

Saving Behavior across the Wealth Distribution

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What We Do

- Use Norwegian administrative data on income & wealth to examine saving behavior across the wealth distribution

Why Care?

Macro

- Many workhorse models: saving rate \approx independent of wealth (or slightly decreasing with wealth, especially at bottom)
- Related result: aggregate dynamics \approx independent of wealth dist
- Does saving behavior in data look anything like in these models?

Inequality

- Is saving behavior a force toward diverging wealth inequality?

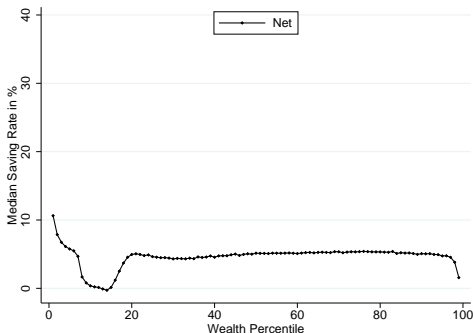
Our Findings

1. Relation between saving rates and wealth depends on whether saving includes capital gains
 - (a) saving rates **net of capital gains** (“net saving”)
 - (b) saving rates **including capital gains** (“gross saving”)

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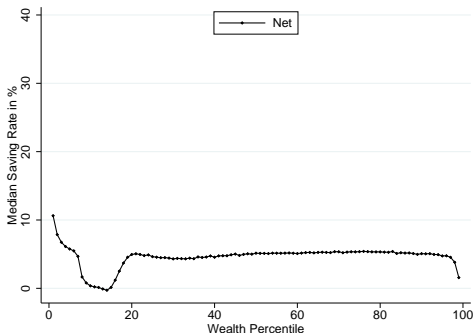
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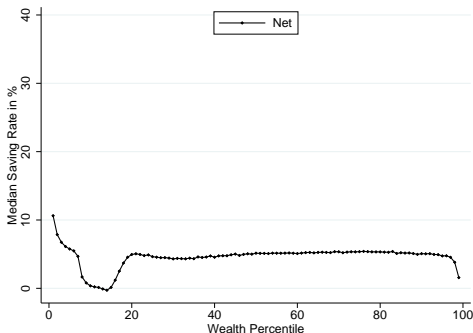


- seemingly consistent with workhorse models

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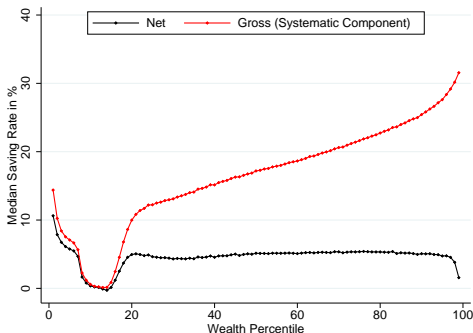
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- seemingly consistent with workhorse models
- but: economic theories are **not** about **net** saving

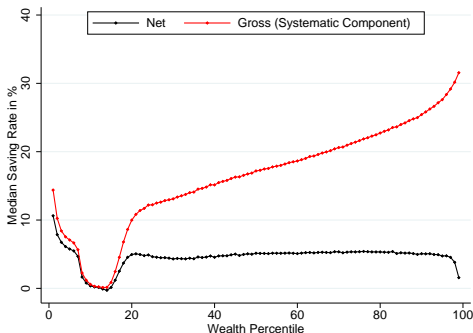
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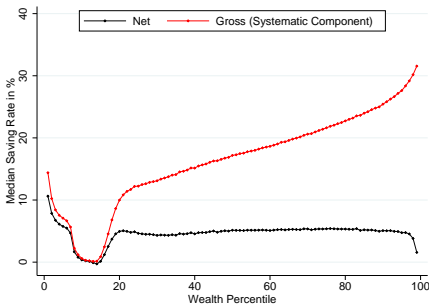
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- rich people hold assets that experience persistent capital gains, **do not sell these to consume** \Rightarrow **they save more**

Our Findings: “Saving by Holding” – Back-of-Envelope

1. Saving rates excluding and including capital gains



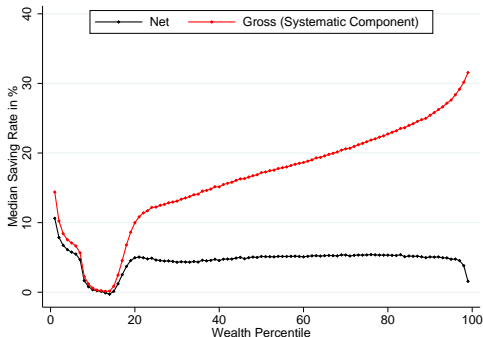
Back-of-envelope example to clarify:

- assume net saving rate = 10%, capital gains on all assets = 2%
- **Paul**: income (excluding cap gains) = \$100,000, assets = \$0
- **Richie**: income (excluding cap gains) = \$100,000, assets = \$1,000,000
- gross savings are \$10,000 and \$10,000 + \$20,000 = \$30,000
- gross saving rates are 10% and $\frac{30,000}{100,000+20,000} = 25\%$

Our Findings

2. Implications for theory:

- Joint pattern for net & gross saving rates \neq workhorse models



- Potential explanations
 - multiple assets + portfolio adjustment “frictions”
 - ... (will discuss a few others)

Related Literature

Empirics:

1. saving across **wealth** distribution Bach-Calvet-Sodini
2. saving across **permanent income** distribution Dynan-Skinner-Zeldes, Straub
3. **rates of return** across wealth distribution Fagereng et al, Bach-Calvet-Sodini

Macro:

- aggregate implications of income & wealth heterogeneity
Krusell-Smith, Krueger-Mitman-Perri, Quadrini-RiosRull, Kaplan-Violante, Auclert-Rognlie, Straub,...
- consumption response to asset price changes Poterba, Paiella-Pistaferri
Christelis-Georgarakos-Jappelli, Berger-Guerrieri-Lorenzoni-Vara, Kaplan-Mitman-Violante, Guren et al,...

Inequality:

- theories of wealth inequality at point in time
Benhabib-Bisin, DeNardi-Fella, Jones, Piketty-Zucman, ...
- wealth inequality dynamics, type/scale dependence?
Gabaix-Lasry-Lions-Moll, Kaymak-Poschke, Hubmer-Krusell-Smith, Garbinti-GoupilleLebret-Piketty, Gomez, ...

Other areas:

- public finance, particularly capital taxation Saez-Stantcheva, Jakobsen-Kleven-Zucman
- household finance Campbell, Calvet-Campbell-Sodini

Plan

1. Data
2. Theoretical benchmarks
3. Key conceptual issue: how to think about changing asset prices
4. Results
5. Theoretical interpretation

Data

Norwegian Population Tax Record Data

- Sample: roughly 3.3 mio persons per year
- Period: 1993 to 2015 but focus on 2004 to 2015 (12 years) so as to combine with shareholder and housing registries
- Tax records include (Norway has a wealth tax):
 - asset holdings by broad asset class (e.g. deposits, housing)
 - income (labor, business, capital, and transfers)
- Third-party reported: scope for tax evasion limited
- **Advantages:** long panel data, no attrition, even very top tail in data set, limited measurement errors
- **Disadvantages:** don't observe individual asset prices/unrealized capital gains directly

Definition of Wealth and Asset Categories [▶ wealth distribution](#)

- Wealth = deposits + stocks + stock fund holdings + informal loans + bonds + housing + private equity + vehicles/boats – liabilities
- For most categories: tax value = market value
- Private equity: tax value \approx book value \leq market value [▶ details](#)
- Housing: use transaction data and house characteristics to estimate market values
- Pensions: not included in wealth or saving (to be estimated)

Why not US or EU data?

- Why not simply use, say, the US Survey of Consumer Finances (SCF) or EU Household Finance and Consumption Survey (HFCS)?
- Because they do not fulfill requirements to make our main figure
 1. reliable information on assets, liabilities
 2. panel data
 3. large number of observations

Theoretical Benchmarks

A Series of Benchmark Models

1. The simplest consumption-saving model
2. The simplest consumption-saving model + changing asset prices
3. Labor income risk, borrowing constraints, lifecycle, β heterogeneity
4. Housing

1. The simplest consumption-saving model

- Households solve:

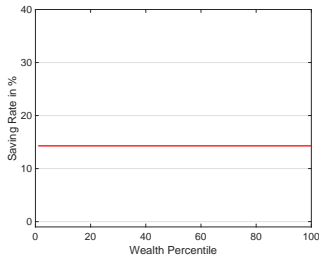
$$\max_{\{c(t)\}_{t \geq 0}} \int_0^{\infty} e^{-\rho t} \frac{c(t)^{1-\gamma}}{1-\gamma} dt \quad \text{s.t.}$$
$$\dot{a} = w + ra - c, \quad a \geq -w/r$$

- Saving policy function is **linear** in wealth a

$$\dot{a} = s(a) = \frac{r - \rho}{\gamma} \left(\frac{w}{r} + a \right)$$

- Constant saving rate** out of total income

$$\frac{s}{y} = \frac{s}{w + ra} = \frac{r - \rho}{\gamma r}$$



- Aside: no clean prediction for saving rate out of **wealth** (Bach-Calvet-Sodini)

$$\frac{s}{a} = \frac{r - \rho}{\gamma} \left(\frac{w}{ra} + 1 \right)$$

2. Changing asset prices

- Consider asset with price p , dividend yield θ

$$c + pk = w + \theta pk, \quad \frac{\dot{p}}{p} = \mu + \varepsilon$$

μ = “persistent”, ε = “transitory”

- Map into previous model by defining **wealth** $a := pk$

$$c + \dot{a} = w + \underbrace{(\theta + \mu + \varepsilon)}_r a$$

- Solution:

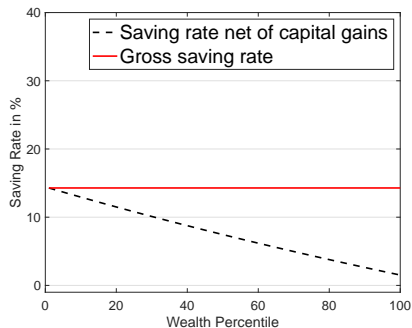
$$\dot{a} = s(a, w, \bar{r}) + \varepsilon a \approx \bar{s}(w + \bar{r}a) + \varepsilon a, \quad \bar{r} = \theta + \mu$$

- **Unrealized capital gains are income** (Schanz-Haig-Simons)...
- ... but different responses to different types of capital gains:
 - transitory $\varepsilon > 0$: 100% saving rate out of these
 - persistent $\mu > 0$: consume part of resulting income flow(similar logic as transitory vs persistent labor income shocks)

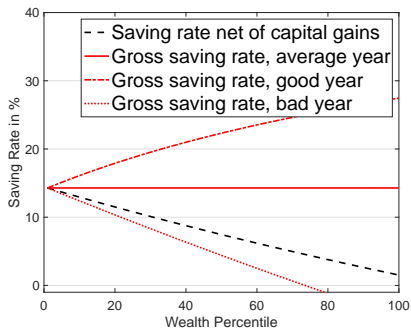
2. Changing asset prices

In cross-section, richer \Rightarrow capital gains = larger fraction of income

- transitory $\varepsilon > 0$: 100% saving rate out of these
- persistent $\mu > 0$: consume part of resulting income flow



(a) Only persistent: $\mu > 0, \varepsilon = 0$



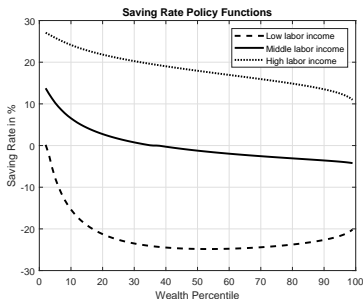
(b) Both: $\mu > 0, \varepsilon \leq 0$

1. **net** saving rate **de**creasing with wealth (if $\mu > 0$)
2. **systematic** component of **gross** saving rate **independent** of wealth

3. Labor income risk etc ▶ details

(a) Labor income risk and borrowing constraints:

- flat/slightly decreasing saving rate **conditional on labor income**
- previously noticed by De Nardi & Fella (2017)



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(b) More realistic life cycle:

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(c) Discount rate heterogeneity:

- flat/slightly decreasing **conditional on discount rate**

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Overall:

- \approx constant saving rate **conditional on observables** (age, ...)
- could be \nearrow in cross-section due to spurious correlation
But our data allows us to **control** for these!

4. Housing ▶ details

Housing differs from other assets:

1. not just asset but also consumption good (Glaeser, Buiter, ...)
2. indivisibilities/adjustment costs

Lots of people's intuition: (1) by itself \Rightarrow should save $\dot{p} > 0$. Logic:

- $p \uparrow$ means housing more expensive = bad for you
- \Rightarrow should not consume out of $\dot{p} > 0$, even if persistent

We show: (1) by itself is not enough, instead need (2). Without (2):

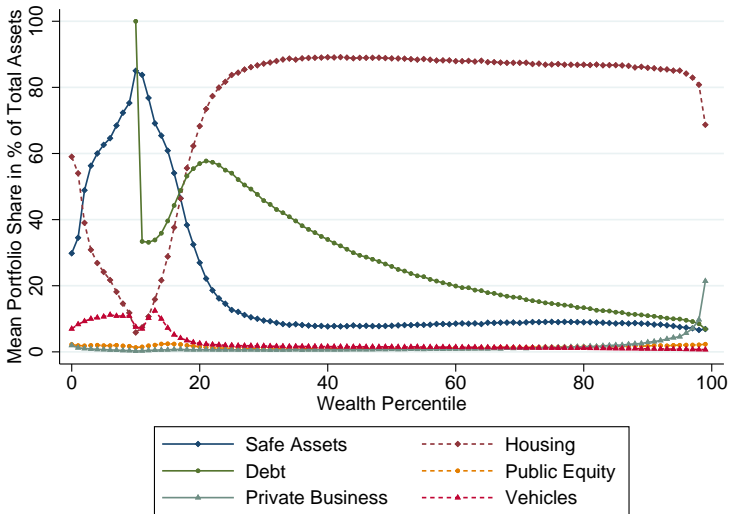
- intuition above is wrong because it ignores **intertemporal substitution of housing**
- $\dot{p} > 0 \Rightarrow$ buy bigger house now, then gradually **sell off over time**
- collapses to one-asset model with \approx **constant gross saving rate**

Takeaway: it's true that housing is different, but because of (2) not (1)

Key Concepts and Definitions with Changing Asset Prices

Portfolio Shares: The Importance of Housing

▶ zoom top 1%



Notes: 12th pctile = 0 net worth. Safe assets = deposits + bonds + informal loans.

Net, Gross and Recurrent Saving

- Two ways of writing **consumption + saving = income**

$$c + \underbrace{pk}_{\text{net saving}} = \underbrace{w + \theta pk}_{\text{disposable income}} \quad (1)$$

$$c + \underbrace{pk + \dot{p}k}_{\text{gross saving}} = \underbrace{w + (\theta + \dot{p}/p)pk}_{\text{Haig-Simons income}} \quad (2)$$

- Standard theories only have implications for gross saving in (2)
- Have shown: implications different for transitory vs persistent \dot{p}/p
 - expect saving rates to vary strongly with market performance
- \Rightarrow focus on **recurrent saving** = systematic component

$$c + \underbrace{(\dot{k}/k + \mu)pk}_{\text{recurrent saving}} = \underbrace{w + (\theta + \mu)pk}_{\text{recurrent income}}, \quad \mu := \overline{\dot{p}/p} \quad (3)$$

- Simple benchmark: recurrent saving rate = independent of wealth

Additional Issues with Housing

- Housing is not just asset but also consumption good

$$\underbrace{c + Rh}_{\text{consumption}} + \underbrace{\dot{p}h + ph + \dot{b}}_{\text{gross saving}} = \underbrace{w + rb + Rh + \dot{p}h - \delta ph}_{\text{Haig-Simons income}}$$

- Rental-equivalence approach: $R =$ rental rate on similar properties
 $= 2.88\% \times ph$ (Eika-Mogstad-Vestad)
- Alternative (not today): user-cost approach: $R = (r + \delta - \dot{p}/p)p$

Implementation

1. **Separate gross** saving into **net** saving and **capital gains**
 - housing: use transaction data
 - public equity: use holdings of individual stocks (shareholder registry)
 - private equity: arguably $\Delta(\text{book value}) \approx \text{net saving}$
 - bonds: compute from arbitrage with treasury rate
2. Estimate **persistent capital gains** μ
 - mean of realized \dot{p}/p from 1950 or as long as series go back
 - housing: very high price growth 2004 – 2015 \Rightarrow this matters

Asset	Average capital gain	Average rate of return
Public equity	3.25 %	6.18 %
Housing	2.25 %	5.13 %
Bonds	1.06 %	2.03 %

3. Calculate saving rates $\frac{s}{y}$

Saving Rates across the Wealth Distribution

Saving Rates across the Wealth Distribution

- Start with **simple descriptive plots** using “raw data”
- Afterwards: **similar patterns** with controls

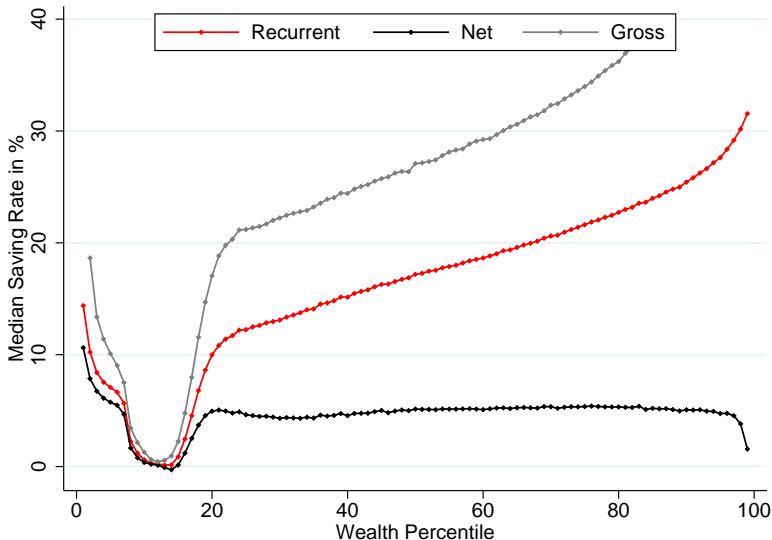
Median Saving Rates

▶ zoom top 1%

▶ bad year

▶ dispersion

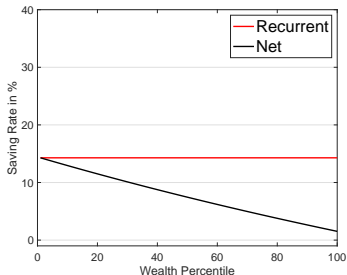
▶ sample restrictions



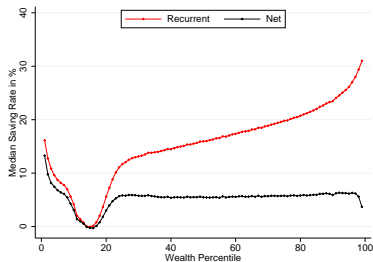
Note: for now, dropped bottom 1st percentile

To be clear

1. Completely different from predictions of simple benchmark model



(a) Benchmark model



(b) Data

2. Not just one lucky year: $\dot{p}/p > 0$ in most years and

Asset	Average capital gain
Public equity	3.25 %
Housing	2.25 %
Bonds	1.06 %

Controlling for the usual suspects

▶ age

▶ inc

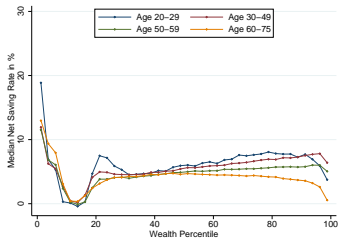
▶ educ

Median regression with controls \mathbf{x}_{it} = age, earnings, education

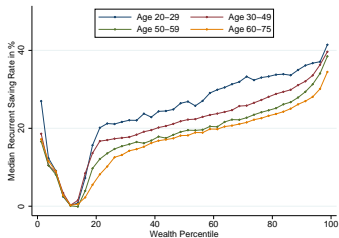
$$\frac{S_{it}}{y_{it}} = \phi_1 + \sum_{p=2}^{100} \phi_p D_{it,p} + f(\mathbf{x}_{it}) + \mu_t + \varepsilon_{it}$$



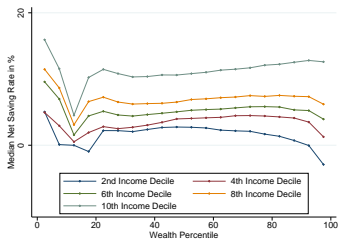
Controlling for age, earnings, and education



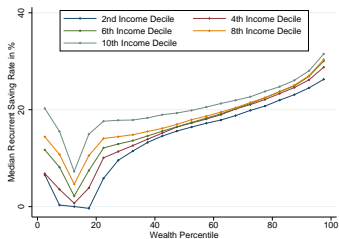
(a) Age, net saving rate



(b) Age, recurrent saving rate



(c) Earnings, net saving rate



(d) Earnings, recurrent saving rate

Is this exclusively a story about housing? No

Question: what if “take out” housing?

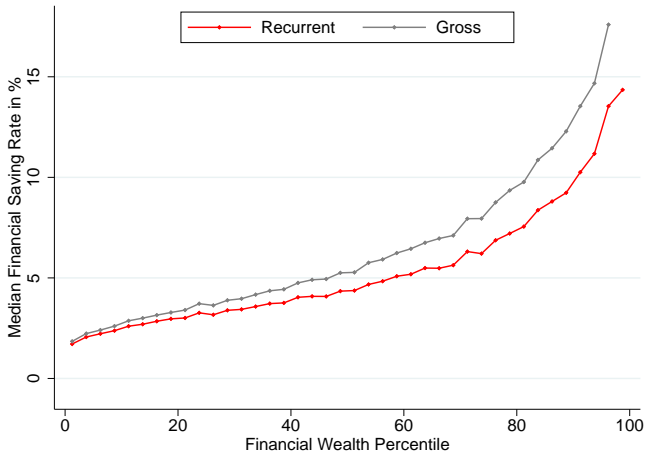
- similar patterns for net and gross saving rates?
- how do households treat capital gains on other assets?

Challenge: Norwegians hold few other assets with capital gains ▶ portfolios

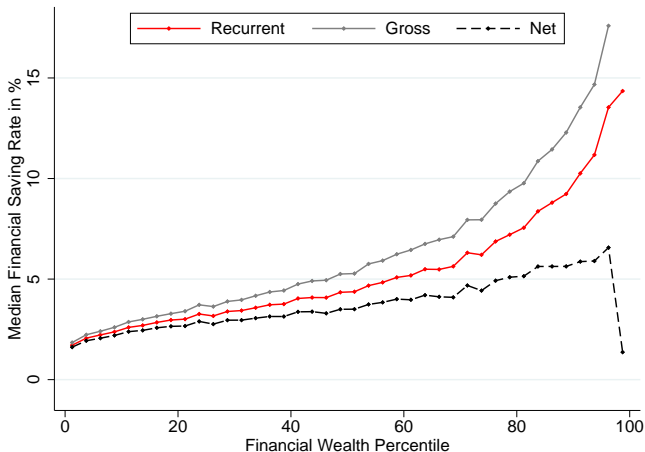
Solution: restrict to households with stocks $> 25\%$ of financial wealth

▶ Alternative exercise: drop all home owners

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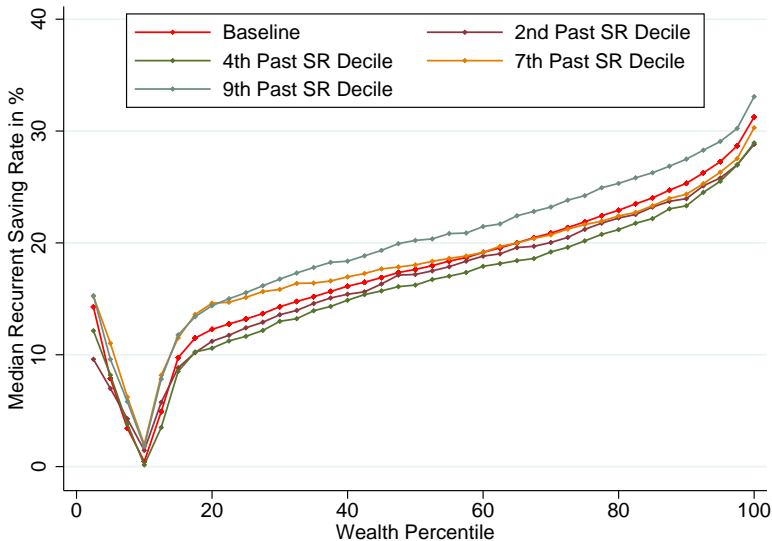


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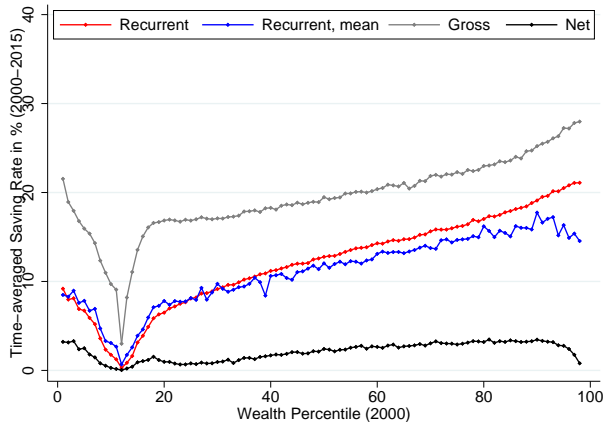
- Caveat: cannot use shareholder registry for stock fund holdings, use aggregate index \Rightarrow net saving biased if $\text{Cov}(a_i, \hat{p}_i) \neq 0$.
- Not just about housing. But smaller capital gains for other assets.

Simply High Saving Rate \Rightarrow High Wealth? No



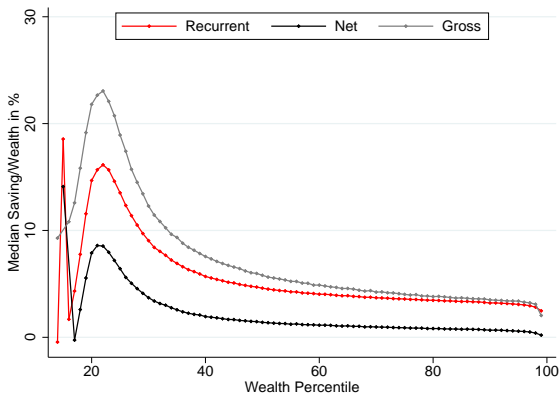
Saving Rates with Time Averaging

- Concern: medians of year-to-year saving rates may get it wrong if expenditure is “lumpy”
- Our solution: **time-average** saving rates **within individuals**



Aside: Saving as Fraction of Wealth (Bach-Calvet-Sodini)

$$\dot{a} = \frac{\rho - r}{\gamma} \left(\frac{w}{r} + a \right), \quad \frac{\dot{a}}{a} = \frac{\rho - r}{\gamma} \left(\frac{w}{ra} + 1 \right)$$



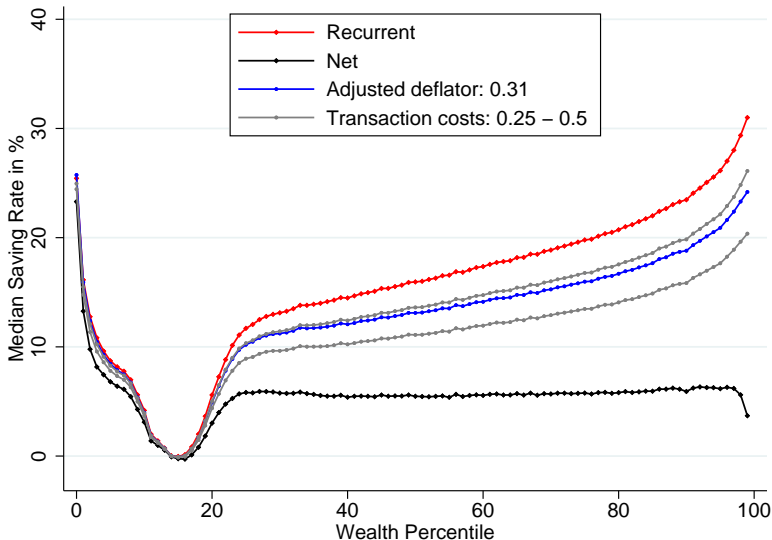
Consumption-Equivalent Saving Rates

- So far: **market values** of wealth, income, saving
 - But: market values may not reflect consumption, welfare
 - \Rightarrow try to translate market values into **consumption equivalents**
1. Housing is not just asset but also consumption good
 - really a matter of choosing the right **deflator** (Poterba, 2000)
 - construct new deflator with implicit rent \propto house price index
 2. Some assets are illiquid (housing, private firms,...)
 - may not want to count illiquid saving/income at market value
 - define effective saving and income ($\chi :=$ adj cost)

effective saving = liquid saving + $(1 - \chi) \times$ **illiquid saving**

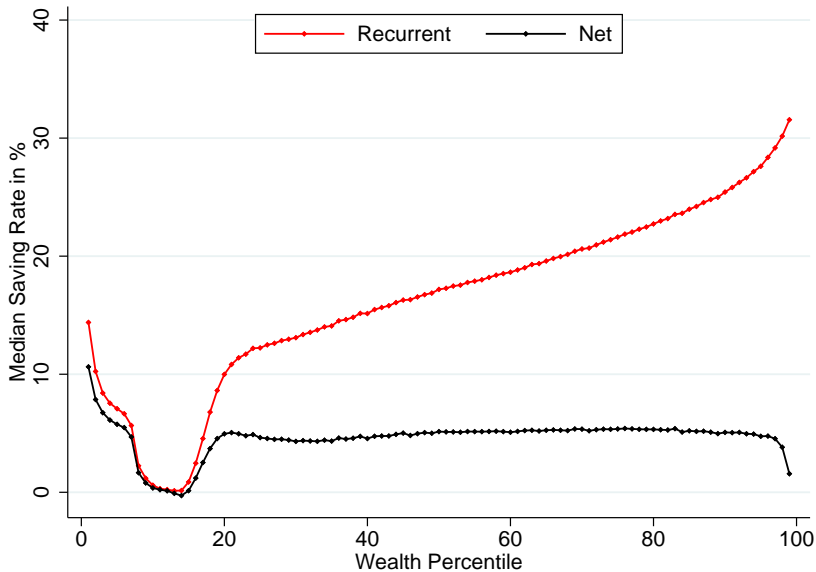
effective income = liquid income + $(1 - \chi) \times$ **illiquid income**

Patterns Remain even with Large Adjustments



Theoretical Interpretation

What explains joint pattern of net & recurrent saving?



What explains joint pattern of net & recurrent saving?

- Reduced form of all our explanations

$$\text{gross saving} = s_d(\text{disp income}) + s_c(\text{cap gains}) \quad s_d \ll s_c \approx 100\%$$

- Next slide: **multiple assets** + portfolio **adjustment** “frictions”
- Other potential explanations (not today)
 1. Capital gains driven by increased demand of asset holders (e.g. home owners experience housing preference shift)
 2. Non-homothetic preferences. But hard to explain flat net saving rate.
 3. (Unlikely) Wrong expectations about asset price changes: perceive all capital gains as transitory (ε rather than μ)
 4. ...

A Model with “Saving by Holding”

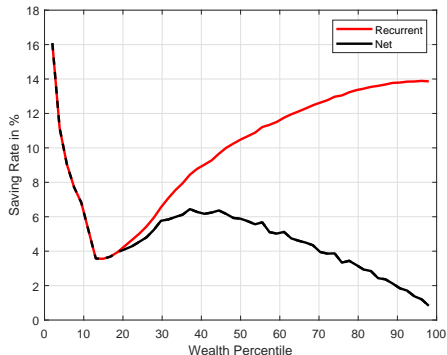
- Kaplan-Violante & Kaplan-Moll-Violante with twist = stochastic asset prices
- Two assets: consumption asset b and investment asset k

$$\dot{b} = w + r^b b + \theta p k - p d - c$$

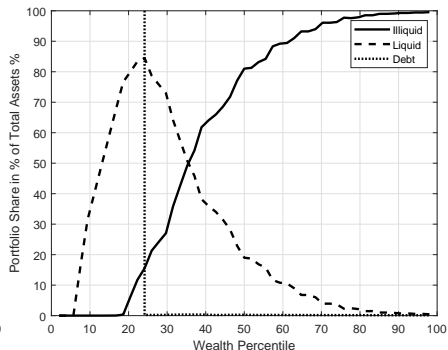
$$\dot{k} = d, \quad \frac{\dot{p}}{p} = \mu + \varepsilon$$

- + some reason for $d = 0$ most of the time
 - e.g. physical transaction cost but could be something else
 - tax on realizing capital gains, inattention, commitment,...
- + wedge between borrowing and saving rates $r_-^b > r_+^b$

The model with “saving by holding” can qualitatively explain the patterns



(e) Saving Rates



(f) Portfolio Shares

Note: assumes $r_-^b > r^a > r_+^b > \rho$ where $r^a := \theta + \mu$

Conclusion

- Little is known about the distribution of saving rates and how these vary across the wealth distribution
- We provide evidence using population tax records from Norway
- Results
 1. **net** saving rate \approx **flat** across wealth distribution
 2. **gross** saving rate **steeply increasing** with wealth
 3. close to 100% saving rate out of (persistent) capital gains
- Take-aways for theory
 - joint pattern for net & gross saving rates \neq workhorse models
 - fits with **multiple assets** + portfolio **adjustment “frictions”**
- Macro & wealth inequality literatures need to take into account changing asset prices!