

A Quantitative Analysis of Subsidy Competition in the U.S.

Ralph Ossa

University of Zurich and CEPR

January 2019

- Motivation

- US cities, counties, and states spend substantial resources on subsidies trying to attract firms from other locations
- Such subsidies had an annual cost of \$45 billion in 2015, equivalent to 30% of average state and local business taxes

- Objectives

- Understand what motivates regional governments to subsidize firm relocations and quantify how strong their incentives are
- Characterize fully non-cooperative and cooperative subsidy choices and assess how far away we are from these extremes

- Strategy

- I pursue these objectives in the context of a quantitative economic geography model which I calibrate to US states
- I calculate optimal subsidies, Nash subsidies, and cooperative subsidies and compare them to observed subsidies

- Findings

- I show that states have strong incentives to subsidize firm relocations in order to gain at the expense of other states
- Observed subsidies are closer to cooperative than non-cooperative subsidies but the potential losses from an escalation of subsidy competition are large

- Mechanism

- My model features agglomeration externalities in the New Economic Geography tradition which policymakers try to exploit
- Consumers want to be close to firms and firms want to be close to firms to have better access to final and intermediate goods

- Approach

- I try to strike a balance between transparency and realism to be able to clearly illustrate the main mechanism and yet obtain broadly credible quantitative results
- Analytical results are notoriously hard to derive in economic geography models and the standard practice has been to resort to simple numerical examples instead

- I am not aware of any comparable analysis of noncooperative and cooperative policy in a spatial environment
- Theoretical work such as Baldwin et al (2005) restricts attention to highly stylized models and does not connect to data
- Quantitative work such as Gaubert (2014), Suarez Serrato and Zidar (2016), and Fajgelbaum et al (2016) takes policy as given
- My modeling of agglomeration forces builds on Krugman (1991), Krugman and Venables (1995), and Allen and Arkolakis (2014)
- Methodologically most similar are the recent contributions by Ossa (2014), Fajgelbaum et al (2016), and Redding (2016)

- Model
- Calibration
- Analysis

- Preferences are common over goods and heterogeneous over amenities:

$$U_{jv} = U_j u_{jv}$$

$$U_j = \frac{A_j}{L_j} \left(\frac{T_j^R}{\mu} \right)^\mu \left(\frac{C_j^F}{1-\mu} \right)^{1-\mu}$$

$$C_j^F = \left(\sum_i \int_0^{M_i} c_{ij}^F(\omega_i)^{\frac{\epsilon-1}{\epsilon}} d\omega_i \right)^{\frac{\epsilon}{\epsilon-1}}$$

$$u_{jv} \sim \text{Frechet}(1, \sigma)$$

NB: Heterogeneity is necessary to allow for a meaningful sense in which states can benefit at the expense of one another

- Firms produce differentiated products using labor, capital, land, and intermediates:

$$q_j = \varphi_j (z_j - f_j)$$

$$z_j = \frac{1}{M_j} \left(\frac{1}{\eta} \left(\frac{L_j}{\theta^L} \right)^{\theta^L} \left(\frac{K_j}{\theta^K} \right)^{\theta^K} \left(\frac{T_j^C}{\theta^T} \right)^{\theta^T} \right)^\eta \left(\frac{C_j^I}{1-\eta} \right)^{1-\eta}$$

$$C_j^I = \left(\sum_i \int_0^{M_i} c_{ij}^I(\omega_i)^{\frac{\varepsilon-1}{\varepsilon}} d\omega_i \right)^{\frac{\varepsilon}{\varepsilon-1}}$$

$$1 = \theta^L + \theta^K + \theta^T$$

NB: Tax-financed cost subsidies would not work if there was only labor because then workers would essentially subsidize themselves

- Government objective

- In the non-cooperative regime, local governments maximize local expected utility, $E(U_{jv} | \text{living in } j)$, which amounts to maximizing U_j
- In the cooperative regime, the federal government maximizes national expected utility, $E(\max_j \{U_{jv}\})$, which amounts to maximizing $\left(\sum_{i=1}^R U_i^\sigma\right)^{\frac{1}{\sigma}}$

- Policy instruments

- Governments provide cost subsidies to local firms which they finance with lump-sum taxes on local residents
- These subsidies capture deviations from a benefit tax benchmark which includes statutory corporate tax rates

- The solution to the model can be expressed as a system of $4N$ equilibrium conditions in the $4N$ unknowns $\hat{\lambda}_i^L$, $\hat{\lambda}_i^K$, $\hat{\lambda}_i^C$, and \hat{P}_i
- It can be calibrated with minimal data requirements using the "exact hat algebra" approach of Dekle et al (2008)
- Following Allen and Arkolakis (2014), the model is isomorphic to an Armington model with external IRS technology if $\phi = \frac{1}{\varepsilon-1}$ and the technology is:

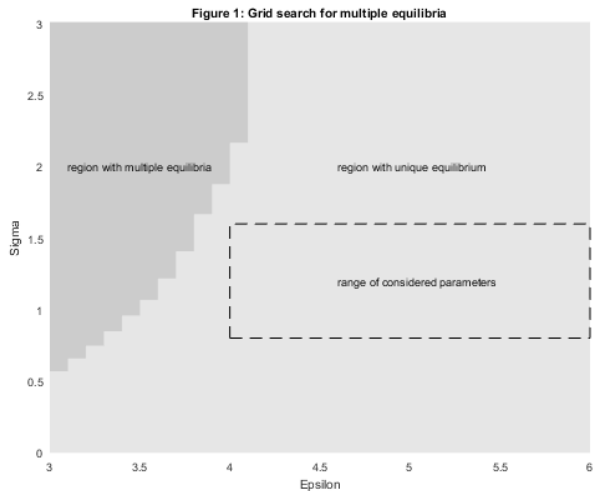
$$Q_i = \varphi_i (Z_i)^{1+\phi}$$

$$Z_i = \left(\frac{1}{\eta} \left(\frac{L_i}{\theta^L} \right)^{\theta^L} \left(\frac{K_i}{\theta^K} \right)^{\theta^K} \left(\frac{T_i^C}{\theta^T} \right)^{\theta^T} \right)^{\eta} \left(\frac{C_i^I}{1-\eta} \right)^{1-\eta}$$

- Business incentives databases of Bartik (2017) and Story et al (2012)
 - $\bar{s}_i = 0.5\%$, $s_i^{\min} = 0.0\%$ (CO), $s_i^{\max} = 3.8\%$ (NM) [▶ Map](#)
- 2007 Commodity Flow Survey
 - T_{ij}
- 2007 Annual Survey of Manufacturing
 - λ_i^L
- 2007 BEA Input-Output Table and BLS Capital Income Table
 - $\theta^L = 0.57$, $\theta^K = 0.33$, $\theta^T = 0.10$, $\eta = 0.58$
- Earlier work including Suarez Serrato and Zidar (2015) and Redding (2015)
 - $\sigma = 1.2$, $\mu = 0.25$, $\varepsilon = 5$

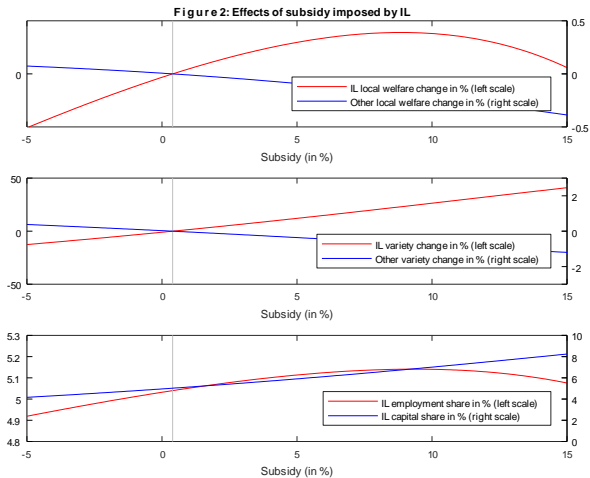
- I purge the trade data of the net exports due to nominal transfers so that subsidies cannot affect the real values of nominal transfers
- For this calculation, I work with a version of the model without labor mobility to preserve the original distribution of employment [▶ Details](#)
- I also allow for a federal subsidy on differentiated goods purchases in order to isolate the beggar-thy-neighbor aspects of state subsidies [▶ Details](#)

$$P_{ij} = \frac{\varepsilon}{\varepsilon - 1} \frac{\left((w_i)^{\theta^L} (i)^{\theta^K} (r)^{\theta^T} \right)^\eta (\rho^F P_i)^{1-\eta} \rho_i \tau_{ij}}{\varphi_i}$$



- The calibration procedure essentially pins down trade costs, amenities, and productivities such that manufacturing trade and employment are exactly matched
- Assuming $\tau_{ij} = \tau_{ji}$ and $\tau_{ii} = 1$, the model can be inverted and relative trade costs, amenities, and productivities can be backed out (as well as many other variables)
- It turns out that the variation in trade flows and manufacturing employment is mainly attributed to variation in trade costs and amenities, respectively [▶ Details](#)

Welfare effects of subsidy - Example



Welfare effects of subsidy - Decomposition

- Under certain restrictions, the welfare effects resulting from small subsidy changes can be decomposed into:

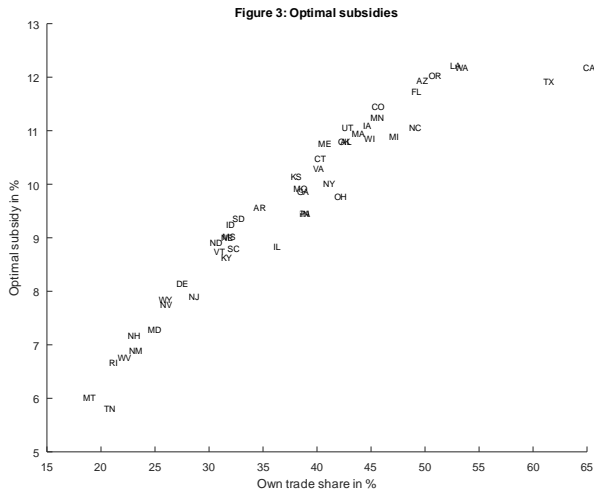
$$\frac{dU_j}{U_j} = \underbrace{\frac{1}{\eta} \sum_i \frac{X_{ij}}{E_j} \frac{1}{\varepsilon - 1} \frac{dM_i}{M_i}}_{\text{home market effect}} + \underbrace{\frac{1}{\eta} \sum_i \frac{X_{ij}}{E_j} \left(\frac{dp_j}{p_j} - \frac{dp_i}{p_i} \right)}_{\text{terms-of-trade effect}} - \underbrace{\mu \left(\frac{dr_j}{r_j} - \frac{dP_j}{P_j} \right)}_{\text{residential congestion}} - \underbrace{\theta^T \left(\frac{d\lambda_j^L}{\lambda_j^L} - \frac{d\lambda_j^C}{\lambda_j^C} \right)}_{\text{commercial congestion}}$$

- The terms-of-trade effect can be further decomposed into:

$$\underbrace{\theta^L \sum_i \frac{X_{ij}}{E_j} \left(\frac{dw_j}{w_j} - \frac{dw_i}{w_i} \right)}_{\text{relative wage effect}} + \underbrace{\theta^T \sum_i \frac{X_{ij}}{E_j} \left(\frac{dr_j}{r_j} - \frac{dr_i}{r_i} \right)}_{\text{relative rent effect}} + \underbrace{\frac{1}{\eta} \sum_i \frac{X_{ij}}{E_j} \left(\frac{d\rho_j}{\rho_j} - \frac{d\rho_i}{\rho_i} \right)}_{\text{direct subsidy effect}} + \underbrace{\frac{1-\eta}{\eta} \sum_i \frac{X_{ij}}{E_j} \left(\frac{dP_j}{P_j} - \frac{dP_i}{P_i} \right)}_{\text{intermediate cost effect}}$$

- For example, if IL unilaterally imposes a 5 percent subsidy, the approximate welfare effects are:

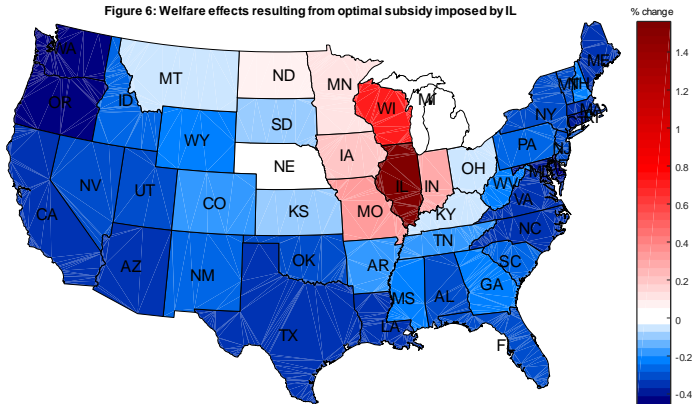
| | U | HME | TOT | CON | TOT _w | TOT _r | TOT _s | TOT _{int} | CON _{res} | CON _{com} |
|----|------|------|------|-------|------------------|------------------|------------------|--------------------|--------------------|--------------------|
| IL | 1.2% | 1.6% | 1.0% | -1.4% | 5.4% | 0.5% | -4.5% | -0.3% | -2.1% | 0.7% |



NB: Optimal subsidies average 9.6% or \$14.9 billion

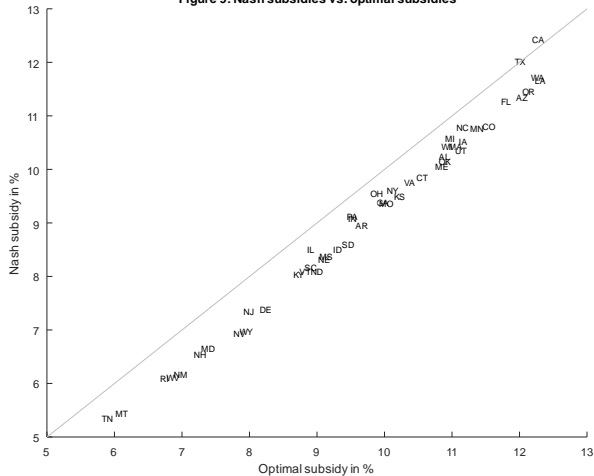
Optimal subsidies IL - Geography of welfare effects

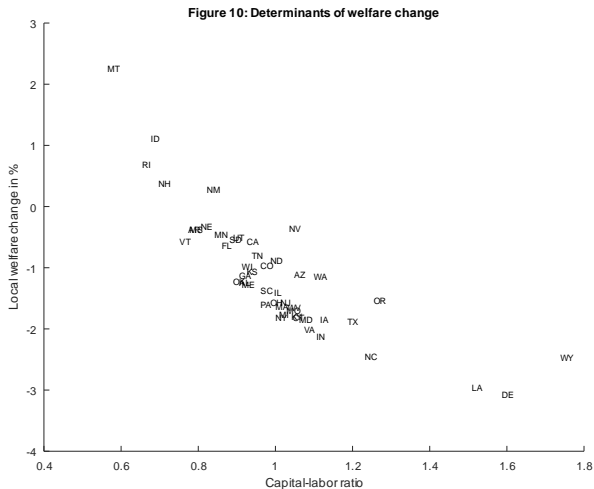
Figure 6: Welfare effects resulting from optimal subsidy imposed by IL



► Sensitivity

Figure 9: Nash subsidies vs. optimal subsidies

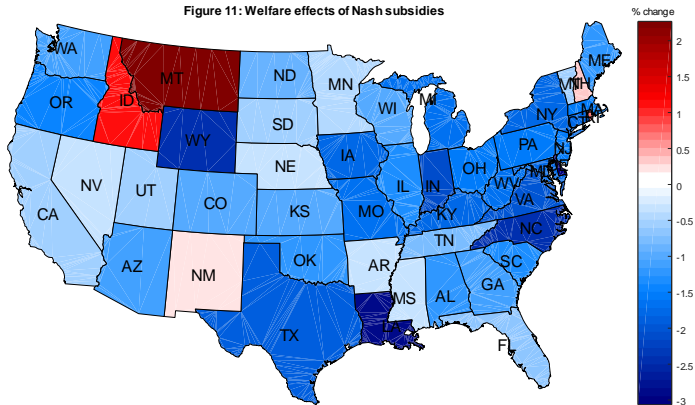




NB: Local welfare falls by -1.1% on average which adds up to a nationwide loss of -\$30.9 billion

Nash subsidies - Geography of welfare effects

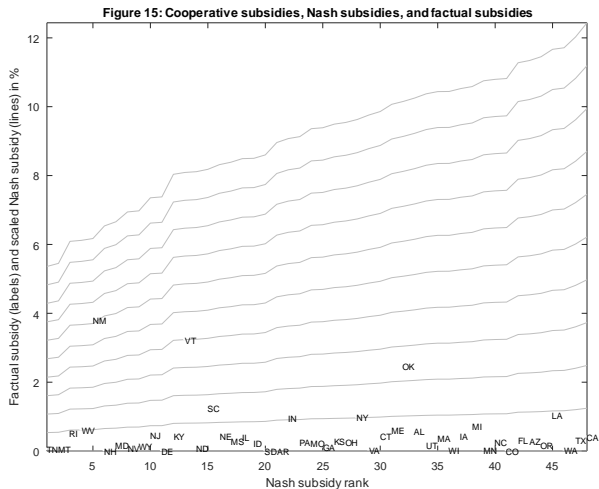
Figure 11: Welfare effects of Nash subsidies



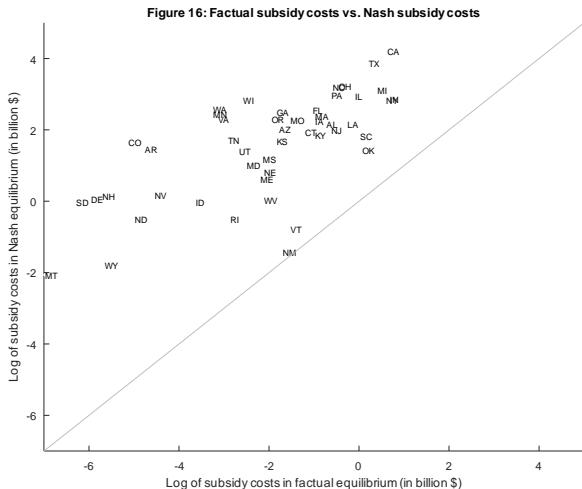
► Sensitivity

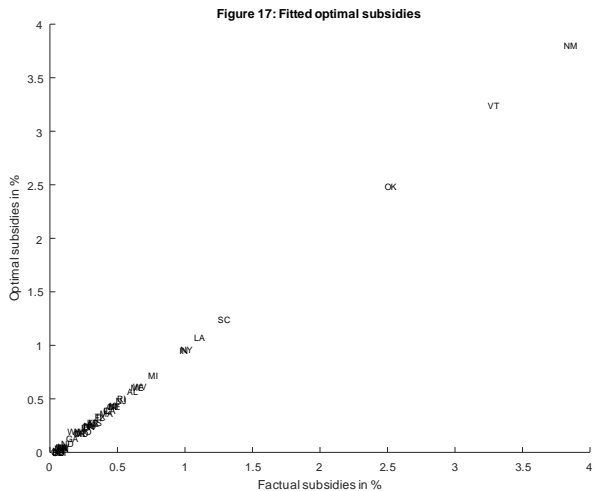


- If the federal government maximizes expected welfare, it sets all subsidies equal to zero and uses transfers to reduce inequality
- Starting at factual subsidies, this increases expected welfare by 0.5% which amounts to a gain of \$11.4 billion for the entire country
- Almost the entire effect is due to the use of transfers, just setting subsidies to zero brings about a total gain of only \$50.7 million
- If the federal government was not allowed to make transfers, it would mimic them by cooperatively manipulating the terms-of-trade



Observed vs. counterfactual subsidy costs





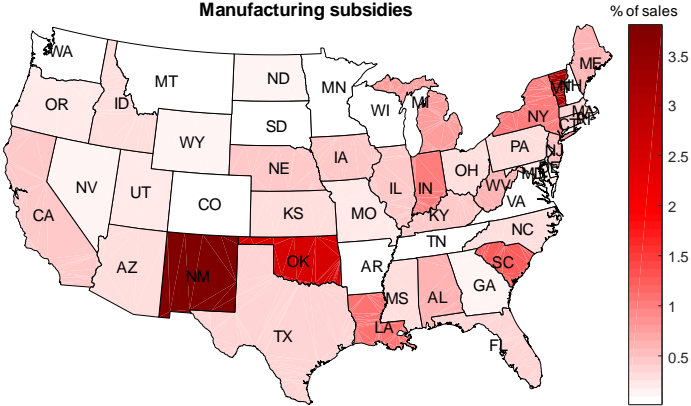
► Nash

Fitted subsidies - Own welfare weights

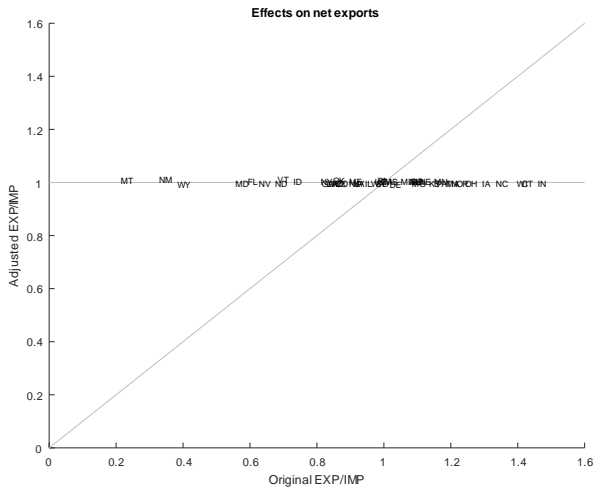
| Own welfare weights | | | |
|---------------------|------------|-------|------------|
| State | Weight (%) | State | Weight (%) |
| IN | 0.54 | MS | 0.05 |
| NY | 0.52 | GA | 0.05 |
| CA | 0.41 | KS | 0.05 |
| OK | 0.40 | RI | 0.04 |
| SC | 0.38 | AZ | 0.04 |
| MI | 0.37 | ME | 0.03 |
| IL | 0.29 | MD | 0.03 |
| TX | 0.20 | TN | 0.03 |
| NJ | 0.20 | OR | 0.02 |
| NM | 0.19 | WI | 0.02 |
| OH | 0.17 | UT | 0.02 |
| PA | 0.16 | ID | 0.01 |
| VT | 0.15 | MN | 0.01 |
| AL | 0.14 | VA | 0.01 |
| KY | 0.12 | WA | 0.01 |
| LA | 0.11 | NV | 0.00 |
| NC | 0.10 | AR | 0.00 |
| FL | 0.10 | MT | 0.00 |
| MA | 0.09 | NH | 0.00 |
| IA | 0.08 | ND | 0.00 |
| CT | 0.08 | CO | 0.00 |
| MO | 0.06 | SD | 0.00 |
| WV | 0.05 | DE | 0.00 |
| NE | 0.05 | WY | 0.00 |

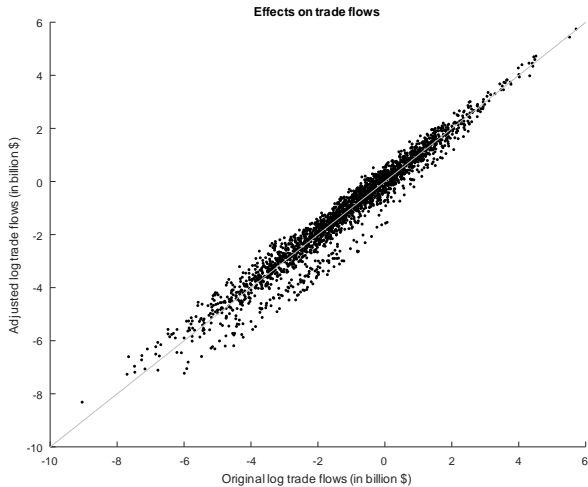
▶ More

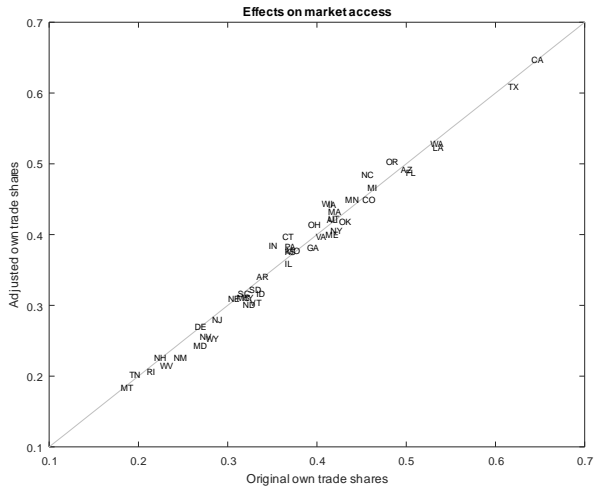
- I analyze subsidy wars and subsidy talks among US states using a quantitative economic geography model
- I believe this is the first quantitative analysis of noncooperative and cooperative policy in a spatial environment
- I show that states have strong incentives to subsidize firm relocations in order to gain at the expense of other states
- Observed subsidies are closer to cooperative than non-cooperative subsidies but the potential losses from an escalation of subsidy competition are large



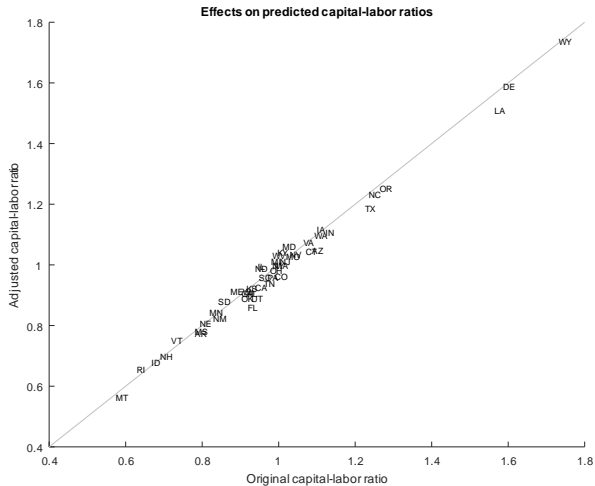
▶ Back

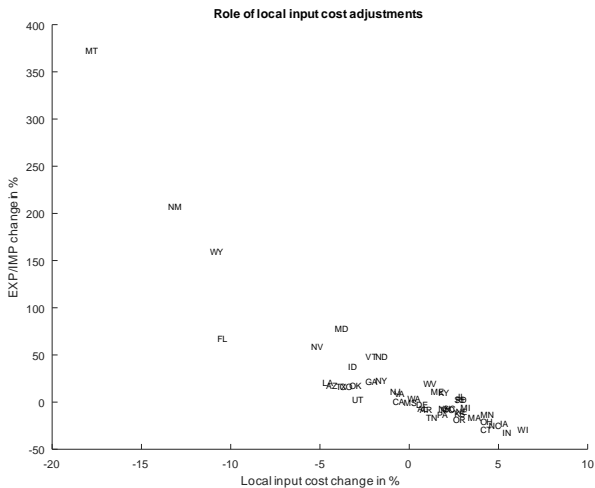






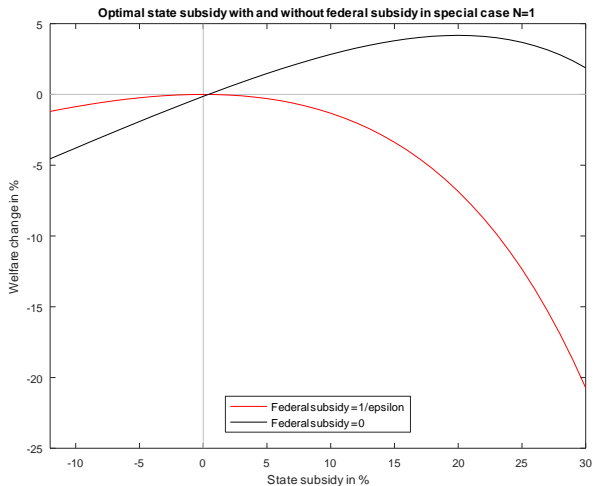
Adjustment I - Transfers



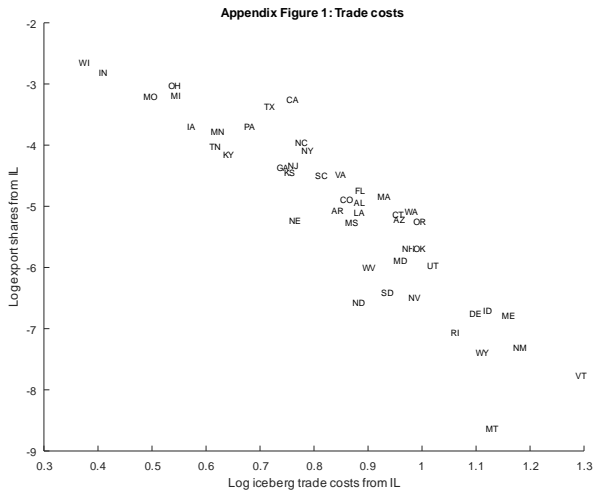


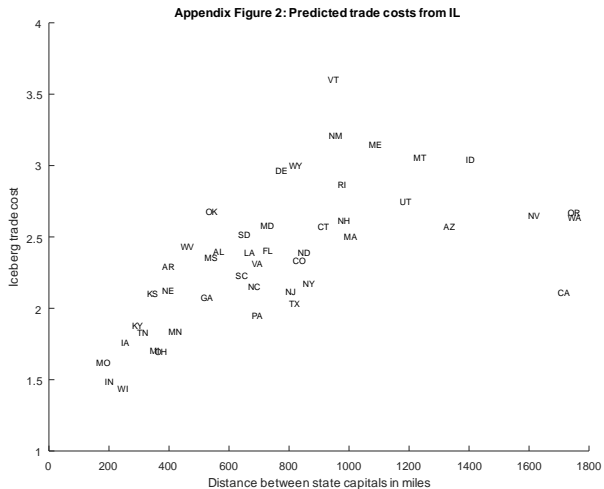
▶ Back

Adjustment II - Federal subsidy

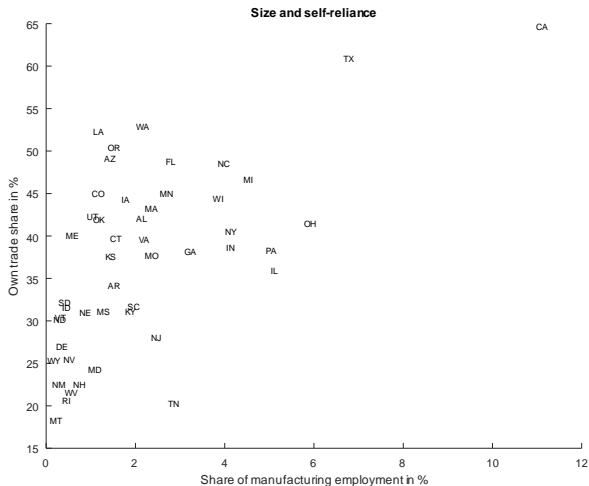


▶ Back



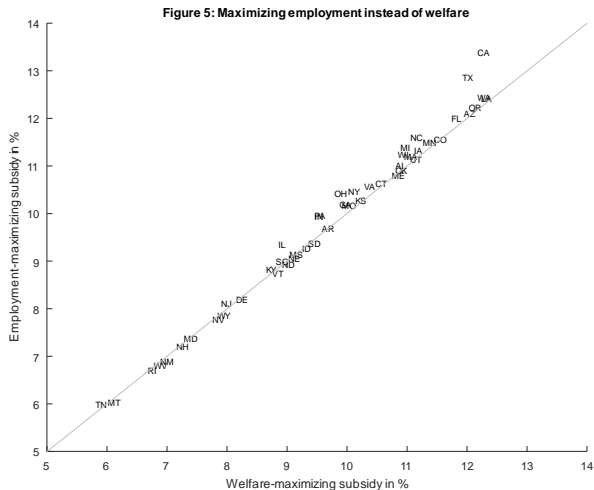


Optimal subsidies - Determinants of own trade share



▶ Back

Optimal subsidies - Maximizing employment



▶ Back

Sensitivity wrt. sigma

| σ | subsidy | | Δ welfare | | $\Delta\lambda^t$ |
|----------|---------|-----|------------------|----------|-------------------|
| | avg | own | other | expected | avg. |
| 0.80 | 9.6 | 2.2 | -0.2 | -0.1 | 1.8 |
| 1.20 | 9.6 | 2.2 | -0.2 | -0.1 | 2.7 |
| 1.60 | 9.7 | 2.1 | -0.2 | -0.1 | 3.5 |

Sensitivity wrt. epsilon

| ϵ | subsidy | | Δ welfare | | $\Delta\lambda^t$ |
|------------|---------|-----|------------------|----------|-------------------|
| | avg | own | other | expected | avg. |
| 4.00 | 13.0 | 6.7 | -0.7 | -0.3 | 8.5 |
| 5.00 | 9.6 | 2.2 | -0.2 | -0.1 | 2.7 |
| 6.00 | 7.8 | 1.1 | -0.1 | 0.0 | 1.3 |

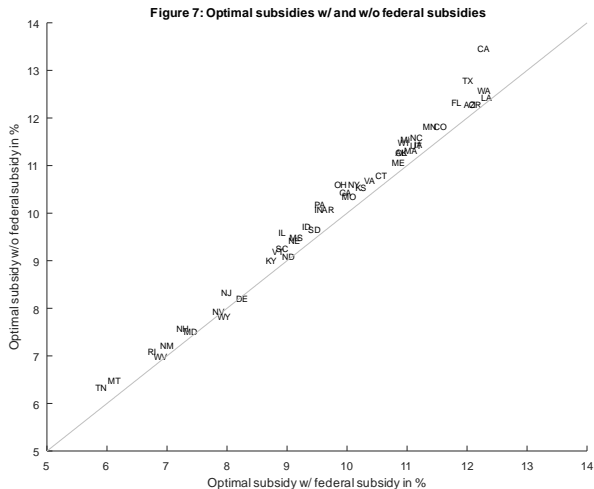
Sensitivity wrt. phi

| ϕ | subsidy | | Δ welfare | | $\Delta\lambda^t$ |
|--------|---------|------|------------------|----------|-------------------|
| | avg | own | other | expected | avg. |
| 0.33 | 16.4 | 15.7 | -1.5 | -0.6 | 20.2 |
| 0.25 | 9.6 | 2.2 | -0.2 | -0.1 | 2.7 |
| 0.20 | 5.6 | 0.5 | 0.0 | 0.0 | 0.7 |

Optimal subsidies - Sensitivity

Sensitivity wrt. intial subsidies

| state | subsidy | | state | subsidy | |
|-------|---------|------|-------|---------|------|
| | min | max | | min | max |
| AL | 10.6 | 10.8 | NE | 8.7 | 9.1 |
| AZ | 11.7 | 12.0 | NV | 7.4 | 7.8 |
| AR | 9.3 | 9.6 | NH | 6.9 | 7.2 |
| CA | 12.2 | 12.3 | NJ | 7.7 | 8 |
| CO | 11.2 | 11.5 | NM | 6.9 | 7.2 |
| CT | 10.2 | 10.5 | NY | 9.9 | 10.1 |
| DE | 7.8 | 8.2 | NC | 10.9 | 11.1 |
| FL | 11.5 | 11.8 | ND | 8.6 | 8.9 |
| GA | 9.6 | 9.9 | OH | 9.6 | 9.8 |
| ID | 8.9 | 9.3 | OK | 10.7 | 11 |
| IL | 8.7 | 8.9 | OR | 11.8 | 12 |
| IN | 9.3 | 9.5 | PA | 9.3 | 9.5 |
| IA | 10.9 | 11.1 | RI | 6.4 | 6.7 |
| KS | 9.9 | 10.2 | SC | 8.6 | 8.9 |
| KY | 8.4 | 8.7 | SD | 9 | 9.4 |
| LA | 12.1 | 12.3 | TN | 5.6 | 5.8 |
| ME | 10.5 | 10.8 | TX | 11.9 | 12 |
| MD | 7.0 | 7.3 | UT | 10.8 | 11.1 |
| MA | 10.7 | 11.0 | VT | 8.7 | 9 |
| MI | 10.8 | 10.9 | VA | 10 | 10.3 |
| MN | 11.0 | 11.3 | WA | 12 | 12.2 |
| MS | 8.7 | 9.1 | WV | 6.5 | 6.8 |
| MO | 9.7 | 9.9 | WI | 10.6 | 10.9 |
| MT | 5.7 | 6.0 | WY | 7.5 | 7.9 |



Sensitivity wrt. sigma

| σ | subsidy | | Δ welfare | | $\Delta\lambda^L$ |
|----------|---------|-----------|------------------|------|-------------------|
| | avg. | incumbent | expected | avg. | |
| 0.80 | 9.1 | -1.1 | -1.3 | 0.2 | |
| 1.20 | 9.1 | -1.1 | -1.3 | 0.3 | |
| 1.60 | 9.1 | -1.1 | -1.3 | 0.4 | |

Sensitivity wrt. epsilon

| ϵ | subsidy | | Δ welfare | | $\Delta\lambda^L$ |
|------------|---------|-----------|------------------|------|-------------------|
| | avg. | incumbent | expected | avg. | |
| 4.00 | 11.7 | -2.8 | -3.2 | 0.6 | |
| 5.00 | 9.1 | -1.1 | -1.3 | 0.3 | |
| 6.00 | 7.5 | -0.6 | -0.7 | 0.2 | |

Sensitivity wrt. phi

| ϕ | subsidy | | Δ welfare | | $\Delta\lambda^L$ |
|--------|---------|-----------|------------------|------|-------------------|
| | avg. | incumbent | expected | avg. | |
| 0.33 | 14.9 | -4.5 | -4.9 | 0.5 | |
| 0.25 | 9.1 | -1.1 | -1.3 | 0.3 | |
| 0.20 | 5.3 | -0.3 | -0.4 | 0.2 | |

Nash subsidies - Sensitivity

Sensitivity to initial subsidies

| state | min | max | state | min | max |
|-------|------|------|-------|------|------|
| AL | 10.0 | 10.4 | NE | 8.0 | 8.4 |
| AZ | 11.1 | 11.4 | NV | 6.6 | 7.1 |
| AR | 8.6 | 9.0 | NH | 6.2 | 6.6 |
| CA | 12.4 | 12.5 | NJ | 7.1 | 7.5 |
| CO | 10.5 | 10.9 | NM | 6.2 | 6.5 |
| CT | 9.6 | 10.0 | NY | 9.4 | 9.8 |
| DE | 7.1 | 7.5 | NC | 10.6 | 10.9 |
| FL | 11.1 | 11.3 | ND | 7.8 | 8.2 |
| GA | 9.1 | 9.5 | OH | 9.3 | 9.6 |
| ID | 8.2 | 8.6 | OK | 10.0 | 10.4 |
| IL | 8.3 | 8.6 | OR | 11.2 | 11.6 |
| IN | 8.9 | 9.2 | PA | 8.9 | 9.2 |
| IA | 10.3 | 10.6 | RI | 5.8 | 6.2 |
| KS | 9.2 | 9.6 | SC | 8.0 | 8.4 |
| KY | 7.8 | 8.1 | SD | 8.3 | 8.7 |
| LA | 11.5 | 11.8 | TN | 5.1 | 5.4 |
| ME | 9.8 | 10.2 | TX | 11.9 | 12.0 |
| MD | 6.4 | 6.8 | UT | 10.1 | 10.5 |
| MA | 10.2 | 10.5 | VT | 8.0 | 8.4 |
| MI | 10.4 | 10.7 | VA | 9.5 | 9.8 |
| MN | 10.5 | 10.8 | WA | 11.5 | 11.8 |
| MS | 8.1 | 8.5 | WV | 5.9 | 6.2 |
| MO | 9.1 | 9.4 | WI | 10.2 | 10.5 |
| MT | 5.2 | 5.5 | WY | 6.7 | 7.1 |

Figure 12: Nash subsidies w/ and w/o federal subsidies

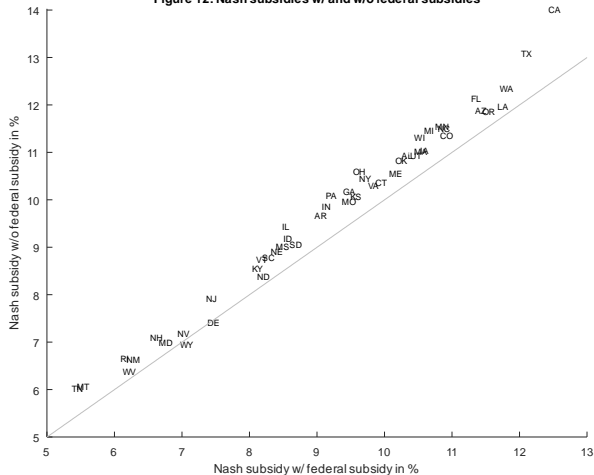
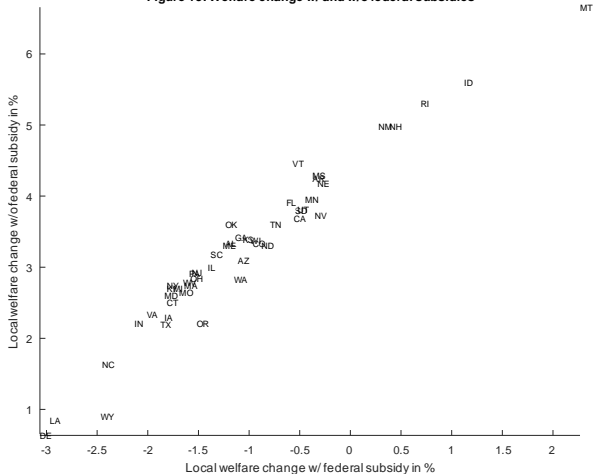


Figure 13: Welfare change w/ and w/o federal subsidies



▶ Back

Cooperative subsidies - Sensitivity

Sensitivity wrt. sigma

| σ | subsidy | Δ welfare | | $\Delta\lambda^L$ avg. |
|----------|---------|------------------|----------|---------------------------|
| | | incumbent | expected | |
| 0.80 | 0.0 | 2.7 | 0.5 | 1.6 |
| 1.20 | 0.0 | 2.3 | 0.5 | 2.2 |
| 1.60 | 0.0 | 2.0 | 0.5 | 2.7 |

Sensitivity wrt. epsilon

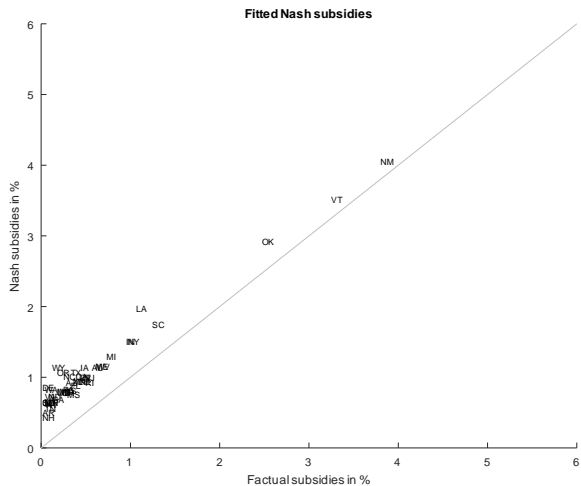
| ϵ | subsidy | Δ welfare | | $\Delta\lambda^L$ avg. |
|------------|---------|------------------|----------|---------------------------|
| | | incumbent | expected | |
| 4.00 | 0.0 | 3.6 | 0.8 | 3.5 |
| 5.00 | 0.0 | 2.3 | 0.5 | 2.2 |
| 6.00 | 0.0 | 1.8 | 0.4 | 1.7 |

Sensitivity wrt. phi

| ϕ | subsidy | Δ welfare | | $\Delta\lambda^L$ avg. |
|--------|---------|------------------|----------|---------------------------|
| | | incumbent | expected | |
| 0.33 | 0.0 | 2.9 | 0.8 | 2.8 |
| 0.25 | 0.0 | 2.3 | 0.5 | 2.2 |
| 0.20 | 0.9 | 2.4 | 0.4 | 2.5 |

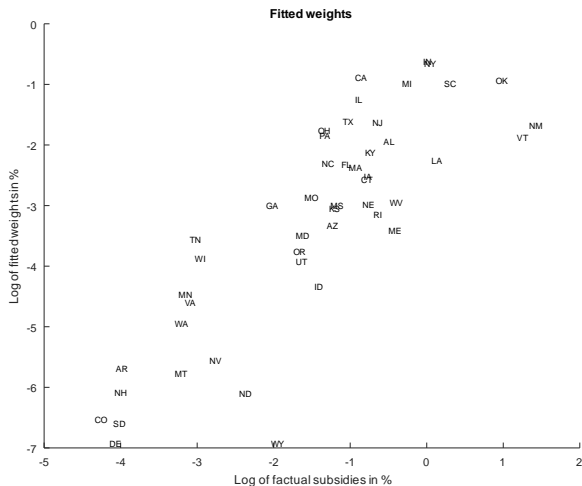
NB: Without federal subsidies, the cooperative subsidy would be set to undo the markup distortion

Fitted subsidies - Nash



▶ Back

Fitted subsidies - Weights



▶ Back