

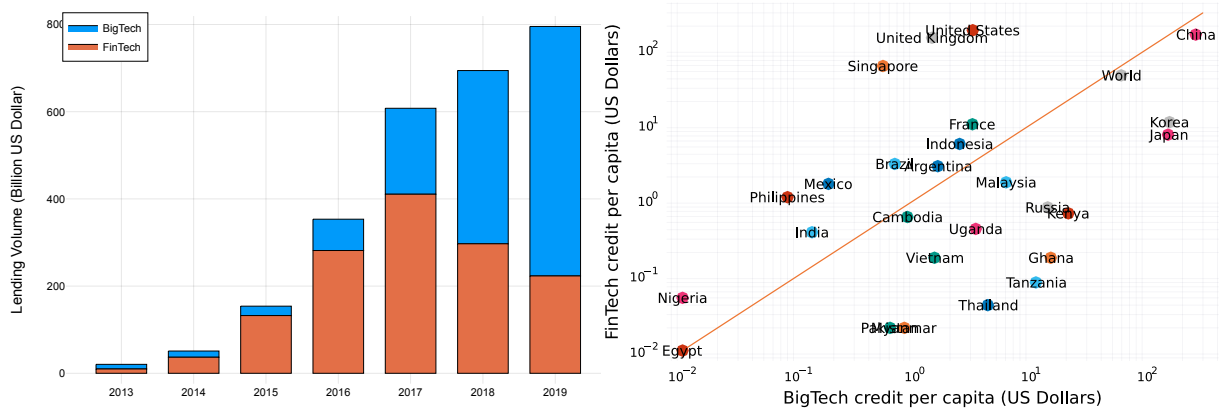
THE MACROECONOMICS OF BIGTECH

Dan Su

CKGSB

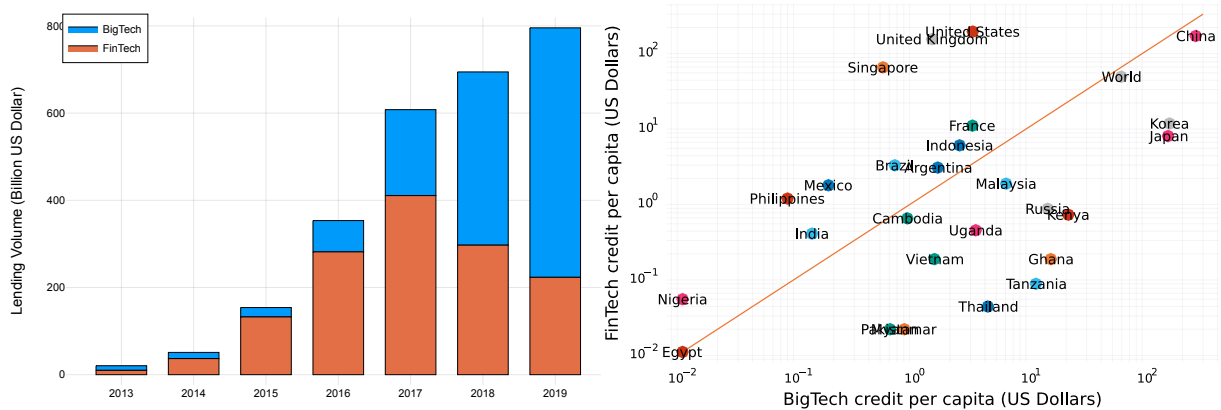
2024 ASSA Annual Meeting
Investment and Technological Change Session

NEW FINANCIAL INTERMEDIARIES



- ▶ **FinTech:** digital lending facilitated by online platforms (e.g., P2P, ...)
- ▶ **BigTech/TechFin:** large tech companies lend in the credit markets (e.g., Ant Group, WeBank, ...)

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- ▶ **BigTech/TechFin**: large tech companies lend in the credit markets (e.g., Ant Group, WeBank, ...)
- ▶ **a growing empirical literature, but theoretical implications?**

RESEARCH QUESTION: ROLE OF BIGTECH IN MACROECONOMY

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why BigTech instead of FinTech: BigTech is more bank-like (Stulz, 2019; King, 2019)

BANK V.S. BIGTECH: MACRO PERSPECTIVE

- ▶ **Banking sector:** collateral-based borrowing constraint
- ▶ **BigTech sector:** (expected-)earnings-based borrowing constraint

BANK V.S. BIGTECH: MACRO PERSPECTIVE

- ▶ **Banking sector:** collateral-based borrowing constraint
- ▶ **BigTech sector:** (expected-)earnings-based borrowing constraint
- ▶ **Microfoundation** of incomplete-collateralization contract:
 1. *technology story*: tech/data advantages → reduced cost of state verification
 2. *intangible capital story*: intangible capital → low liquidation value

BANK V.S. BIGTECH: MACRO PERSPECTIVE

- ▶ **Banking sector:** collateral-based borrowing constraint
- ▶ **BigTech sector:** (expected-)earnings-based borrowing constraint
- ▶ **Empirical evidence:**
 1. Gambacorta et al. (2023): ✗ local business conditions and house prices; ✓ firm-specific characteristics
 2. Beck et al. (2022): liquidation cost decreasing in asset tangibility

BANK V.S. BIGTECH: MACRO PERSPECTIVE

- ▶ **Banking sector:** collateral-based borrowing constraint
- ▶ **BigTech sector:** (expected-)earnings-based borrowing constraint
- ▶ **Other possible difference:** fast data processing ability (Fuster et al., 2019); new credit-sorting models (Gambacorta et al., 2019); different maturities (Liu, Lu and Xiong, 2022)...

MACROFIN \Rightarrow MACROBIGTECH

FRAMEWORK

► **A macro model with three key elements:**

1. heterogeneous agent model with incomplete markets
2. two types of borrowing constraints
3. defaultable debt

MACROFIN \Rightarrow MACROBIGTECH

MECHANISM

- ▶ **Key feature:** **convex** relationship between (expected) productivity and wealth growth rate
 - **advantage:** rely less on collateral, which is unrelated to *individual* productivity
 - **disadvantage:** depend on the accuracy of predicting *individual* earnings
- ▶ **expected-earnings**-based borrowing constraint

MACROFIN \Rightarrow MACROBIGTECH

IMPLICATION

► **Main conclusions** on the rise of BigTech

1. **efficiency-instability trade-off**: smaller aggregate productivity losses but more financial instability in the steady state
2. **different financial accelerator**: amplification and propagation of second-moment uncertainty shocks
3. **extensions**: algorithm bias; optimal BigTech development; pricing effect; non-M.I.T. shocks

RELATED LITERATURE

- ▶ **FinTech/BigTech:** Gambacorta et al. (2023); Tang (2019); Hau et al. (2018); Cornelli et al. (2023); Huang (2022); Manea, Fiore and Gambarcorta (2023); Liu, Lu and Xiong (2022)...
- ▶ **Financial frictions and macroeconomy:** Kiyotaki and Moore (1997); Bernanke and Gertler (1989); Brunnermeier and Sannikov (2014); Di Tella (2017); He and Krishnamurthy (2013); Fernandez-Villaverde, Hurtado and Nuno (2019); ...
- ▶ **Distributional macro:** Moll (2014); Fernandez-Villaverde, Hurtado and Nuno (2019); Achdou et al. (2022); ...
- ▶ **Earnings-based borrowing constraint:** Lian and Ma (2021); Greenwald (2019); Drechsel (2023); Drechsel and Kim (2022); ...

MODEL

- ▶ **Infinite-horizon, continuous-time economy**
- ▶ **Two types of entrepreneurs** + Homogeneous hand-to-mouth workers ($S = 1$ in baseline)
 - i 1 continuum of entrepreneurs borrowing from the banking sector **B**
 - ii S continuum of entrepreneurs borrowing from the BigTech sector **F**
- ▶ **Preference:** $\mathbb{E}_0 \int_0^\infty e^{-\rho t} \log c(t) dt$
- ▶ **Production function:** $y = zk^\alpha l^{1-\alpha}$
- ▶ **Stochastic productivity process:** $dz = \frac{1}{\theta} (\bar{\mu} - z) dt + \sigma \sqrt{\frac{1}{\theta}} dW$

TIMING AND EXPECTATION

- ▶ **Expected productivity** ($\gamma = 0$ in baseline):

$$\tilde{\mathbb{E}}[z] = \tilde{\mathbb{E}}[\tilde{z} + dz] = \underbrace{\frac{1}{\theta} [\bar{\mu} + (\theta - 1) \tilde{z}]}_{\text{rational expectation}} + \underbrace{\gamma (\tilde{z} - \bar{\mu})}_{\text{algorithm bias}}$$

- γ : degree of bias
- extrapolative expectation literature (e.g., Bordalo, Gennaioli and Shleifer, 2018)

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- ▶ **“Costless” default** (in the baseline): focus on exogenous borrowing constraints
- ▶ **State of the economy**:

$$\{\omega_F(t, a, z, \tilde{z}), \omega_B(t, a, z, \tilde{z})\}$$

TWO TYPES OF BORROWING CONSTRAINTS

- ▶ **Banking sector:** collateral-based borrowing constraint

$$k - a \leq \lambda_B k \Rightarrow k \leq \frac{1}{1 - \lambda_B} a$$

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$$k - a \leq \lambda_B k \Rightarrow k \leq \frac{1}{1 - \lambda_B} a$$

- ▶ **BigTech sector:** earnings-based borrowing constraint

$$k - a \leq \lambda_F \tilde{\mathbb{E}}[\pi] \Rightarrow k \leq \frac{1}{1 + \lambda_F \left[\frac{r+\delta}{\alpha} - \zeta \tilde{\mathbb{E}}[z] \right]} a$$

where $\zeta \equiv \left(\frac{(1-\alpha)(r+\delta)}{\alpha w} \right)^{1-\alpha}$

SIMILARITY AND DIFFERENCE I

- ▶ **Similarity**: corporate debt capacity depends on **(expected) net worth**

$$\text{debt capacity} = \phi \times \text{net worth}$$

- ? “With cash flow-based lending and EBCs, we find that asset price feedback through firms’ balance sheets could diminish significantly.”(Lian and Ma, 2021)
- ? “This evidence implies that a greater use of big tech credit could reduce the importance of collateral in credit markets and potentially weaken the financial accelerator mechanism.” (Gambacorta et al., 2023)

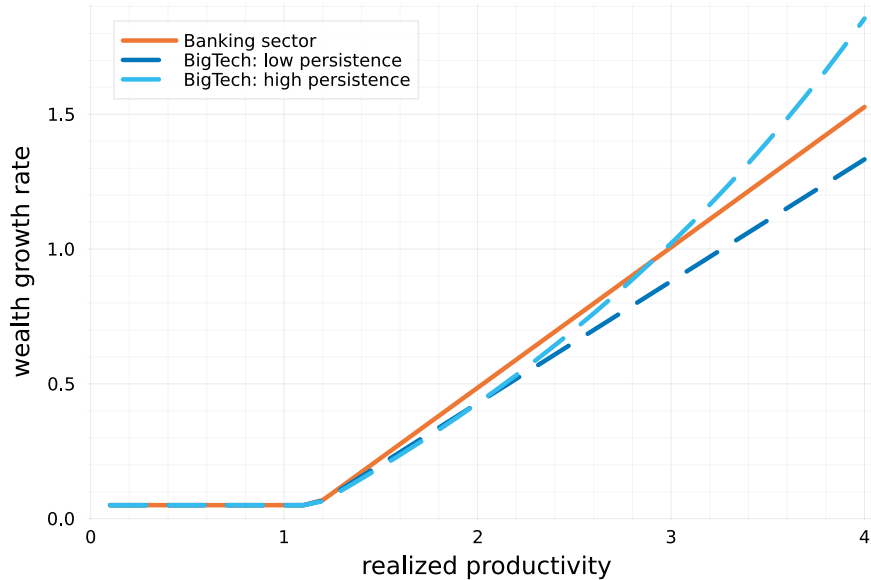
SIMILARITY AND DIFFERENCE II

- ▶ **Difference:** (expected) productive firms get to use more leverage in BigTech

$$k \leq \frac{1}{1 - \lambda_B} a$$
$$k \leq \frac{1}{1 + \lambda_F \left[\frac{r + \delta}{\alpha} - \zeta \tilde{\mathbb{E}}[z] \right]} a$$

- ▶ asymmetric **wealth** growth rate for firms with different (expected) productivity

KEY MECHANISM: CONVEXITY + UNCERTAINTY



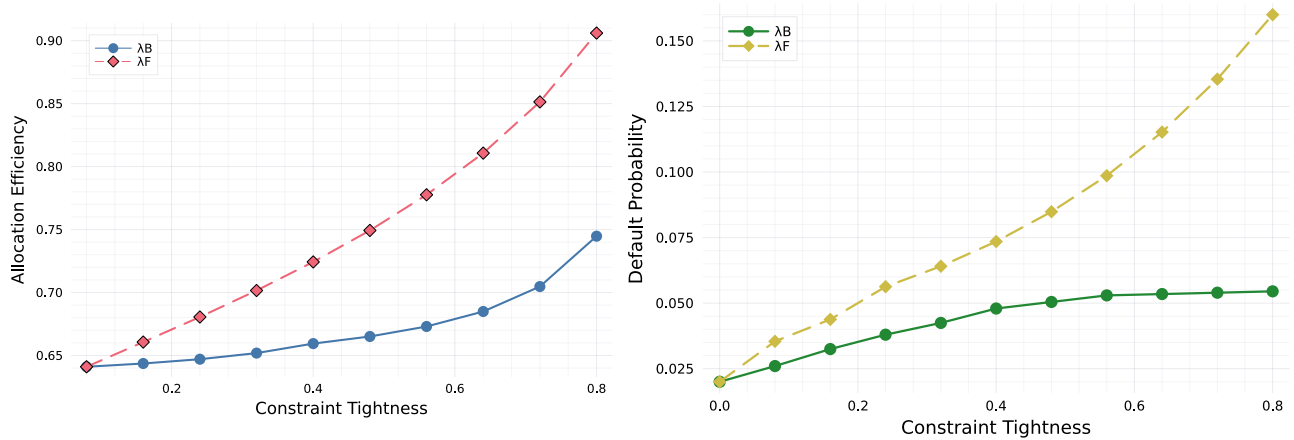
▸ Policy Function ▸ Wealth Dynamics ▸ Distribution Dynamics

PARAMETRIZATION

Parameter	Description	Value	Source/Reference
ρ	rate of time preference	0.05	Moll (2014)
α	capital share	0.33	
\mathcal{L}	labor market size	1.0	
δ	capital depreciation rate	0.06	BEA-FAT
γ	algorithm bias	0.4	match the default probability
\mathcal{S}	size of BigTech	1.0	
$\bar{\mu}$	log idiosyncratic productivity mean	0.0	
θ	autocorrelation $e^{-\theta}$	0.16 (corr = 0.85)	Asker, Collard-Wexler and Loecker (2014)
σ	log idiosyncratic productivity s.d.	0.56	

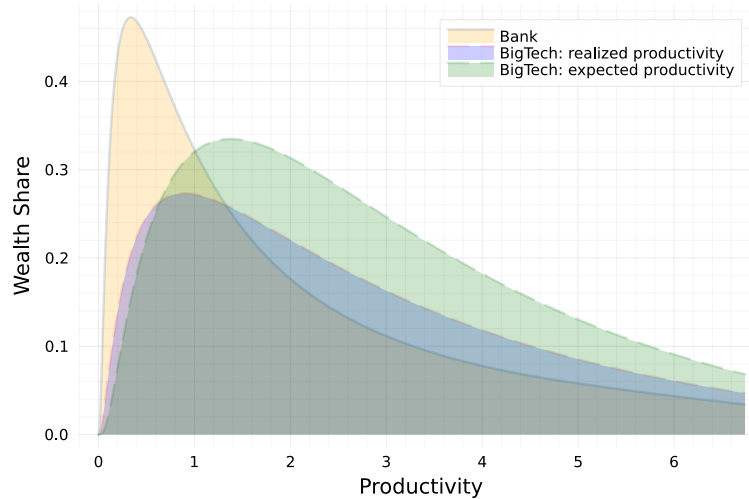
1. steady state analysis
2. business cycles with M.I.T shocks
3. extensions

EFFICIENCY-INSTABILITY TRADE-OFF



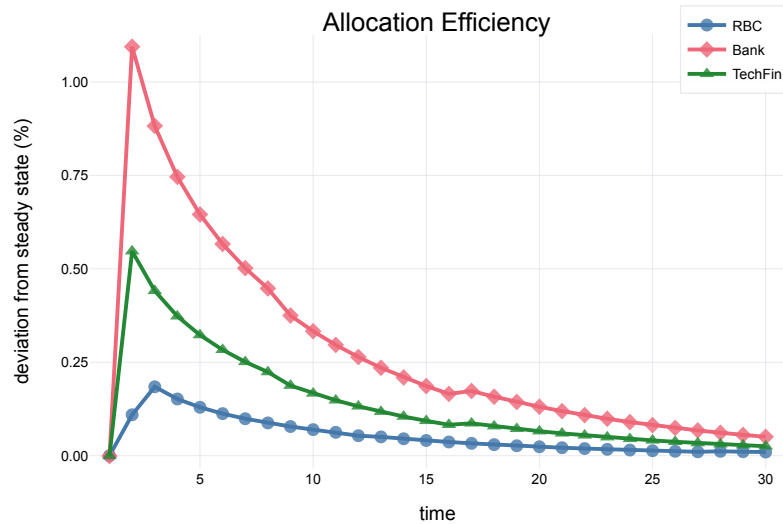
► **BigTech cannot fully replace the role of traditional banks**

EFFICIENCY-INSTABILITY TRADE-OFF

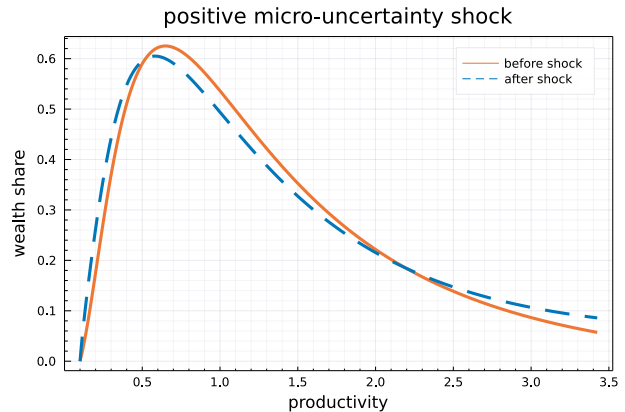
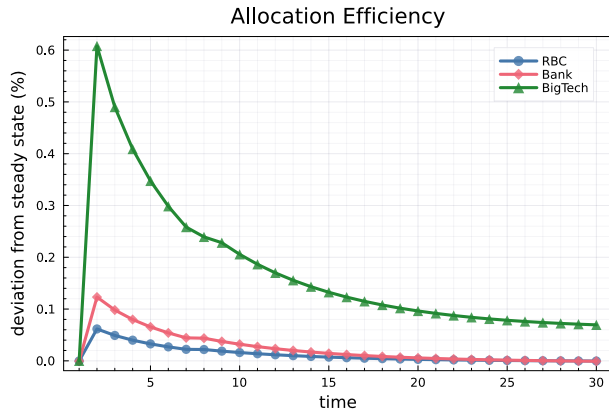


► **BigTech cannot fully replace the role of traditional banks**

BUSINESS CYCLES: FIRST-MOMENT SHOCKS

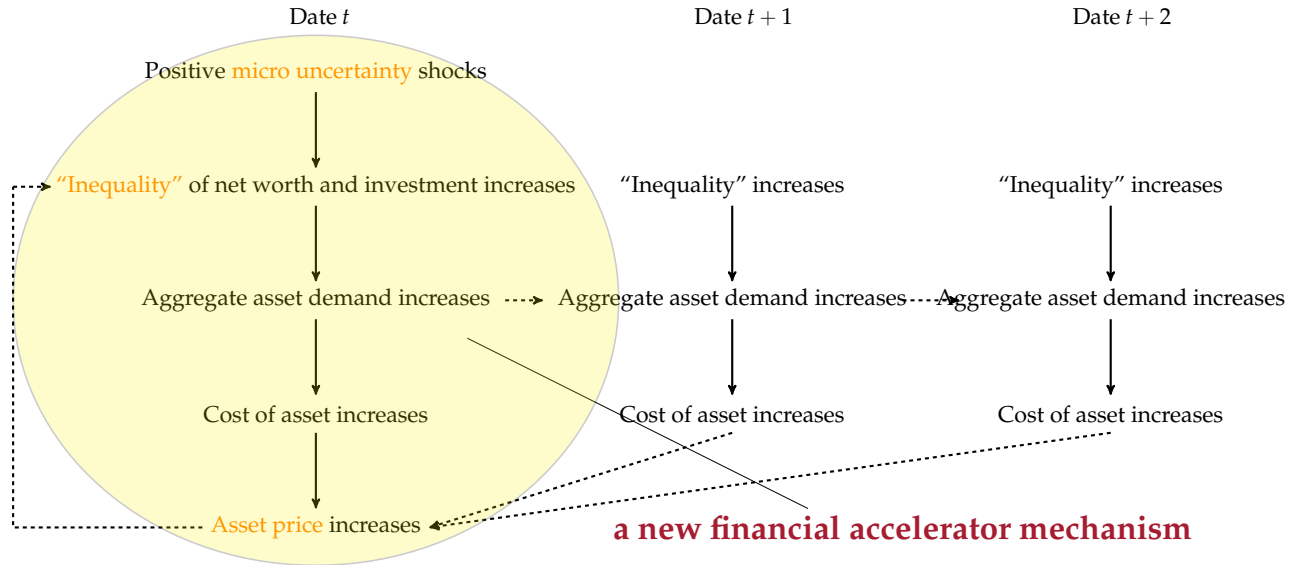


BUSINESS CYCLES: SECOND-MOMENT SHOCKS



► **BigTech lending is sensitive to uncertainty shocks**

AMPLIFICATION AND PERSISTENCE



AMPLIFICATION AND PERSISTENCE

CREDIT CYCLES

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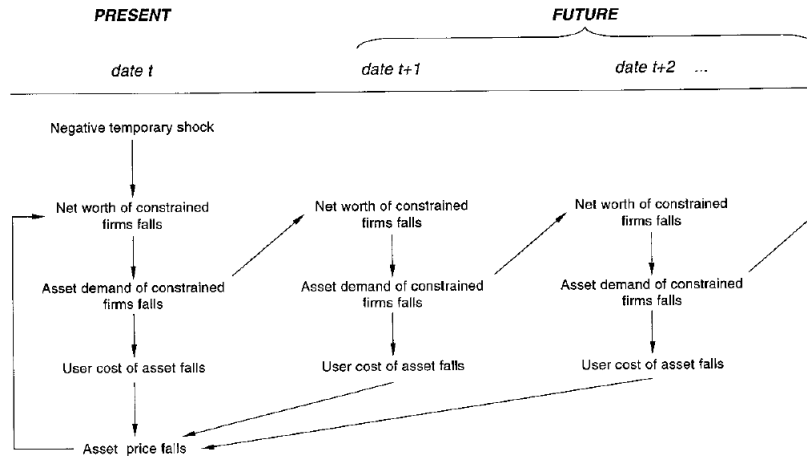


FIG. 1

Figure. Kiyotaki and Moore (1997)

ON FINANCIAL ACCELERATOR MECHANISM

- ▶ Different from the classical one (e.g., Kiyotaki and Moore, 1997; Bernanke and Gertler, 1989) in three aspects
 - **primitive shock**: micro uncertainty instead of aggregate productivity
 - **financial friction**: earnings-based borrowing constraint instead of collateral-based borrowing constraint
 - **feedback loops**: between net worth inequality, instead of net worth level, and asset prices

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- ▶ **Macroeconomics of BigTech**: a different financial accelerator mechanism

EXTENSIONS

▶ **Algorithm Bias:** $\gamma \neq 0$

▶ **Optimal BigTech Development:** $\mathcal{S} \neq 1$

$$\mathcal{U}(\mathcal{S}) = \mathcal{Z}'(\mathcal{S}) - \eta \mathcal{P}(\mathcal{S})$$

▶ **Risky Bond:**

$$qb' = \frac{\mathbb{E} \{ \mathbf{1}_{V' \geq 0} b' + \mathbf{1}_{V' < 0} (\chi_k k + \chi_\pi \pi) \}}{1 + r}$$

▶ **Non-M.I.T. Shocks:**

$$dz = \frac{1}{\theta} (\bar{\mu} - z) dt + \sigma \sqrt{\frac{1}{\theta}} d\mathcal{W}$$

$$\bar{\mu} \in \{ \bar{\mu}_L, \bar{\mu}_H \}, \text{ where } Pr(\bar{\mu}' = \bar{\mu}_l | \bar{\mu} = \bar{\mu}_k) = \zeta_{kl}$$

$$\sigma \in \{ \sigma_L, \sigma_H \}, \text{ where } Pr(\sigma' = \sigma_l | \sigma = \sigma_k) = \chi_{kl}$$

▶ Algorithm Bias ▶ Optimality ▶ Risky Debt ▶ Non-MIT Shock

CONCLUSION

- ▶ **Research question:** introduce BigTech into the existing macro-finance literature
- ▶ **Key take-aways:** BigTech v.s. Bank as two types of borrowing constraints
 - efficiency-instability trade-off
 - a different financial accelerator
- ▶ **Extensions:**
 - algorithm bias
 - optimal BigTech development

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▶ Banking sector

$$k^B(a, z, \tilde{z}) = \begin{cases} \frac{a}{1-\lambda_B} & \tilde{\mathbb{E}}[z] \geq \tilde{z} \\ 0 & \tilde{\mathbb{E}}[z] < \tilde{z} \end{cases}$$

▶ BigTech sector

$$k^F(a, z, \tilde{z}) = \begin{cases} \frac{1}{1+\lambda_F(\frac{r+\delta}{\alpha}-\zeta\tilde{\mathbb{E}}[z])} a & \tilde{\mathbb{E}}[z] \geq \tilde{z} \\ 0 & \tilde{\mathbb{E}}[z] < \tilde{z} \end{cases}$$

where $\tilde{z} = \left(\frac{r+\delta}{\alpha}\right)^\alpha \left(\frac{w}{1-\alpha}\right)^{1-\alpha}$

$$da_B = \left\{ 1_{\tilde{\mathbb{E}}[z] \geq \tilde{z}} \times \left[\frac{\zeta z - \frac{r+\delta}{\alpha}}{1 - \lambda_B} + r - \rho \right] + 1_{\tilde{\mathbb{E}}[z] < \tilde{z}} \times (r - \rho) \right\} a_B dt$$

$$da_F = \left\{ 1_{\tilde{\mathbb{E}}[z] \geq \tilde{z}} \times \left[\frac{\zeta z - \frac{r+\delta}{\alpha}}{1 + \lambda_F \left[\frac{r+\delta}{\alpha} - \zeta \left(\frac{1}{\theta} - \gamma \right) \bar{\mu} - \frac{\zeta(\theta-1+\theta\gamma)}{\theta} \tilde{z} \right]} + r - \rho \right] + 1_{\tilde{\mathbb{E}}[z] < \tilde{z}} \times (r - \rho) \right\} a_F dt$$

► **Low productivity firms**

- constant net worth growth rate
- low-productivity entrepreneurs do not operate and lend all their net worth to good firms

► **High productivity firms**

- net worth growth rate is higher than its actual productivity: leverage effect
- BigTech: most-productive firm's net worth grows even faster

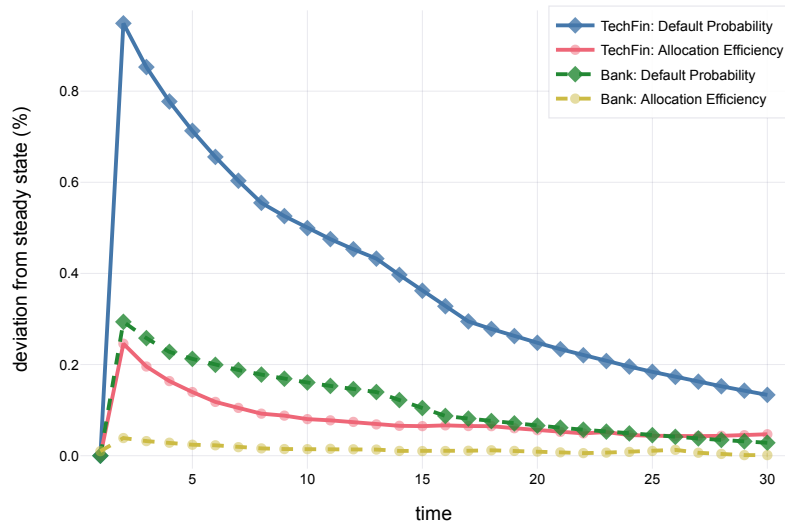
$$\begin{aligned} \frac{\partial \omega^j(t, a, z, \tilde{z})}{\partial t} &= - \frac{\partial [\Gamma^j(t, z, \tilde{z}) a \omega^j(t, a, z, \tilde{z})]}{\partial a} - \frac{\partial \left[\frac{1}{\theta} (\bar{\mu} - z) \omega^j(t, a, z, \tilde{z}) \right]}{\partial z} - \frac{\partial \left[\frac{1}{\theta} (\bar{\mu} - \tilde{z}) \omega^j(t, a, z, \tilde{z}) \right]}{\partial \tilde{z}} \\ &+ \frac{\sigma^2}{2\theta} \frac{\partial^2 [\omega^j(t, a, z, \tilde{z})]}{\partial \tilde{z}^2} + \frac{\sigma^2}{2\theta} \frac{\partial^2 [\omega^j(t, a, z, \tilde{z})]}{\partial z^2} \text{ where } j \in \{\mathcal{B}, \mathcal{F}\} \end{aligned}$$

- ✗ **wealth share approach:** Caselli and Gennaioli (2013); Moll (2014); ...
- ✗ **(adaptive) sparse grid approach:** Brumm and Scheidegger (2017); ...
- ✓ **deep learning approach:** Han and E (2016); Raissi, Perdikaris and Karniadakis (2019); Fernandez-Villaverde et al. (2020); Chen, Didisheim and Scheidegger (2021); ...

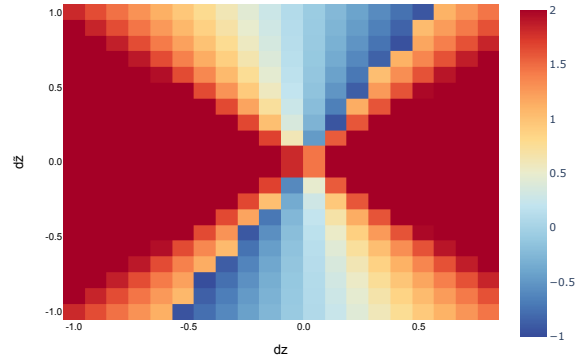
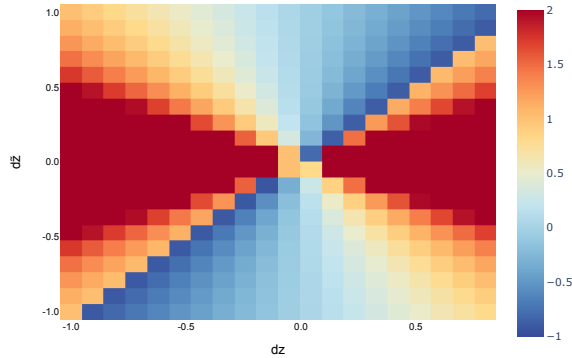
EXTENSION: ALGORITHM BIAS

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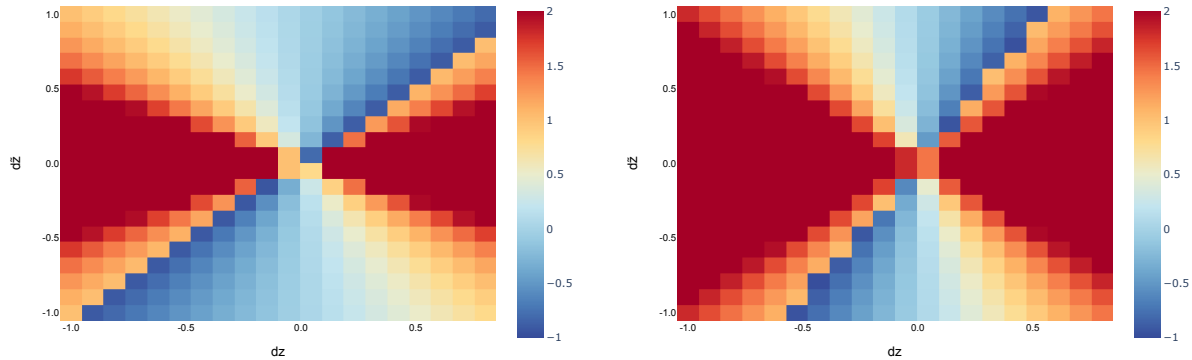
► fragile booms



▶ overlending issues



▶ overlending issues



▶ Financial markets are *less* efficient in booms than in recessions:

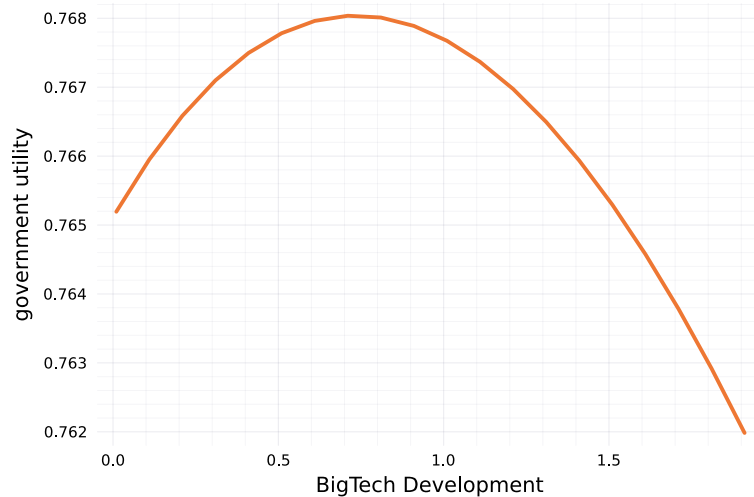
- **Minsky's financial instability hypothesis:** economic prosperity encourages borrowers and lender to be reckless
- **Greenspan/Shiller's irrational exuberance:** overheated economy generates bubbles

EXTENSION: OPTIMAL BIGTECH DEVELOPMENT

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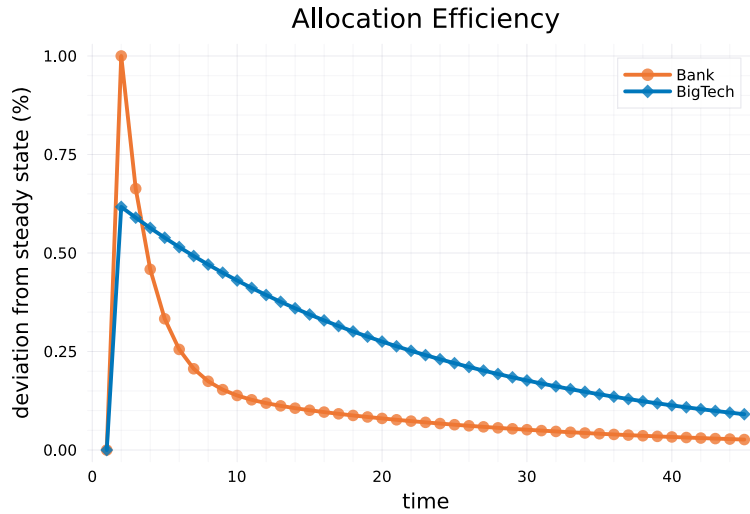
- ▶ assume that the government cares about both efficiency and financial stability

$$U(S) = Z'(S) - \eta P(S)$$



EXTENSION: RISKY BOND

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EXTENSION: NON-MIT SHOCKS

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