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## Abstract

This paper studies how global macroeconomic conditions affect sovereign bond prices.

Weak and volatile economic performance during recessions increases a country's default probability more than strong and stable performance during expansions reduces it, leading to countercyclical and unconditionally high sovereign credit spreads.

**We identify the sovereign bond premium arising from this exposure to severe but low-frequency changes in global macroeconomic conditions.**

Our model predicts that this bond premium is higher for countries that are more exposed to the global business cycle, particularly around recessions. We find support for this prediction using emerging market sovereign bond data over the 1994Q1-2018Q2 period.

## Introduction

The 2007-9 crisis has renewed interest in understanding the role of business cycles in finance (e.g., Bloom et al., 2018).

Empirically, we observe that:

- Most countries are exposed to the global business cycle.
  - Lower output growth and higher volatility during global recessions
  - Strong heterogeneity across countries
- This exposure is known to affect sovereign risk.
  - Higher probability of sovereign default in recession
  - Greater sovereign credit spreads (Augustin and Tedongap, 2016)

**How does it impact expected excess bond returns?**

## Economic environment

The stream of **consumption** follows:

$$\frac{dC_t}{C_t} = \mu_{c,s_t} dt + \sigma_{c,s_t} dZ_{c,t}, \quad s_t = \{L, H\}$$

where  $\mu_{c,H} > \mu_{c,L}$  and  $\sigma_{c,H} < \sigma_{c,L}$ .  $s_t$  is the state of the economy expansion (H) or recession (L). The agent has **Epstein-Zin preferences** with a state-price density  $\pi_t$ :

$$\pi_t = (\beta e^{-\beta t})^{1-\frac{1}{\psi}} C_t^{-\gamma} \left( p_{c,t} e^{\int_0^t p_{c,u}^{-1} du} \right)^{\frac{1}{\psi}}$$

where  $\gamma$  is the RRA's coefficient,  $\psi$  the EIS of consumption,  $\beta$  the time discount factor, and  $p_{c,t}$  the price-consumption ratio. When  $\psi > 1$ ,  $p_{c,t}$  is procyclical.

The **dynamic of country  $i$ 's revenue**:

$$\frac{dY_{i,t}}{Y_{i,t}} = \mu_{Y,s_t} dt + \sigma_{Y,s_t} dZ_t, \quad s_t = \{L, H\}$$

where  $\mu_{Y,s_t} = \mu_{X,s_t}$  and  $\sigma_{Y,s_t} = \eta \sigma_{X,s_t}$ ,  $\mu_{X,s_t}$  and  $\sigma_{X,s_t}$  are the conditional expected growth rate and the conditional volatility of output, and  $\eta > 1$  amplifies the volatility of government revenue relative to output growth volatility.

## Sovereign Bond Valuation

The government defaults on its debt when its revenue  $Y_{i,t}$  falls to a state-dependent default thresholds  $Y_{D,i,s_D}$ ,  $s_D = \{L, H\}$ . When the government defaults on its bond, at a time denoted by  $t_{D,i}$  the coupon  $c_i$  is reduced by a fraction  $\kappa \in (0, 1)$  due to debt restructuring. The **bond value** is:

$$B_{i,s_t} = E_t \left[ \int_t^{t_{D,i}} c_i \frac{\pi_u}{\pi_t} du \middle| s_t \right] + E_t \left[ \int_{t_{D,i}}^{\infty} (1-\kappa) c_i \frac{\pi_u}{\pi_t} du \middle| s_t \right], \quad s_t = \{L, H\}$$

**Optimal decisions:** Find  $c_{i,s_0}$  and  $Y_{D,i,s_D}$

$$\text{Sovereign wealth} = W_{i,s_t}(Y_{i,s_t}) \\ = \text{Return on public in investment} + \text{fiscal revenue}$$

$$c_{i,s_0} = \arg \max W_{i,s_0} \text{ s.t. } \frac{\partial (W_{i,s_t} - B_{i,s_t})}{\partial Y_{i,t}} \bigg|_{Y_t = Y_{D,i,s_D}} = \frac{\partial}{\partial Y_{D,i,s_D}} (W_{i,s_t} - B_{i,s_t} |_{Y_t = Y_{D,i,s_D}})$$

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## Sovereign Bond Premium

The **sovereign bond premium**  $BP_{i,s_t}$  in state  $s_t$ :

$$BP_{i,s_t} = \underbrace{\rho_{i,s_t} \theta_{i,s_t}^B \sigma_{i,s_t}^B}_{\text{due to conso shocks or Short-run risk}} + \underbrace{\lambda_{s_t} \theta_{i,s_t}^J \sigma_{i,s_t}^J}_{\text{due to changes of state or Long-run risk}}, \quad s_t = \{L, H\}$$

- $\rho_{i,s_t}$  is the output-consumption correlation,  $\theta_{i,s_t}^B = \gamma \sigma_{c,s_t}$  the price of consumption shocks,  $\sigma_{i,s_t}^B$  the volatility of sovereign bond returns;
- $\lambda_{s_t}$  is the probability of leaving state  $s_t$ ,  $\theta_{i,s_t}^J = 1 - \frac{\pi_j}{\pi_{s_t}}$  is the price of risk due to the change of state from  $s_t$  to  $j$ ,  $\sigma_{i,s_t}^J = \frac{B_{i,j}}{B_{i,s_t}} - 1$  the change in bond valuation caused by the change of state.

## Predictions

	Short-run risk	Long-run risk	Total
Risk premium (bps)	4.76	55.53	60.29
Percentage (%)	7.90	92.10	100

Table 1. Sovereign bond premium decomposition.

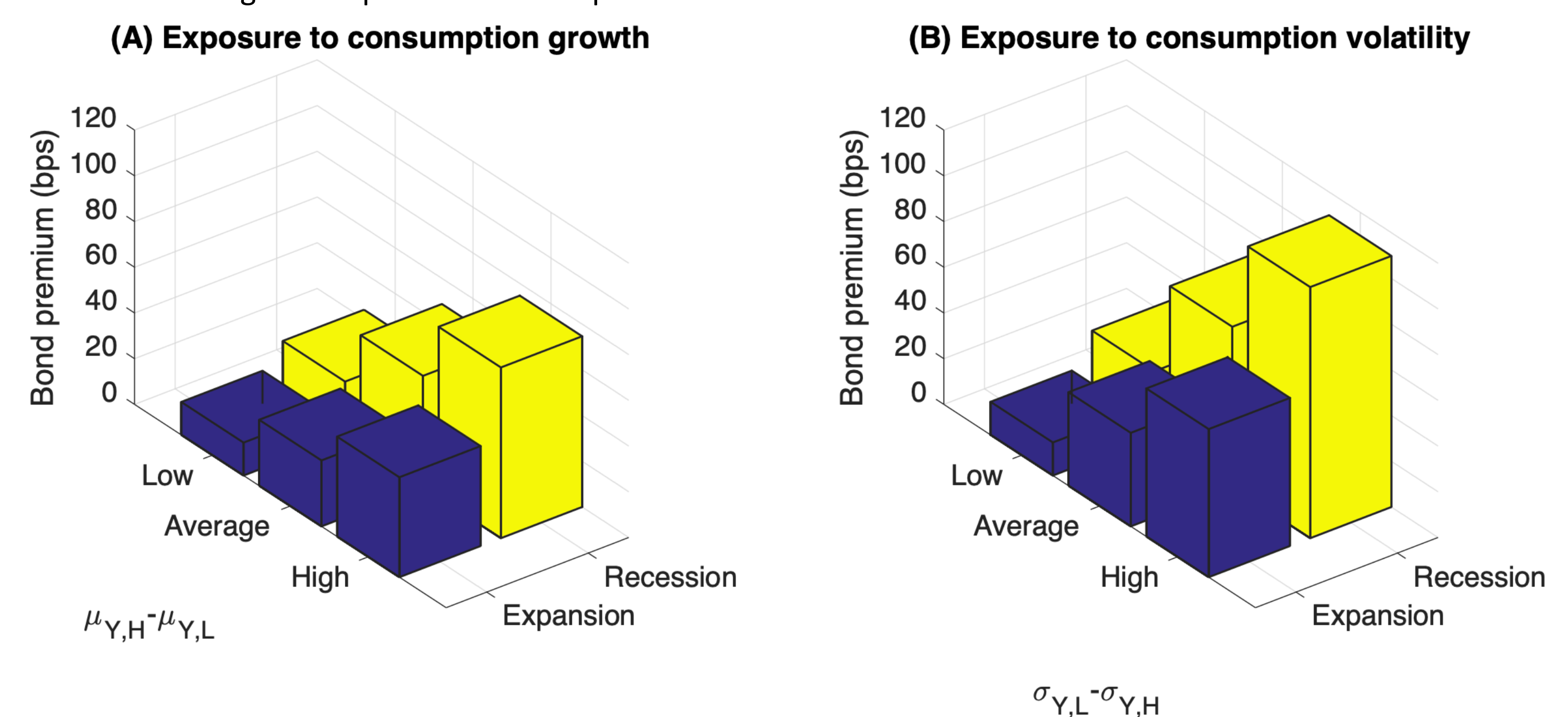


Figure 1. Sovereign bond premium and cross-sectional predictions.

## Empirical evidence

Regression

$$R_{i,t}^e = \alpha_{i,t} + \beta_{i,t}^c \Delta \hat{c}_t + \beta_{i,t}^\mu \Delta \hat{\mu}_{c,t} + \beta_{i,t}^\sigma \Delta \hat{\sigma}_{c,t}$$

- $R_{i,t}^e$  is the country  $i$ 's bond excess returns,  $\Delta \hat{\mu}_{c,t}$  is the consumption shocks,  $\Delta \hat{\mu}_{c,t}$  the change in expected conso growth and  $\Delta \hat{\sigma}_{c,t}$  the change in expected conso volatility.

Exposure		Low		High		High - Low
		$\beta^c$	$\beta^\mu$	$\beta^c$	$\beta^\mu$	
$\beta^c$	Excess returns	2.87	1.61	1.67	2.26	-0.61
	t-stat	3.41	4.31	4.85	4.58	-0.67
$\beta^\mu$	Excess returns	2.09	1.59	1.75	3.02	0.94
	t-stat	3.67	3.65	4.81	5.19	1.91
$\beta^\sigma$	Excess returns	3.52	1.90	1.70	1.35	-2.17
	t-stat	4.23	4.68	4.56	3.80	-2.87

Table 2. Portfolio formed on exposure to each source of risk (annualized individual estimation).

## Conclusions

We uncover a new sovereign bond premium arising from a country's exposure to the global business cycle, which differs from the exposure to higher-frequency global economic shocks.

Investors buying bonds with high long-run macro risk and selling bonds with low long-run macro risk obtain a sizable excess return.

## References

1. Bloom, N., Floetotto, M., Jaimovich, N., Saporta-Eksten, I., and Terry, S. J. 2018, Really Uncertain Business Cycles, *Econometrica* 86(3), 1031-1065.
2. Augustin, P., and Tedongap, R., 2016, Real Economic Shocks and Sovereign Credit Risk, *Journal of Financial and Quantitative Analysis* 51(2), 541-587.