

# Risky Business Cycles

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Susanto Basu - *Boston College*

Ryan Chahrour - *Boston College*

Giacomo Candian - *HEC Montréal*

Rosen Valchev - *Boston College*

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# Motivation

Financial economists tell us that excess returns are predictable.

*Discount-rate variation is the central organizing question of current asset-pricing research.*

John Cochrane - 2011 Presidential Address to American Fin. Assoc.

This fact is not part of most theories of macroeconomic fluctuations.

Cycles driven by risk promising, but most models imply

- precautionary increase in savings/investment
- precautionary labor supply increase
- very hard to get comovement between  $Y, C, I, N$   
(not-to-mention asset prices)

## 1. Empirical patterns associated with changes in expected returns

- Strong comovement of  $Y$ ,  $C$ ,  $I$  and labor
- Shifts towards part-time/flexible-contract workers
- Small changes in safe interest rates

## 2. Provide theory of these patterns

- Core idea: if safe stores are less productive, then fear  $\rightarrow$  recession
- Between markets: labor relationships more risky than capital investment
- Within markets: long-term labor relationships more risky than part-time/contract work

- **Time-varying Risk-Premia:** Campbell and Shiller (1988), Fama and French (1989), Cochrane (2011), Martin (2017), ...
- **Risk and labor market frictions:** Petrosky-Naudau et. al. (2015), Flavilikus and Lin (2016), Leduc and Liu (2016), Hall (2017), Schaal (2017), Swanson (2019), Cacciatore and Ravenna (2020), Kehoe et al. (2020), ...
- **Uncertainty and RBC:** Bachmann and Bayer (2013), Bloom et. al. (2014), Gilchrist et al. (2014), Di Tella and Hall (2020), ...
- **Uncertainty in models with nominal frictions:** Ilut and Schneider (2014), Christiano et al. (2014), Fernandez-Villaverde, Guerron-Quintana, Kuester, and Rubio-Ramirez (2015), Basu and Bundick (2017), ...
- **Max-share empirical strategy:** Uhlig (2003), Angeletos, Collard and Dellas (2020)

1. Empirical Patterns
2. Theory: Real model with Two Labor Types
3. Quantification and Inspecting the Mechanism

# **Risk Premia and Business Cycles in the Data**

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In aggregate data...

- VAR using standard macro series and equity/bond returns
- Identify shock which drives bulk of excess returns
- Look at comovements with real variables, labor markets, etc.

Sample Period: 1985Q1 - 2018Q4

Core series:  $Y_t$

- Real per-capita output
- Real per-capita consumption
- Real per-capita investment
- Real per-capita hours
- Real stock return (incl. dividends)
- Real bond return
- Dividend-price ratio

Auxiliary Series:  $S_t$

- Employment (part-time vs full-time)
- Others



# Empirical Approach

Statistical Model:

$$Y_t = B(L)Y_{t-1} + \underbrace{A\epsilon_t}_{\mu_t} \quad (\text{Core})$$

$$S_t = \Gamma(L)Y_t + v_t \quad (\text{Aux})$$

Risk premium definition:

$$rp_{t,t+j} \equiv [r_{t+1}^s + r_{t+2}^s + \dots + r_{t+j}^s] - [r_{t+1}^b + r_{t+2}^b + \dots + r_{t+j}^b]$$

Using expectation implied by VAR:

$$E_t[rp_{t,t+j}] = (e_5 - e_6)(B + B^2 + \dots + B^j)(I - BL)^{-1}A\epsilon_t$$

# Identification

$$E_t[rp_{t,t+j}] = (e_5 - e_6)(B + B^2 + \dots + B^j)(I - BL)^{-1}A\epsilon_t$$

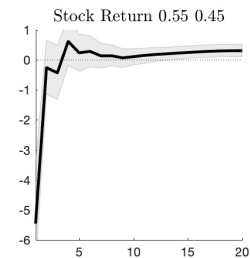
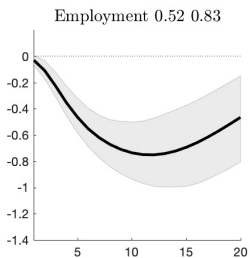
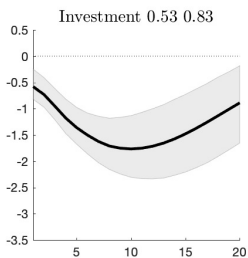
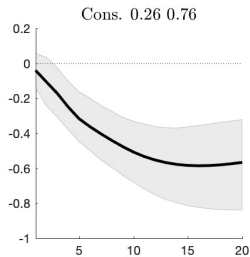
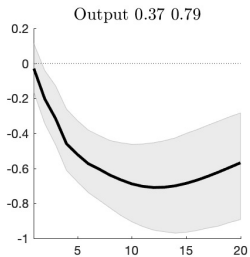
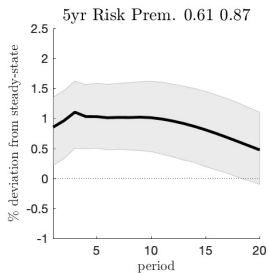
Pick  $A$  so that first shock explains most of  $E_t[rp_{t,t+j}]$ . (Uhlig, 2003)

Choices:

- Horizon  $j \rightarrow$  choose  $j = 20$ , for predictability at longer horizons
- Frequency band  $\rightarrow$  choose unconditional variance, robust to
  - business-cycle frequency (ACD, 2020)
  - one-period innovation

*Not imposing any prior on structural interpretation of the shock.*

# Results I - Response to a RP shock



## Results II - Driver of Covariances

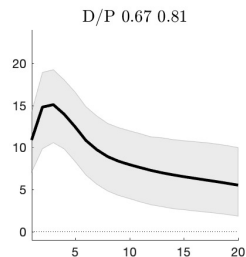
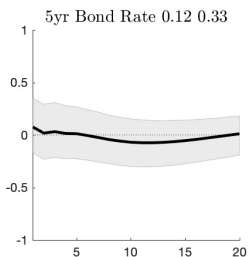
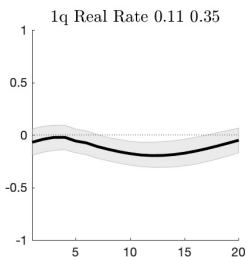
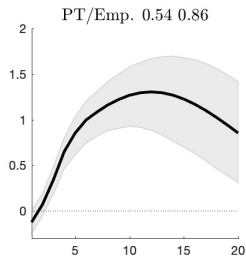
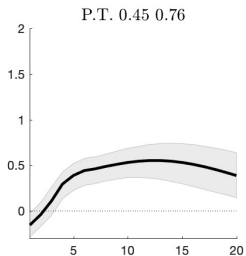
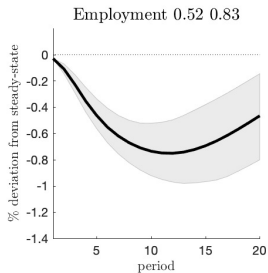
“Percent-explained” covariance:

$$1 - \text{cov}(Y_t|\epsilon_1)/\text{cov}(Y_t)$$

	<b>Output</b>	<b>Cons.</b>	<b>Investment</b>	<b>Employment</b>	<b>Stock Return</b>
Output	0.79				
Cons.	0.79	0.76			
Investment	0.87	0.92	0.83		
Employment	0.92	0.96	0.90	0.83	
Stock Return	1.31	1.02	1.40	0.98	0.45

**Fraction of Covariance Explained**

# Result III - Response to a RP shock

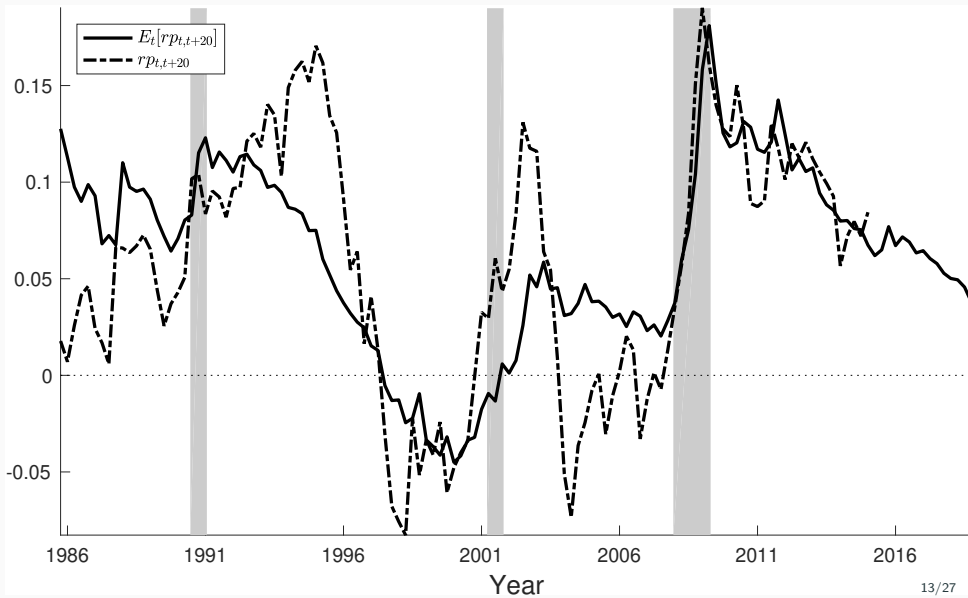


## Comparison to “Main business cycle shock”

ACD (2020) identify shock that explains BC variance of e.g. *GDP*

- Shock time series strongly correlated  $\rightarrow \sim 70\%$
- Same qualitative patterns
- Accounts for less of stock return covariances

# Result IV - Time-series of RP



# Theory

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Aggregate “RBC” model with

1. Epstein-Zin preferences
2. Capital adjustment costs
3. Variable capacity utilization
4. Labor market search
  - Two types of labor relationships: temporary and long-term

# Household

$$V_t \equiv \max_{C_t, X_{t+1}, B_{t+1}} \left[ (1 - \beta) C_t^{1-1/\psi} + \beta (\mathbb{E}_t V_{t+1}^{1-\gamma_t})^{\frac{1-1/\psi}{1-\gamma_t}} \right]^{\frac{1}{1-1/\psi}}$$

subject to

$$C_t + P_t^E X_{t+1} + \frac{1}{R_t^R} B_{t+1} + G_t \leq W_{1,t} N_{1,t} + W_{2,t} N_{2,t} + (D_t^E + P_t^E) X_t + B_t$$

Notes:

- Hold risk-free bonds ( $B_t$ ) and equity ( $X_t$ ).
- Labor supply exogenous: searchers given by

$$S_{1,t} = 1 - (1 - \rho_1) N_{1,t-1} - (1 - \rho_2) N_{2,t-1}$$

$$S_{2,t} = 1 - N_{1,t} - (1 - \rho_2) N_{2,t-1}$$

- Successful searchers become productive within-period.

$$V_t^E(i) = \max \mathbb{E}_t \sum_{s=0}^{\infty} M_{t+s} D_{t+s}$$

subject to

$$D_t = Y_t - W_{1,t} N_{1,t} - W_{2,t} N_{2,t} - I_t - \gamma_{1,t} v_{1,t} - \gamma_{2,t} v_{2,t}$$

$$Y_t = [K_t u_t]^\alpha [Z_t N_t]^{1-\alpha}$$

$$K_{t+1} = \left( 1 - \delta(u_t) - \frac{\phi_K}{2} \left( \frac{I_t(i)}{K_t} - \delta \right)^2 \right) K_t + I_t$$

$$N_t = N_{1,t}^{1-\Omega} N_{2,t}^\Omega$$

$$N_{1,t} = (1 - \rho_1) N_{1,t-1} + Q_{1,t}^m v_{1,t}$$

$$N_{2,t} = (1 - \rho_2) N_{2,t-1} + Q_{2,t}^m v_{2,t}$$

- Matching probs,  $P_t^m$  and  $Q_t^m$ , determined by CD matching function
- N1: (nearly) fixed real wage.
- N2: Nash-bargained wage.
- Vacancy posting conditions defines value of a worker

$$\mathbb{J}_{i,t} = MPL_{i,t} - W_{i,t} + \mathbb{E}_t \{ M_{t+1} (1 - \rho_i) \mathbb{J}_{i,t+1} \}$$

1. Technology:

$$\ln Z_t = \ln Z_{t-1} + \sigma_z \epsilon_t^z$$

2. Risk aversion:

$$\ln(\gamma_t/\gamma) = \rho_{1,\gamma} \ln(\gamma_{t-1}/\gamma) + \rho_{2,\gamma} \ln(\gamma_{t-2}/\gamma) + \sigma_\gamma \epsilon_t^\gamma$$

3. Cointegration of  $\{\gamma_{1,t}, \gamma_{2,t}, W_{1,t}\}$ : E.g.

$$W_{1,t+1} = W_{1,t}^\omega Z_t^{1-\omega}$$

## Barro and King (1984) problem

Worried about future?  $\Rightarrow$  desire to (i) save more (ii) consume less

(i) implies that investment rises

(ii) if labor supply endogenous, hours increase

$\hookrightarrow$  I,C,N cannot move together!

## How our model works

Risk aversion rises  $\Rightarrow$  (i) save more in safer assets (ii) consume less

(i) premium for  $N_1$  rises most  $\Rightarrow$  “savings” shifts away from  $N_1$

(ii) if  $N_1$  and cap. util. fall enough, then  $Y \downarrow$  causes both  $C \downarrow, I \downarrow$

$\hookrightarrow$  I,C,N *can* move together!

# Quantifying the Mechanism

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# Impulse Response Matching

- Solve model using 3rd-order perturbation
- Target first six impulse responses in  $Y_t$
- Additional steady-state targets

<b>Description</b>	<b>Value</b>
Equity risk premium	0.064
Share of part-time	0.180
Agg. separation rate	0.100
PT sep./FT sep.	8.000
PT earn./FT earn.	0.500
Vacancy Rate	0.035
LR unemployment	0.060
Std. HP log(Emp/Pop)	0.011
Std. log(vacan.)	0.264

- Look at implication for non-targeted variables

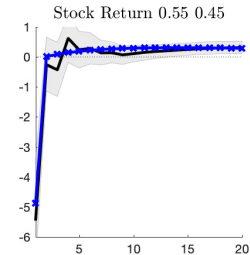
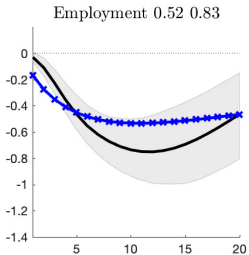
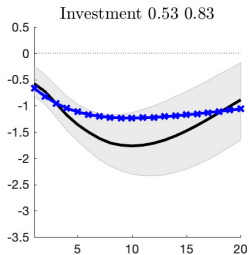
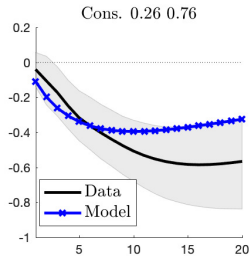
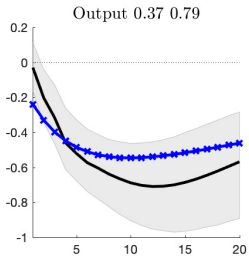
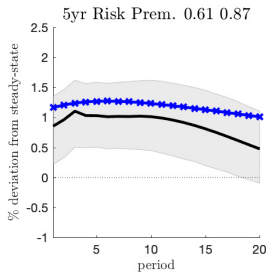
# Calibrated parameters

Name	Description	Value
$\beta$	Discount rate	0.994
$\psi$	Intertemporal elasticity of substitution	1.500
$\alpha$	Capital share	0.300
$\delta$	Cap depreciation rate	0.025
$\delta_2$	Cap. util. cost $\times$ 100	0.030
$\bar{g}$	Steady-state G/Y	0.200
$d$	Corporate bond duration	0.975
<b>Labor Markets</b>		
$\rho_1$	Separation Rate - FT	0.044
$\rho_2$	Separation Rate - PT	0.354
$\eta_1$	HH's bargaining power - FT	0.500
$\eta_2$	HH's bargaining power - PT	0.200
<b>Exogenous Processes</b>		
$\sigma_z$	Std. dev. of tech shock	0.006
$\rho_{1,\gamma}$	AR(1) risk av. shock	1.802
$\rho_{2,\gamma}$	AR(2) risk av. shock	-0.806

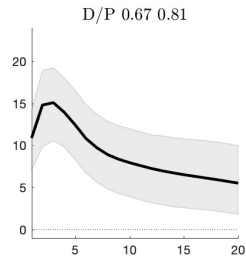
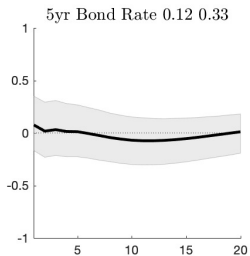
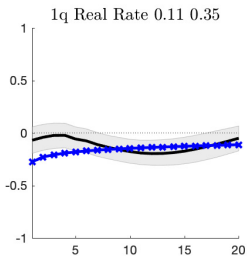
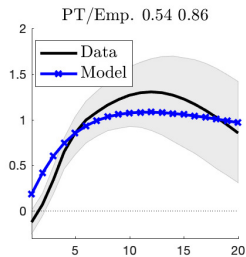
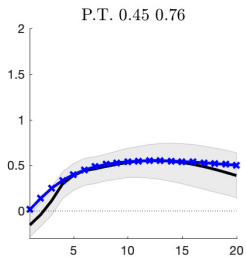
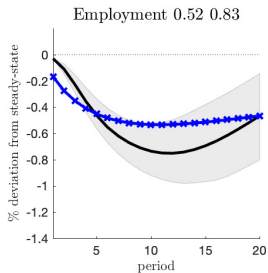
# Estimated Parameters

Name	Description	Point Est.	Std Err.
$\gamma_{ss}$	Steady-state risk aversion	102.072	1.403
$\phi_k$	Capital Adj. Cost	11.444	0.294
$\nu$	Leverage Ratio	0.739	0.005
<b>Labor Markets</b>			
$\gamma_1$	Vacancy posting cost - FT	3.000	0.101
$\gamma_2$	Vacancy posting cost - PT	1.050	0.027
$b_1$	Value if no perm posit.	1.153	0.003
$b_2$	Value if unemployed	0.526	0.005
$\Omega$	Labor contrib. of PT	0.124	0.001
$\epsilon^1$	Matching elasticity - FT	0.161	0.002
$\epsilon^2$	Matching elasticity - PT	0.789	0.007
$\chi^1$	Matching technology - FT	0.440	0.003
$\chi^2$	Matching technology - PT	1.322	0.020
$\omega$	Gradual wage adj.	0.987	0.000
<b>Risk Aversion Process</b>			
$\sigma_\gamma$	Std. dev. of risk av. shock	0.050	0.001

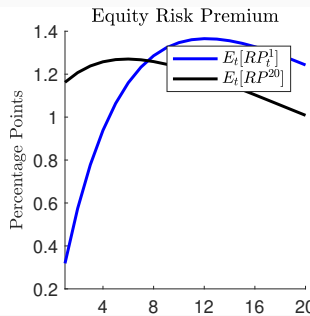
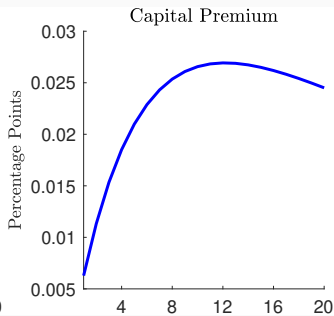
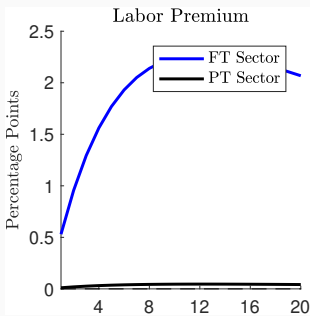
# Estimation Results I



# Estimation Results II



# Impulse Responses: Risk Premia



# Conclusions

1. Risk-premia changes strongly associated with macroeconomic flucs.
2. Theory where causality flows from premia  $\Rightarrow$  macro fluctuations
3. Captures *many* qualitative features of the cycle
4. Quantitatively promising