S$
- Taxes/subsidies on investment in agility $\{\theta_s\}_{s=0}^S$
- Taxes/subsidies on investment in link formation $\{\vartheta_s\}_{s=1}^S$ Find:
 - $au_0^* = au_S^* = 1
 ightarrow$ no subsidy at extremes
 - $\tau_s^* = \frac{1}{\gamma_s + (1 \gamma_s)\mu_{s-1}} < 1 \rightarrow$ subsidy on purchases in the middle to correct consumption distortion
 - $heta_0^* < 1$
 - $\theta_s^* = \vartheta_s^* = \frac{1-\beta_{s+1}}{\tau_s^*} \gtrless 1 \rightarrow \text{correct for excess incentives caused by transaction subsidies}$
 - Key: If $\beta_s = \beta$ and $\sigma_s \ge \sigma_{s+1}$ for all *s*, resilience and link formation subsidies decrease as we go downstream

Second-Best Policies

Setting where $\tau_s = 1$ for all s

Findings:

$$\theta_s^\circ = \frac{1 - \beta_{s+1}}{J \prod_{j=s+1}^{S-1} B_j} \gtrless 1 \text{ for } s \in \{0, 1, ..., S-1\}$$

where $B_j = \gamma_j + (1-\gamma_j)\mu_{j-1}$ and J < 1

Intuition: second-best subsidies *increase* with markups and input shares downstream from s since markups reduce downstream sales and profits and depress incentives to invest

- If $\beta_s = \beta$ for all *s*, then second-best resilience subsidy is larger upstream
- Upstream firms create positive externalities for *more* downstream firms
- Second-best link subsidies same as second-best resilience subsidies: $\theta^{\circ} = \vartheta^{\circ}$

- New model of vertical supply chains with multiple tiers, endogenous networks, endogenous resilience, bilateral and sequential bargaining in general equilibrium
- Bilateral bargaining with shared surplus generates private cost of inputs greater than social cost
- First-best policy offsets effect of "markups" on perceived costs
- Second-best depends on accumulation of downstream conditions
- Under reasonable conditions on bargaining and production parameters, first and second-best resilience and link subsidies are larger upstream