

# Option Liquidity and Gamma Imbalances

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## 1. Story

### Summary

We study the relationship between the market makers' inventory and liquidity for S&P 500 options. Option spreads are higher when the aggregate gamma inventory is negative, i.e., when market makers act as momentum traders to keep their portfolio delta neutral. Aggregate gamma inventory can explain up to 1/3 of the daily variation in spreads. We show that market makers have balanced gamma inventory whenever markets are illiquid, volatile, and financial intermediaries are constrained. Our results indicate that market makers actively adjust option expensiveness to balance their inventory in the desired direction. Standard option valuation models and market microstructure theories contradict our findings.

### Option market making and liquidity provision

- Market makers (MM) provide liquidity on option markets → take opposite side of a trade when counterparts' positions are not exactly met → zero net supply
- MM build up large inventories → might deviate from optimal MM inventory → hedge demand for (possible risky) inventory positions
- Hedging is costly and risky due to market imperfections (Figlewski, 1989)
- Deviations from optimal inventory, associated risks, and hedging costs should be reflected in **MM compensation for liquidity provision** → option spread

### Three questions

- What is the relation between hedging needs and option liquidity?
- When do market makers require more compensation for providing liquidity?
- Which positions are associated with higher liquidity costs?

### What we do

- We compute the daily aggregated inventory
- We determine the magnitude of MM hedging activity by the aggregated gamma inventory ( $AGI$ )
- Gamma: Change in option's delta → good proxy for rebalancing activity of market makers inventory
- Gamma exposure approximates hedging costs of market makers (Gârleanu et al., 2009)
- We relate  $AGI$  to liquidity measures from intraday option trades

### In a nutshell

#### What do we find?

- Negative  $AGI$  is associated with wider spreads → higher compensation for providing liquidity
- Effect appears to be largest in magnitude and significance for OTM calls/puts
- MM manage their inventory in turbulent times → balanced gamma inventory (near zero) → especially when markets are volatile, illiquid, and intermediaries are especially constrained → rebalancing activity reduces to a minimum
- Balanced inventory → option expensiveness is high and liquidity risk premium is high

### Mechanical trading to stay delta neutral

#### Hedging and trading.

- MM manage their book using delta hedging → non-informational channel why stock prices move
- Negative  $AGI$ : MM is **momentum** trader
- Positive  $AGI$ : MM is **reversal** trader

#### What could rationalize our findings? E.g. MM is short gamma (negative $AGI$ )

- $S \downarrow$  → MM sells to stay delta neutral → trades in the same direction market → hard to find a counterpart → illiquid markets →  $AGI$  survives existing illiquidity measures → MM appear to care about further risk sources

## 2. Data and Methodology

### Gamma weighted inventory

**Construction.** We follow Ni et al. (2021)

$$OI_{j,t}^{buy,y} = \underbrace{OI_{j,t-1}^{buy,y}}_{\text{Existing}} + \underbrace{Volume_{j,t}^{Open\ buy,y} - Volume_{j,t}^{Close\ sell,y}}_{\text{Order imbalance}}$$

$$OI_{j,t}^{sell,y} = OI_{j,t-1}^{sell,y} + Volume_{j,t}^{Open\ sell,y} - Volume_{j,t}^{Close\ buy,y}$$

$$netOI_{j,t} = -1 \cdot [OI_{j,t}^{buy,cust} - OI_{j,t}^{sell,cust} + OI_{j,t}^{buy,firm} - OI_{j,t}^{sell,firm}]$$

**Gamma weighting.**

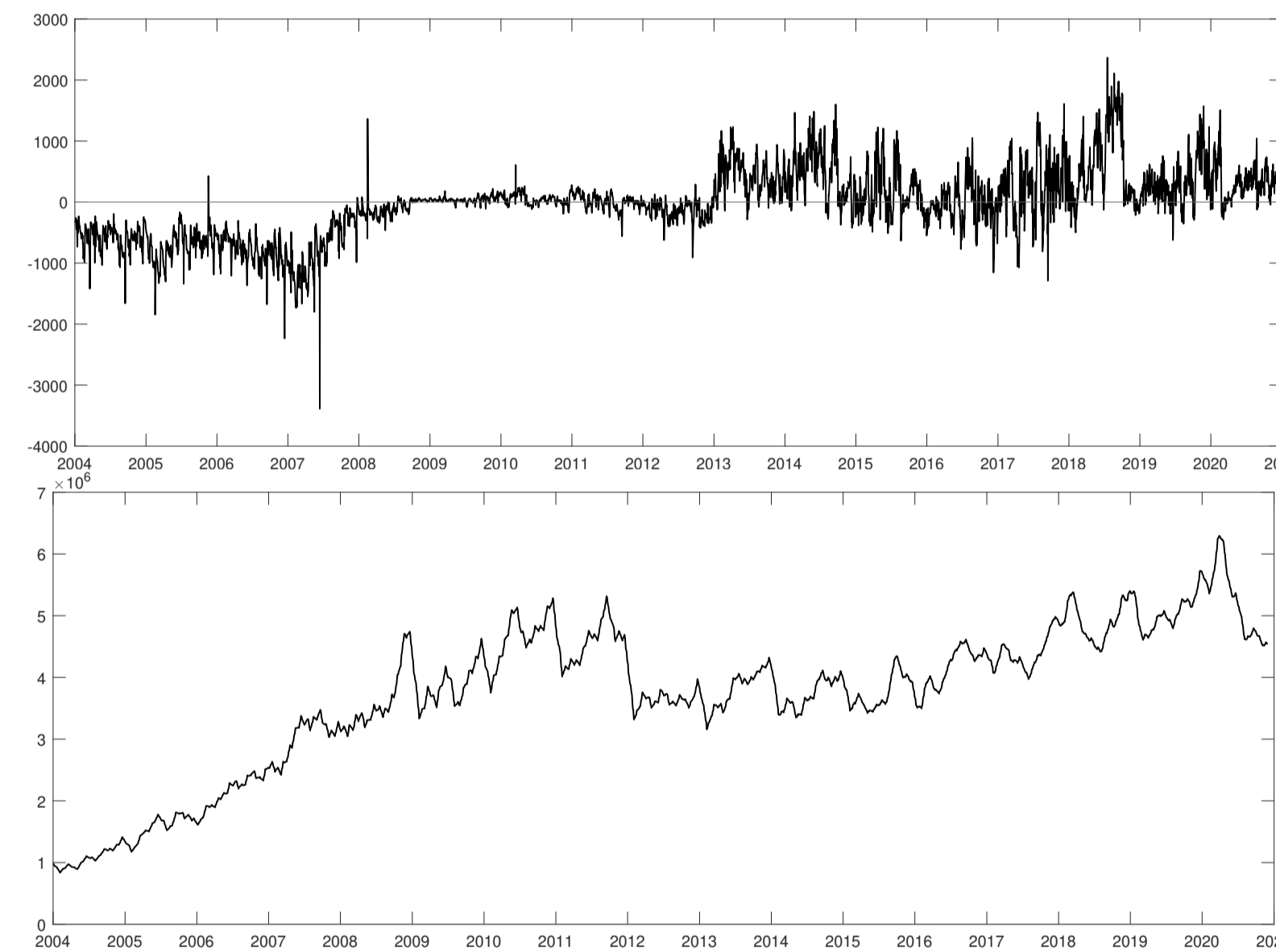
$$net\Gamma_t = S_t^2 \cdot \sum_{j=1}^N (netOI_{j,t} \cdot \Gamma_j(S_t, K, \tau, IV, r, d))$$

where  $\Gamma_j$  is the Black and Scholes (1973) gamma for option  $j$ .

$$AGI_t = \frac{net\Gamma_t}{\frac{1}{M} \sum_{i=0}^{M-1} Total\ Contracts_{M-i}}$$

where  $AGI_t$  is the aggregated dollar gamma exposure per unit of contract.

### AGI and absolute number of contracts in inventory.



### Implied volatility effective spreads

**Effective spreads.** We follow Christoffersen et al. (2018) and Chaudhury (2015)

$$IVES_{k,j} = \frac{2 \cdot |O_{k,j}^P - O_{k,j}^M|}{O_{k,j}^M}$$

$$IVES_j = \frac{\sum_k Vol_k \cdot IVES_{k,j}}{\sum_k Vol_k}$$

- Compute the median  $ES_j^B$  within each moneyness bucket to obtain  $ES_t^B$

### Data

#### Focus on S&P 500 Options.

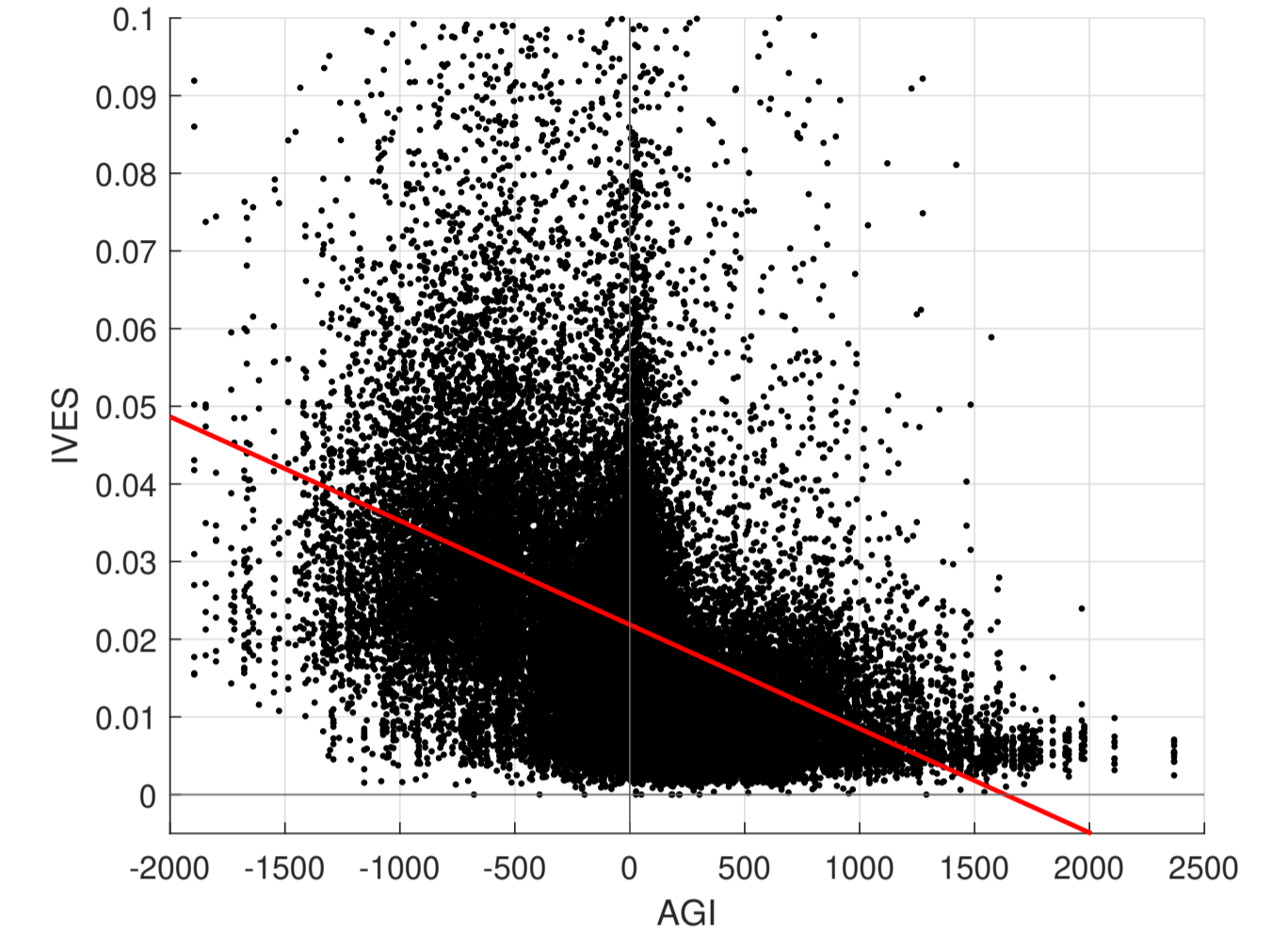
- C1 CBOE Open-Close database → signed trades
- OptionMetrics → Option mid-quotes,  $\Delta$ , IVs → calculate  $\Gamma$
- CBOE intraday option trades → liquidity measures

#### Sample period.

- January 01, 2004 - December 31, 2020
- Preceding years as a "burn-in period"

## 3. Empirical Results

### Negative gamma inventory → wider spreads



- Highest  $R^2$  for ATM options → highest  $\Gamma$  risk
- A one standard deviation decrease in  $AGI_t$  increases  $IVES_t$  by 0.73% on average
- Our result is not a phenomenon of illiquidity spillovers from underlying

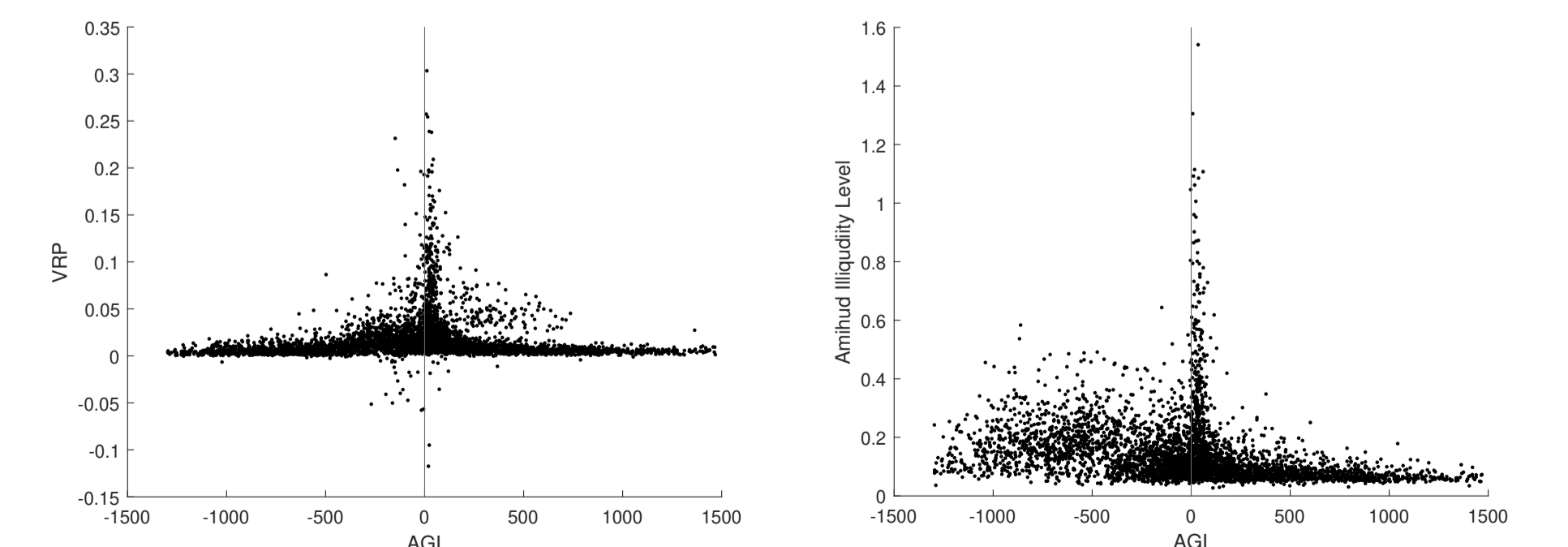
### More uncertain states → balanced gamma inventory

$$\mathbb{1}_t^{20} = \alpha + \beta_1 MI_t + \beta_2 RV_t + \beta_3 HKM_t + e_t$$

	(1)	(2)	(3)	(4)	(5)	(6)	(7)
$\alpha$	-1.2670 (-31.73)	-1.5440 (-27.02)	1.7640 (16.28)	-1.6200 (-29.89)	1.0800 (10.40)	1.0970 (8.05)	0.8820 (7.37)
MI	3.0050 (15.38)			1.0330 (4.08)	2.2020 (7.93)		1.4800 (4.57)
RV		5.4950 (13.52)		4.8880 (10.69)		2.2030 (7.14)	1.4200 (4.00)
HKM			-4.5970 (-21.42)		-3.8650 (-22.74)	-3.9140 (-18.15)	-3.6800 (-20.14)
adj. $R^2$	0.0608	0.1250	0.2690	0.1290	0.2840	0.2830	0.2880

Higher probability to end up in 20<sup>th</sup> quantile of  $abs(AGI_t)$  if

- ... markets are more illiquid (Amihud, 2002),  $RV$  is higher, intermediaries are more constrained (they have lower financial health) (He et al., 2017)



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