

# Demographic Trends and the Transmission of Monetary Policy

Giacomo Mangiante

Bank of Italy<sup>1</sup>

ASSA

January, 2024

---

<sup>1</sup>*Disclaimer: The views expressed here are those of the authors alone and do not necessarily represent the views of the Bank of Italy or the Eurosystem*

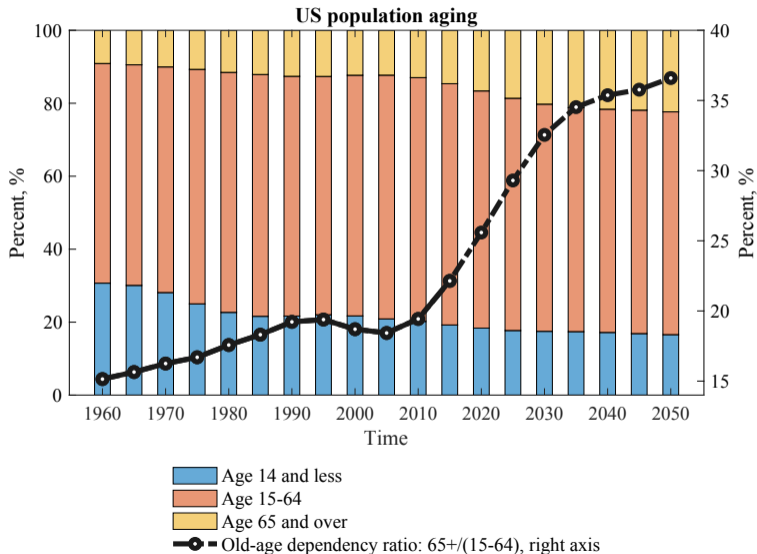
# Table of Contents

- 1 Introduction
- 2 Micro-level evidence
- 3 Theoretical model
  - Demographic trends and MP effectiveness
  - Age-group heterogeneity
  - The importance of consumption heterogeneity
- 4 Conclusion

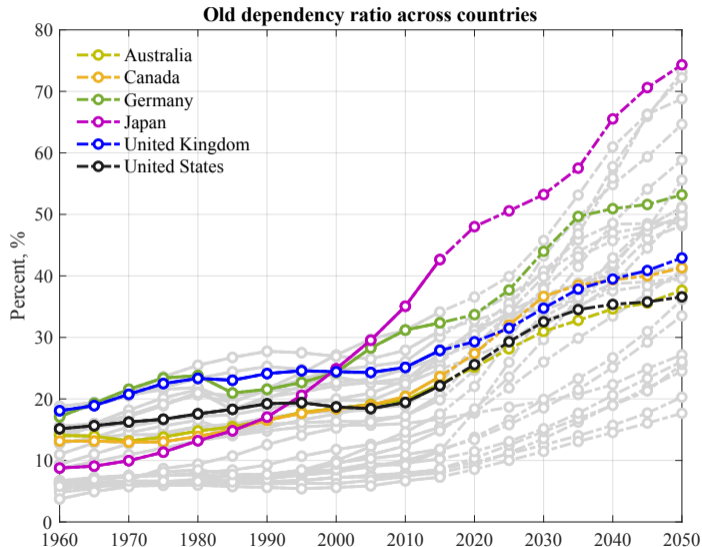
# Table of Contents

- 1 Introduction
- 2 Micro-level evidence
- 3 Theoretical model
  - Demographic trends and MP effectiveness
  - Age-group heterogeneity
  - The importance of consumption heterogeneity
- 4 Conclusion

# Demographic trends, *Source: UN (2017) World Population Prospects*



# Demographic trends, *Source: WB Population Estimate and Projection*



- **Demographic trends** are likely to influence different aspects of the economy (e.g., pension system, savings rates, investment, etc.)

- **Demographic trends** are likely to influence different aspects of the economy (e.g., pension system, savings rates, investment, etc.)
- There are **long-term** effects for monetary policy (MP) as well (e.g., steady-state levels of inflation and interest rates)

- **Demographic trends** are likely to influence different aspects of the economy (e.g., pension system, savings rates, investment, etc.)
- There are **long-term** effects for monetary policy (MP) as well (e.g., steady-state levels of inflation and interest rates)
- What about **short-term** implications?



# This paper

Propose and analyze a **new channel**:

# This paper

Propose and analyze a **new channel**:

⇒ Age groups are **heterogeneous** in their consumption bundles

Propose and analyze a **new channel**:

- ⇒ Age groups are **heterogeneous** in their consumption bundles
- ⇒ Older people purchase more from **price stickier** product categories (prices are adjusted less often)

Propose and analyze a **new channel**:

- ⇒ Age groups are **heterogeneous** in their consumption bundles
- ⇒ Older people purchase more from **price stickier** product categories (prices are adjusted less often)
- ⇒ **Population aging decreases the frequency of price adjustment**

Propose and analyze a **new channel**:

- ⇒ Age groups are **heterogeneous** in their consumption bundles
- ⇒ Older people purchase more from **price stickier** product categories (prices are adjusted less often)
- ⇒ **Population aging decreases the frequency of price adjustment**
- ⇒ Output responds more to MP shocks

- **Micro-level evidence:**

- ▶ Huge **heterogeneity in price stickiness** across consumption bundles of different age groups

- **Micro-level evidence:**

- ▶ Huge **heterogeneity in price stickiness** across consumption bundles of different age groups
- ▶ **Why?**
  - The **services share** of households (HHs) over 80 yo is 20 pp higher wrt one of the HHs in their early 30s.
- ▶ Services adjust their prices on average every 13 months whereas goods every three months
- ▶ The average frequency ranges from **8.2 months for young HHs** to almost **10 for older HHs**

- **Micro-level evidence:**

- ▶ Huge **heterogeneity in price stickiness** across consumption bundles of different age groups
- ▶ **Why?**
  - The **services share** of households (HHs) over 80 yo is 20 pp higher wrt one of the HHs in their early 30s.
- ▶ Services adjust their prices on average every 13 months whereas goods every three months
- ▶ The average frequency ranges from **8.2 months for young HHs** to almost **10 for older HHs**

- **From Micro to Macro:**

- ▶ Output in U.S. states with higher old-age dependency ratio **is more responsive** to MP shocks (not shown today) ▶ Macro evidence



- Develop a **two-sector OLG-NK** model to:
  - ▶ **Estimate the impact** of demographic trends on MP propagation
    - ★ 6% (+10%) in the **responsiveness of output** from 1980 to 2010 (2050) due to demographic trends alone
  - ▶ **Quantify the size** of the new channel (i.e., consumption heterogeneity)
    - ★ Without consumption heterogeneity output responsiveness would increase by only 5.3% by 2050

- **Monetary policy and demographic trends:**

**Theory:** Fujiwara and Teranishi (2008), Carvalho et al. (2016), Yoshino and Miyamoto (2017), Aksoy et al. (2019), Eggertsson et al. (2019), Papetti (2019), Lis et al. (2020), Bielecki et al. (2020), Lisack et al. (2021), Brzoza-Brzezina and Kolasa (2021), ...

**Empirics:** Wong (2014), Bobeica et al. (2017), de Albuquerque et al. (2020), Leahy and Thapar (2022), Berg et al. (2021), Wong (2021), Kopecky (2022), ...

- ▶ *Propose new channel through which dem. trends affect MP effectiveness*

- **Time-varying effects of monetary policy:** Boivin et al. (2010), Imam (2014), Galesi and Rachedi (2018), Kronick and Ambler (2019), Paul (2020), ...

- ▶ *Pop. aging and consumption heterogeneity increase output responsiveness to MP shocks*

# Table of Contents

- 1 Introduction
- 2 Micro-level evidence
- 3 Theoretical model
  - Demographic trends and MP effectiveness
  - Age-group heterogeneity
  - The importance of consumption heterogeneity
- 4 Conclusion

# Age-group level price stickiness

Combine data of:

- **HHs' expenditures** from the **Consumer Expenditure Survey (CEX)**  
Available for around 600 Universal Classification Code (UCC) categories (e.g. *white bread*)

# Age-group level price stickiness

Combine data of:

- **HHs' expenditures** from the **Consumer Expenditure Survey (CEX)**  
Available for around 600 Universal Classification Code (UCC) categories (e.g. *white bread*)
- **Frequency of price adjustment**  $\theta_j$  estimated by **Nakamura and Steinsson (2008)**  
Available for 272 Entry Level Items (ELI) categories (e.g. *bread*)

# Age-group level price stickiness

Combine data of:

- **HHs' expenditures** from the **Consumer Expenditure Survey (CEX)**  
Available for around 600 Universal Classification Code (UCC) categories (e.g. *white bread*)
- **Frequency of price adjustment**  $\theta_j$  estimated by **Nakamura and Steinsson (2008)**  
Available for 272 Entry Level Items (ELI) categories (e.g. *bread*)

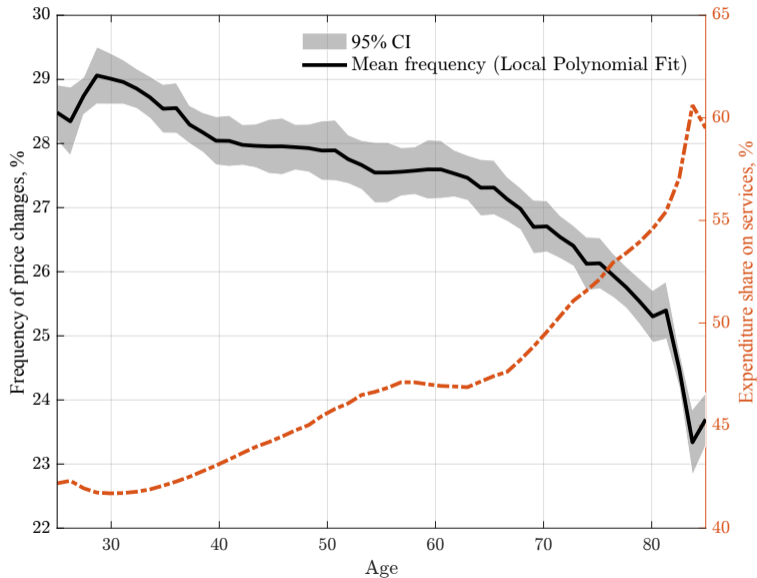
**Age-group price stickiness** level defined as:

$$\theta_t^a = \sum_{j \in J} \omega_{t,j}^a \theta_j$$

with  $\omega_{t,j}^a = \frac{C_{t,j}^a}{\sum_j C_{t,j}^a}$  the **expenditure weight** on category  $j$  for age group  $a$

► Expenditure weights

# Frequency of price adjustment across age groups



- ▶ Over time
- ▶ Expenditure differences
- ▶ Expenditure weights
- ▶ Excluding sales
- ▶ Consumption quantiles
- ▶ Education
- ▶ Service share
- ▶ Alternative aggregation

# Table of Contents

- 1 Introduction
- 2 Micro-level evidence
- 3 Theoretical model**
  - Demographic trends and MP effectiveness
  - Age-group heterogeneity
  - The importance of consumption heterogeneity
- 4 Conclusion



The **two-sector OLG-NK model** in a nutshell:

- Households
- Firms
- Government
- Monetary Authority

The **two-sector OLG-NK model** in a nutshell:

- Households
  - ▶ Born at age  $j = 1$  (real-life age of 15) and live max  $J = 85$  years
  - ▶ Survive with an **age-specific probability**  $s_j$  from age  $j$  to age  $j + 1$
  - ▶ Work until  $jw = 50$  (real-life age of 64) and then retire
  - ▶  $N_j$  denotes the **relative size of cohort**  $j$ ,  $\sum_{j=1}^J N_j = 1$
- Firms
- Government
- Monetary Authority

The **two-sector OLG-NK model** in a nutshell:

- Households

- ▶ Born at age  $j = 1$  (real-life age of 15) and live max  $J = 85$  years
- ▶ Survive with an age-specific probability  $s_j$  from age  $j$  to age  $j + 1$
- ▶ Work until  $jw = 50$  (real-life age of 64) and then retire
- ▶  $N_j$  denotes the relative size of cohort  $j$ ,  $\sum_{j=1}^J N_j = 1$
- ▶ Choose **aggregate consumption**  $c_{t,j}$
- ▶  $c_{t,j}$  is a CES function of services  $c_{t,j}^S$  and goods  $c_{t,j}^G$
- ▶ **Age-specific preferences**  $\alpha_j$  towards the two categories

- Firms

- Government

- Monetary Authority

The **two-sector OLG-NK model** in a nutshell:

- Households

- ▶ Born at age  $j = 1$  (real-life age of 15) and live max  $J = 85$  years
- ▶ Survive with an age-specific probability  $s_j$  from age  $j$  to age  $j + 1$
- ▶ Work until  $jw = 50$  (real-life age of 64) and then retire
- ▶  $N_j$  denotes the relative size of cohort  $j$ ,  $\sum_{j=1}^J N_j = 1$
- ▶ Choose aggregate consumption  $c_{t,j}$
- ▶  $c_{t,j}$  is a CES function of services  $c_{t,j}^S$  and goods  $c_{t,j}^G$
- ▶ Age-specific preferences  $\alpha_j$  towards the two categories
- ▶ **Workers** supply labor, **retirees** receive pension
- ▶ Capital, bonds, and firms' shares are transferred to perfectly competitive and risk-neutral **investment funds** ▶ Equations

- Firms

- Government

- Monetary Authority

The **two-sector OLG-NK model** in a nutshell:

- Households
- Firms
  - ▶ **Perfectly competitive** final-goods firms: **Services** and **Goods**
  - ▶ **Monopolistically competitive** intermediate-good producers
- Government
- Monetary Authority

The **two-sector OLG-NK model** in a nutshell:

- Households
- Firms
  - ▶ Perfectly competitive final-goods firms: Services and Goods
  - ▶ Monopolistically competitive intermediate-good producers
  - ▶ Services need to be consumed once produced
  - ▶ **Calvo price adjustment** mechanism: a fraction  $\theta$  of firms **cannot** reset their prices each period
  - ▶ From the data services adjust prices every 13 months, goods every 3  $\Rightarrow \theta^S > \theta^G$
- Government
- Monetary Authority

The **two-sector OLG-NK model** in a nutshell:

- Households
- Firms
- Government
  - ▶ Taxes labor income of workers ▶ Equations
  - ▶ Provides pension benefit for retirees
- Monetary Authority
  - ▶ Sets interest rate based on a Taylor rule

# Households

The value function of the **representative household** of age  $j$  at time  $t$  is:

$$V_{t,j} = \max_{c_{t,j}, l_{t,j}, a_{t+1,j+1}} u(c_{t,j}, l_{t,j}) + \beta s_j \mathbb{E}_t V_{t+1,j+1},$$

with

$$c_{t,j} = \left[ \alpha_j \frac{1}{\eta} (c_{t,j}^S)^{\frac{\eta-1}{\eta}} + (1 - \alpha_j) \frac{1}{\eta} (c_{t,j}^G)^{\frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}}$$



# Households

The value function of the **representative household** of age  $j$  at time  $t$  is:

$$V_{t,j} = \max_{c_{t,j}, l_{t,j}, a_{t+1,j+1}} u(c_{t,j}, l_{t,j}) + \beta s_j \mathbb{E}_t V_{t+1,j+1},$$

with

$$c_{t,j} = \left[ \alpha_j \frac{1}{\eta} (c_{t,j}^S)^{\frac{\eta-1}{\eta}} + (1 - \alpha_j) \frac{1}{\eta} (c_{t,j}^G)^{\frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}}$$

subject to:

$$P_{t,j} c_{t,j} + a_{t+1,j+1} = a_{t,j} R_t^a + y_{t,j}$$

$$y_{t,j} = (1 - \tau_t) w_t n_{t,j} h_j \mathbf{1}_{j \leq j_w} + pen_t \mathbf{1}_{j > j_w} + beq_t$$

$$a_{t,0} = 0 \quad a_{t+J+1,J+1} = 0$$

The utility function takes the form:

$$u(c_{t,j}, l_{t,j}) = \left( \frac{c_{t,j}^{1-\sigma}}{1-\sigma} - \nu \frac{l_{t,j}^{1+\eta}}{1+\eta} \right)$$

- The model is used to compare the **transmission of MP** shocks around **3 steady states**:
  - ▶ 1980 (baseline), when CEX data becomes available
  - ▶ 2010
  - ▶ 2050, using population projection from World Bank

# Quantitative analysis

- The model is used to compare the **transmission of MP** shocks around **3 steady states**:
    - ▶ 1980 (baseline), when CEX data becomes available
    - ▶ 2010
    - ▶ 2050, using population projection from World Bank
  - The three steady states differ only in terms of:
    - ▶ **population distribution**  $N_j$  ▶ Population distribution
    - ▶ **mortality rate**  $(1 - s_j)$  ▶ Mortality rate
    - ▶ **service preferences**  $\alpha_j$  ▶ Service share ▶ Labor efficiency
- all the other parameters are kept fixed

# Quantitative analysis

- The model is used to compare the **transmission of MP** shocks around **3 steady states**:
    - ▶ 1980 (baseline), when CEX data becomes available
    - ▶ 2010
    - ▶ 2050, using population projection from World Bank
  - The three steady states differ only in terms of:
    - ▶ **population distribution**  $N_j$  ▶ Population distribution
    - ▶ **mortality rate**  $(1 - s_j)$  ▶ Mortality rate
    - ▶ **service preferences**  $\alpha_j$  ▶ Service share ▶ Labor efficiency
- all the other parameters are kept fixed

Answer the following **questions**:

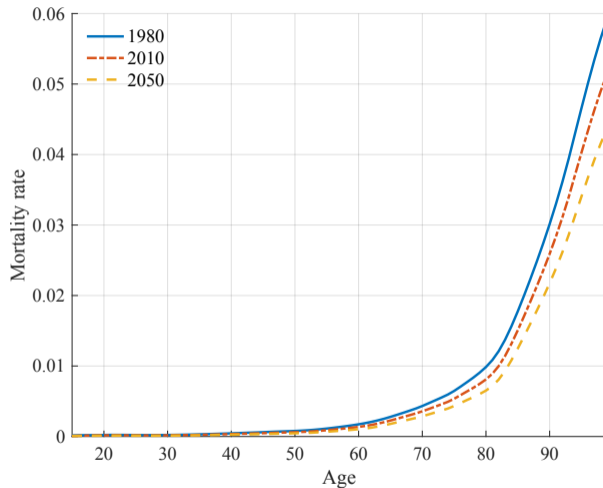
- Do demographic trends **change** the way MP propagates in the U.S.?
- **To what extent** consumption heterogeneity across age groups contributes?

# Calibration

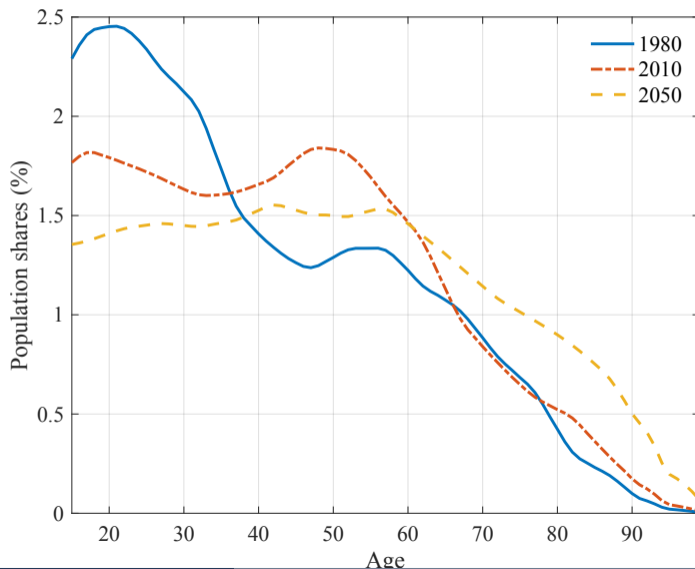
Parameter	Value	Description	Target
$\beta$	0.999	Discount factor	Annual interest rate between 4 and 5 %
$\delta$	0.02	Depreciation rate	Capital-output ratio between 2 and 2.7
$\sigma$	1	Intertemporal elasticity of substitution	Standard value
$\phi$	2	Frisch elasticity of labor supply	Standard value
$N_j$	▸ Population distribution	Population shares. Source: World Bank	
$s_j$	▸ Mortality rate	Survival probability. Source: Social Security Administration	
$\alpha_j$	▸ Service share	Share of consumption devoted to services. Source: CEX	
$h_j$	▸ Labor efficiency	Individual life-cycle labor supply in efficiency units from <a href="#">Fullerton (1999)</a>	Wage profile
$\epsilon$	6	Elasticity of demand for each intermediate good	Steady-state markup of 20 %
$\theta^S$	0.75	Calvo Frequency Services. Source: <a href="#">Nakamura and Steinsson (2008)</a>	Price adjustment every 13 months
$\theta^G$	0.25	Calvo Frequency Goods. Source: <a href="#">Nakamura and Steinsson (2008)</a>	Price adjustment every 3 months
$\alpha$	0.33	Capital share	Standard value

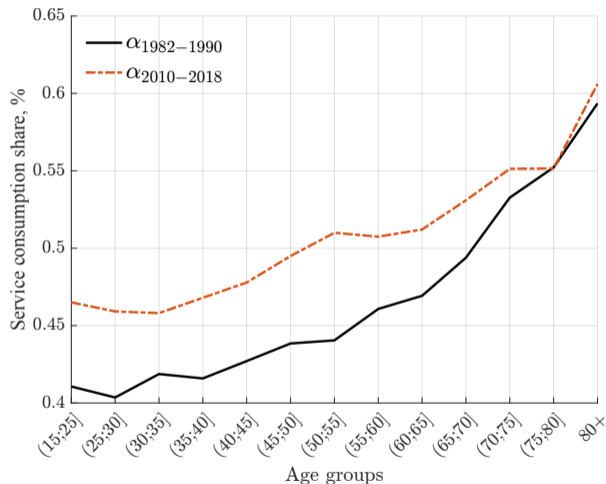
The most important parameters are  $N_j$ ,  $s_j$  and  $\alpha_j$

# Mortality rate across age groups [▶ Back](#)



**Mortality rate** has decreased over time

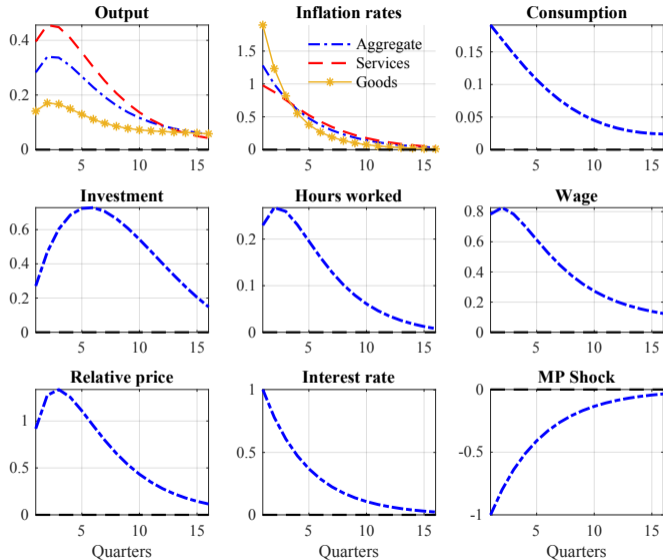




**Income and price effects** have increased the share of services consumed



# Model impulse response function to MP shock

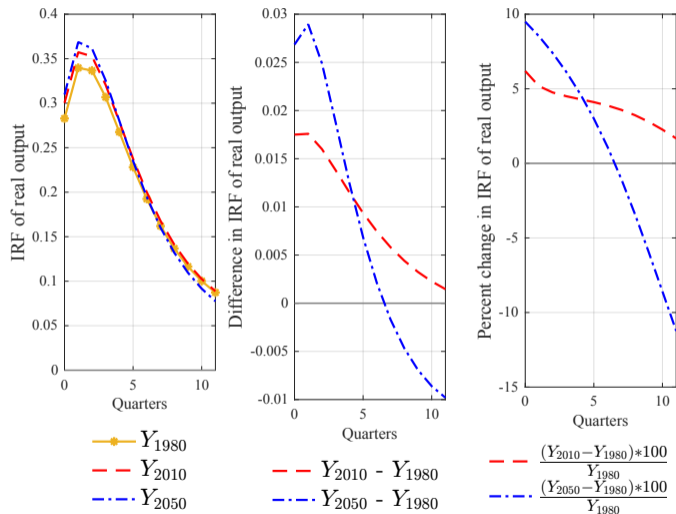


IRFs to a 100 bp expansionary  
MP shocks ▶ Age responses

# Outline

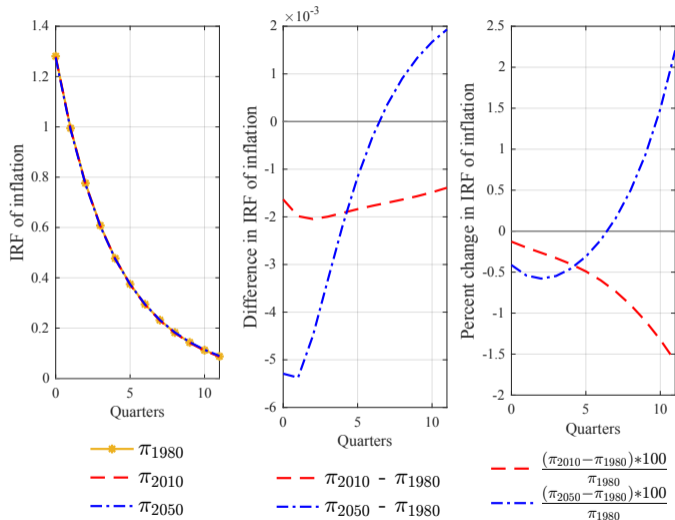
- 1 Introduction
- 2 Micro-level evidence
- 3 Theoretical model**
  - Demographic trends and MP effectiveness
  - Age-group heterogeneity
  - The importance of consumption heterogeneity
- 4 Conclusion

# IRFs difference wrt baseline (changing only dem.), output



IRFs with  $N_j$  and  $s_j$  for  $\{1980, 2010, 2050\}$ ,  $\alpha_j$  fixed at 1980 values

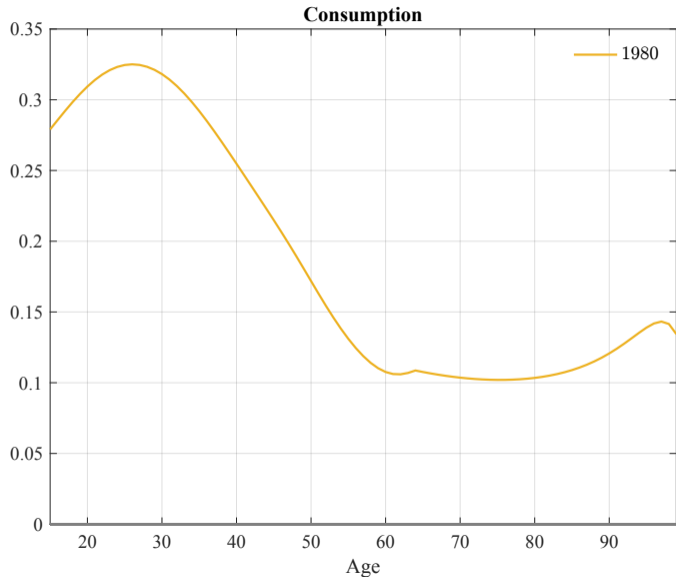
# IRFs difference wrt baseline (changing only dem.), inflation



IRFs with  $N_j$  and  $s_j$  for  
 {1980, 2010, 2050},  
 $\alpha_j$  fixed at 1980 values

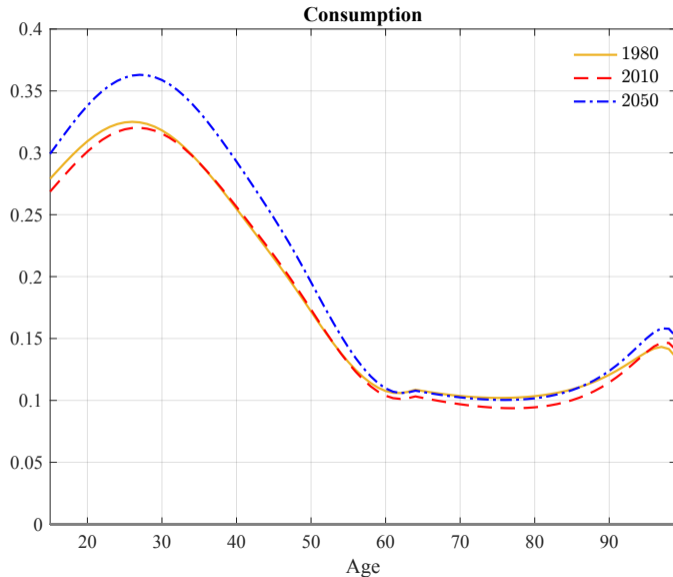
- 1 Introduction
- 2 Micro-level evidence
- 3 Theoretical model**
  - Demographic trends and MP effectiveness
  - **Age-group heterogeneity**
  - The importance of consumption heterogeneity
- 4 Conclusion

# IRF by age



Young households are the most exposed to MP shocks

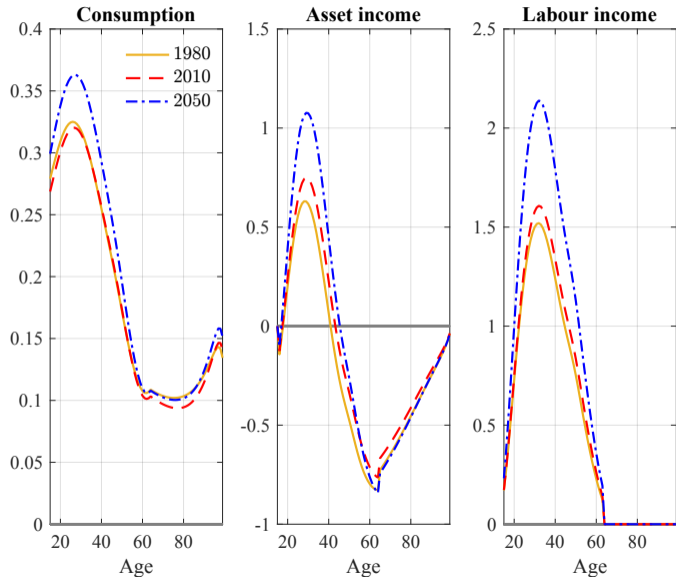
# IRF by age over time



The consumption of **young households** is also increasing in responsiveness

► Empirical evidence

# IRF by age over time



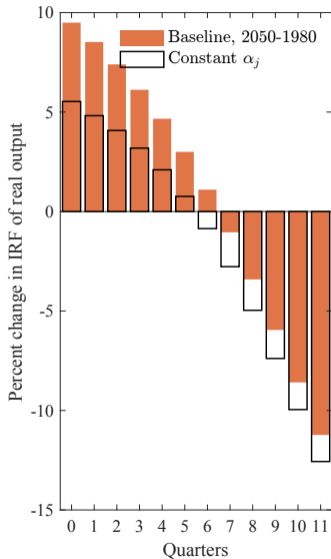
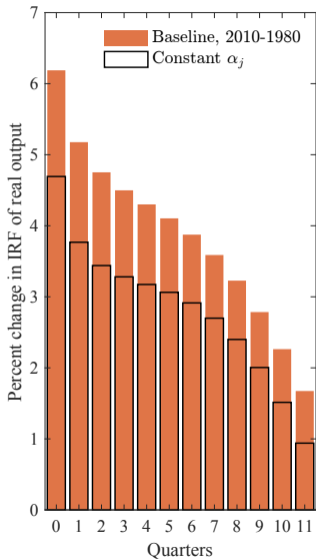
Asset and labour income  
are becoming more responsive



# Outline

- 1 Introduction
- 2 Micro-level evidence
- 3 Theoretical model**
  - Demographic trends and MP effectiveness
  - Age-group heterogeneity
  - **The importance of consumption heterogeneity**
- 4 Conclusion

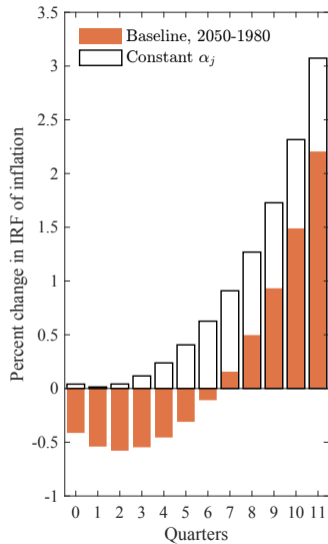
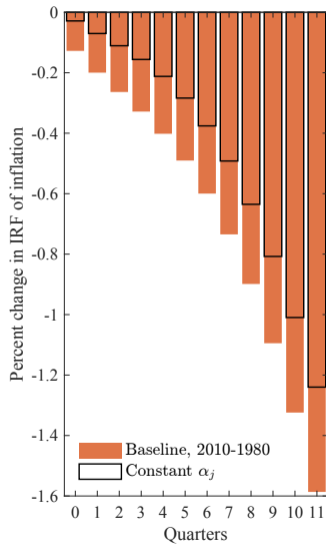
# Size of the new channel, Output



IRFs with change in  $N_j$  and  $s_j$ ;  
Age-specific  $\alpha$  vs Constant  $\alpha$

► Contribution demographics

# Size of the new channel, Inflation



IRFs with change in  $N_j$  and  $s_j$ ;  
 Age-specific  $\alpha$  vs Constant  $\alpha$

# Sensitivity analysis

Response of Output and Inflation - Robustness Checks

	Output response (%)			Inflation response (%)		
	Time 0	After 1 year	After 2 years	Time 0	After 1 year	After 2 years
Baseline	6.18	4.30	3.22	-0.12	-0.40	-0.89
Different $\psi$	5.63	4.01	2.93	-0.07	-0.26	-0.64
Different $\epsilon$	5.07	3.72	2.83	-0.15	-0.34	-0.63
Different $\phi$	6.97	4.58	2.95	-0.12	-0.36	-0.82
Constant $\tau$	5.79	4.03	3.02	-0.09	-0.31	-0.71
$\theta^G = \theta^S$	2.78	3.85	2.79	-0.02	-0.21	-1.09

Percent change in IRFs of output and inflation between 1980 to 2010 under **alternative assumptions** of the model ▶ Different  $\theta$

# Table of Contents

- 1 Introduction
- 2 Micro-level evidence
- 3 Theoretical model
  - Demographic trends and MP effectiveness
  - Age-group heterogeneity
  - The importance of consumption heterogeneity
- 4 Conclusion

## Main results:

- **Negative relationship** between age and the frequency of price adjustments
- This translates in **stronger response** in economic activity for older U.S. states

## Main results:

- **Negative relationship** between age and the frequency of price adjustments
- This translates in **stronger response** in economic activity for older U.S. states
- Develop a **two-sector OLG-NK model** calibrated for the U.S.:
  - ▶ Dem. trends increased **output responsiveness** of +6% (+10%) from 1980 to 2010 (2050)
  - ▶ **Consumption heterogeneity** across age groups sizably contribute to this

## Main results:

- **Negative relationship** between age and the frequency of price adjustments
- This translates in **stronger response** in economic activity for older U.S. states
- Develop a **two-sector OLG-NK model** calibrated for the U.S.:
  - ▶ Dem. trends increased **output responsiveness** of +6% (+10%) from 1980 to 2010 (2050)
  - ▶ **Consumption heterogeneity** across age groups sizably contribute to this

## Policy implications for Central Banks:

- **Population aging matters for MP short-term decisions as well**
- Dem. trends increase price stickiness  $\Rightarrow$  Output more responsive
- **Younger households** are more exposed  $\Rightarrow$  Fiscal policies to stabilize



Thank you for your attention!

- Aksoy, Y., Basso, H. S., Smith, R. P., , and Grasl, T. (2019). "Demographic Structure and Macroeconomic Trends". *American Economic Journal: Macroeconomics 2019*, 11(1): 193–222.
- Berg, K., Curtis, C., Lugauer, S., and Mark, N. C. (2021). "Demographics and Monetary Policy Shocks". *Journal of Money, Credit, and Banking*.
- Bielecki, M., Brzoza-Brzezina, M., and Kolasab, M. (2020). "Demographics and the natural interest rate in the euro area". *European Economic Review*, Volume 129.
- Bobeica, E., Nickel, C., Lis, E., and Sun, Y. (2017). "Demographics and inflation". *ECB Working Paper No 2006*.
- Boivin, J., Kiley, M. T., and Mishkin, F. S. (2010). "How Has the Monetary Transmission Mechanism Evolved Over Time?". *Handbook of Monetary Economics, Volume 3, 2010*, Pages 369-422 Chapter 8.

## References II

- Brzoza-Brzezina, M. and Kolasa, M. (2021). "Intergenerational redistributive effects of monetary policy". *Journal of European Economic Association* 20(2): 549-580 (2022).
- Carvalho, C., Ferrero, A., and Nechio, F. (2016). "Demographics and real interest rates: Inspecting the mechanism". *European Economic Review* 88 (2016) 208–226.
- de Albuquerque, P. C. A. M., Caiado, J., and Pereira, A. (2020). "Population aging and inflation: evidence from panel cointegration". *Journal of Applied Economics* 23(1), 469–484.
- Eggertsson, G. B., Mehrotra, N. R., and Robbins, J. A. (2019). "Population Aging and the Macroeconomy". *A Model of Secular Stagnation: Theory and Quantitative Evaluation*.
- Fujiwara, I. and Teranishi, Y. (2008). "A dynamic new Keynesian life-cycle model: Societal aging, demographics, and monetary policy". *Journal of Economic Dynamics and Control* 32 (2008) 2398–2427.
- Fullerton, H. N. (1999). "Labor force participation: 75 years of change, 1950-98 and 1998-2025". *Monthly Labor Review*, 122:3–12.

## References III

- Galesi, A. and Rachedi, O. (2018). "Services Deepening and the Transmission of Monetary Policy". *Journal of the European Economic Association*, Volume 17, Issue 4, August 2019, Pages 1261–1293.
- Hazell, J., Herreno, J., Nakamura, E., and Steinsson, J. (2022). "The Slope of the Phillips Curve: Evidence from U.S. States". *Quarterly Journal of Economics*, 137(3), 1299-1344.
- Imam, P. (2014). "Shock from Greying: Is the Demographic Shift Weakening Monetary Policy Effectiveness". *International Journal of Finance & Economics*.
- Jordà, O. (2005). "Estimation and Inference of Impulse Responses by Local Projections". *American Economic Review*, 95 (1), 161–182.
- Kopecky, J. (2022). "Okay Boomer... Excess Money Growth, Inflation, and Population Aging". *Macroeconomic Dynamics*.
- Kronick, J. and Ambler, S. (2019). "Do Demographics Affect Monetary Policy Transmission in Canada?". *International Journal of Finance and Economics*. Vol. 24(2), pg. 787–811. April.

## References IV

- Leahy, J. and Thapar, A. (2022). "Age Structure and the Impact of Monetary Policy". *American Economic Journal: Macroeconomics*. 14, NO. 4, 136-73.
- Lis, E., Nickel, C., and Papetti, A. (2020). "Demographics and inflation in the euro area: a two-sector new Keynesian perspective". *Working Paper Series 2382, European Central Bank*.
- Lisack, N., Sajedi, R., and Thwaites, G. (2021). "Population Aging and the Macroeconomy". *International Journal of Central Banking*.
- Nakamura, E. and Steinsson, J. (2008). "Five facts about prices: a reevaluation of menu cost models". *The Quarterly Journal of Economics*, Volume 123, Issue 4, November 2008, Pages 1415–1464.
- Papetti, A. (2019). "Demographics and the natural real interest rate: historical and projected paths for the euro area". *Working Paper Series 2258, European Central Bank*.
- Paul, P. (2020). "The Time-Varying Effect of Monetary Policy on Asset Prices". *The Review of Economics and Statistics* (2020) 102 (4): 690–704.

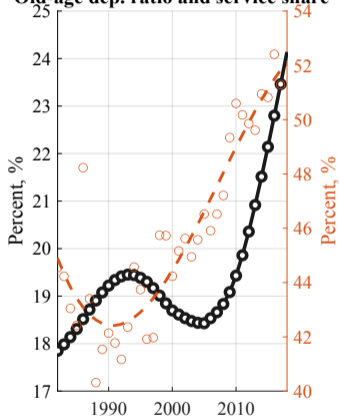
## References V

- Ramey, V. (2016). "Macroeconomic shocks and their propagation". *In Handbook of Macroeconomics. Vol. 2, 71.*
- Romer, C. D. and Romer, D. H. (2004). "A new measure of monetary shocks: Derivation and implications". *American Economic Review 94(4), 1055-84.*
- Wong, A. (2014). "Population Aging and the Aggregate Effects of Monetary Policy". *MPRA Paper No. 57096, University Library of Munich, Germany.*
- Wong, A. (2021). "Refinancing and The Transmission of Monetary Policy to Consumption". *R&R American Economic Review.*
- Yoshino, N. and Miyamoto, H. (2017). "Declined effectiveness of fiscal and monetary policies faced with aging population in Japan". *Japan and the World Economy 42 (2017) 32-44.*

# Old-age dependency ratio, service share, and price stickiness

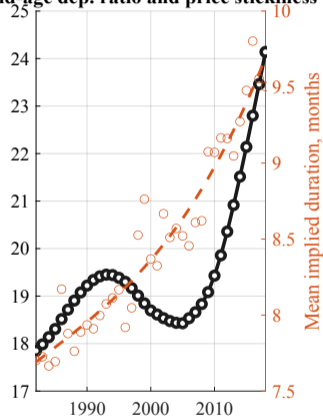
▶ Back

### Old-age dep. ratio and service share



—●— Old-age dependency ratio  
○ Service share (right axis)  
- - - Local pol. fit (right axis)

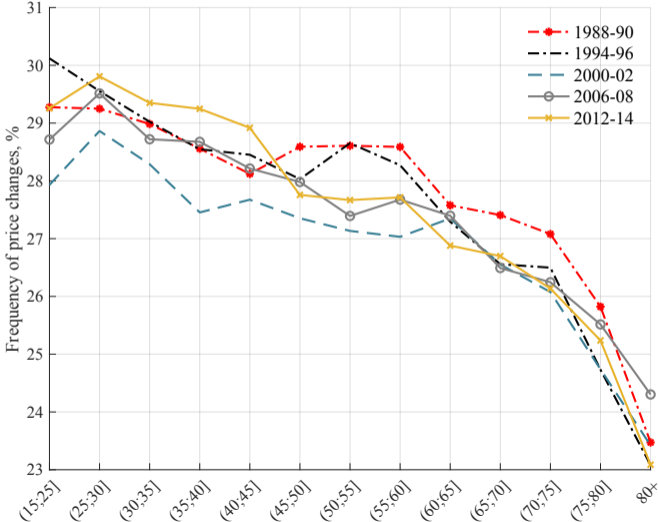
### Old-age dep. ratio and price stickiness



—●— Old-age dependency ratio  
○ Mean implied duration (right axis)  
- - - Local pol. fit (right axis)

# Across age groups and time

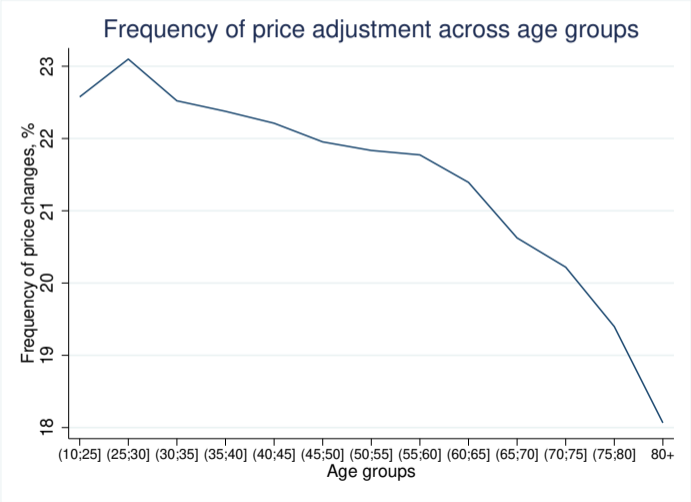
▶ Back





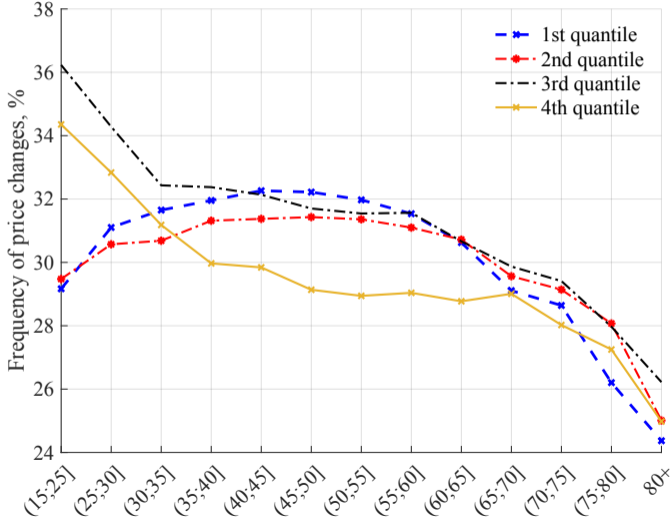
# Frequency of price adjustment excluding sales

▶ Back



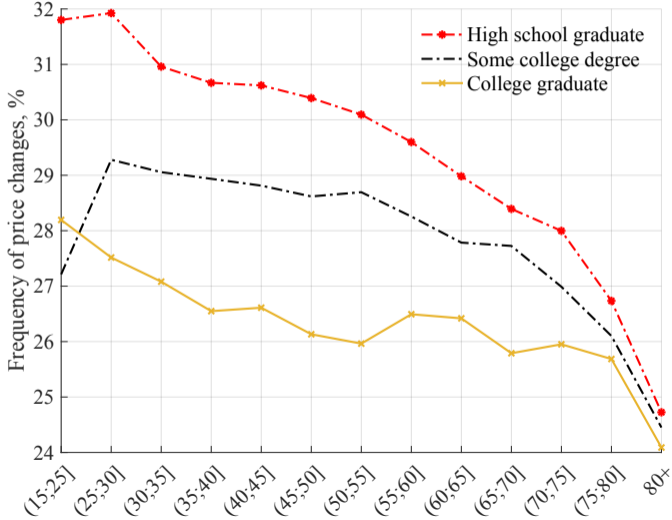
# Across age groups and consumption quantiles

▶ Back

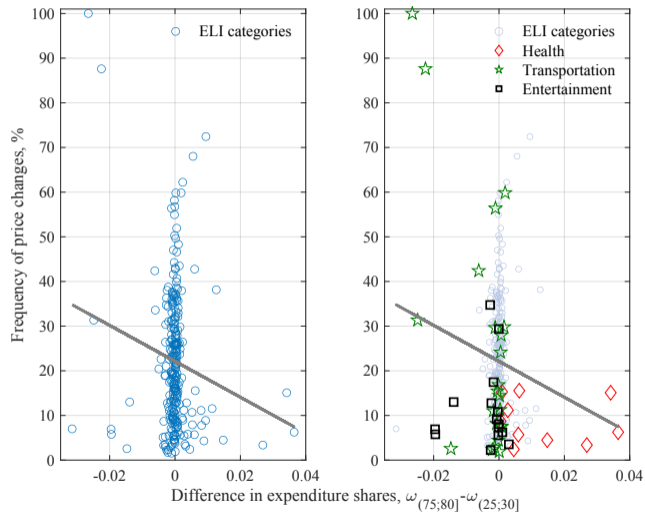


# Across age groups and education levels

▶ Back

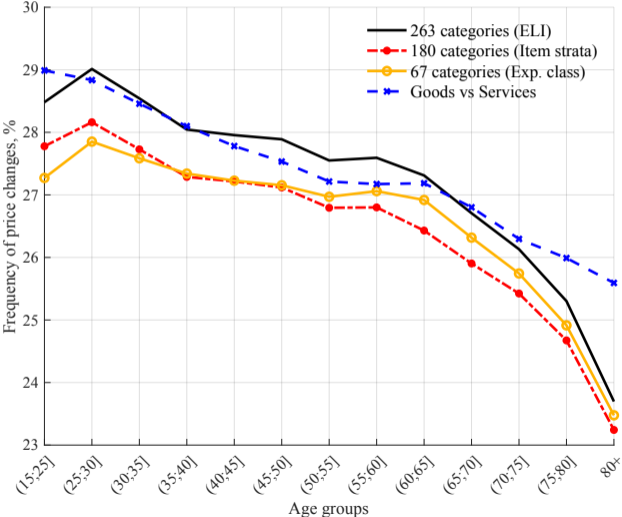


# Expenditure differences across age group



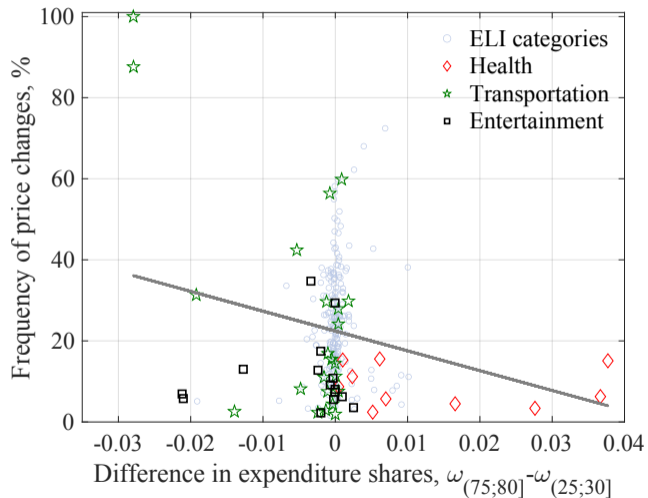
# Alternative aggregation

▶ Back



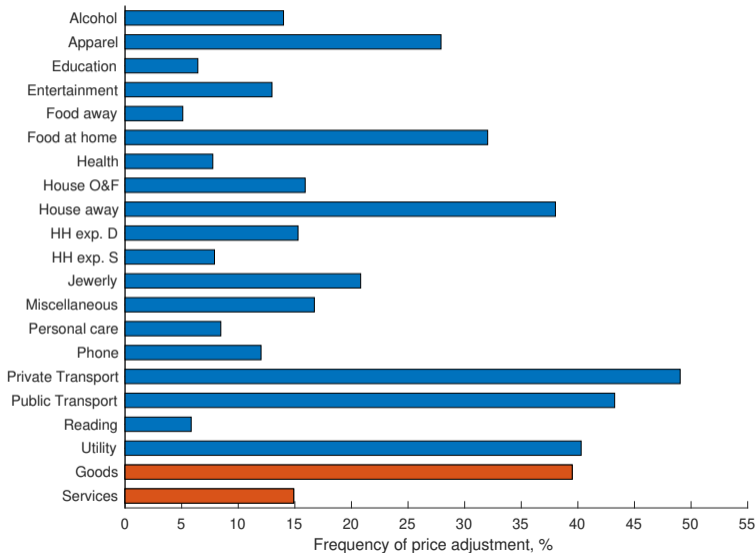
# Expenditure differences across age group

▶ Back

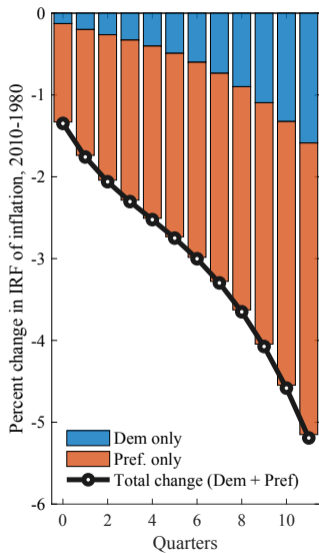
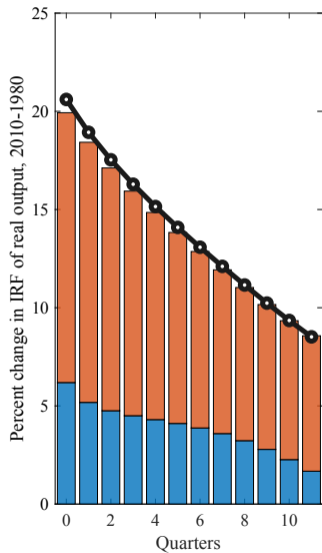


# Price stickiness across categories

▶ Back



# Contribution from demographics change



Blue bars: change in  $N_j$  and  $s_j$ ; fixed  $\alpha_j$   
Orange bars: fixed  $N_j$  and  $s_j$ ; change in  $\alpha_j$

▶ Back



# Within-between decomposition

What percentage of the increase in the share of services in total consumption is explained by changes in the age distribution?

The **share of services** in aggregate consumption can be written as:

$$\alpha_t^s = \frac{\sum_a C_t^{s,a}}{\sum_a \sum_j C_t^{j,a}} = \sum_a \alpha_t^{s,a} s_t^a$$

with  $\alpha_t^{s,a} = \frac{C_t^{s,a}}{\sum_j C_t^{j,a}}$  and  $s_t^a = \frac{\sum_j C_t^{j,a}}{\sum_a \sum_j C_t^{j,a}}$

# Within-between decomposition

What percentage of the increase in the share of services in total consumption is explained by changes in the age distribution?

The **share of services** in aggregate consumption can be written as:

$$\alpha_t^s = \frac{\sum_a C_t^{s,a}}{\sum_a \sum_j C_t^{j,a}} = \sum_a \alpha_t^{s,a} s_t^a$$

with  $\alpha_t^{s,a} = \frac{C_t^{s,a}}{\sum_j C_t^{j,a}}$  and  $s_t^a = \frac{\sum_j C_t^{j,a}}{\sum_a \sum_j C_t^{j,a}}$

The change in services between  $t_1$  and  $t_2$  can then be decomposed in:

$$\Delta \alpha_t^s = \underbrace{\sum_a \Delta \alpha^{s,a} \bar{s}^a}_{\text{Within}} + \underbrace{\sum_a \bar{\alpha}^{s,a} \Delta s^{s,a}}_{\text{Between}}$$

with  $\Delta x = x_{t_2} - x_{t_1}$  and  $\bar{x} = \frac{x_{t_2} + x_{t_1}}{2}$  for any variable  $x$ .

# Within-between decomposition

$$\Delta\alpha_t^s = \underbrace{\sum_a \Delta\alpha^{s,a} \bar{s}^a}_{\text{Within}} + \underbrace{\sum_a \bar{\alpha}^{s,a} \Delta s^{s,a}}_{\text{Between}}$$

Within-between decomposition, 1982-1990 to 2010-2018

	Service share	Contribution	Implied duration, months
Within	0.044	72.3 %	0.42 (+5.4 %)
Between	0.017	27.7 %	0.16 (+2.1 %)
Total	0.061	100 %	0.58 (+7.5 %)
	(46.69 % to 52.75 %)		(7.83 to 8.42)

**Micro-level evidence** suggests:

↑ old-age dependency ratio  $\Rightarrow$  ↑ demand of services  $\Rightarrow$  ↑ price stickiness  $\Rightarrow$   
 $\Rightarrow$  ↑ output responsiveness at macro-level

**Micro-level evidence** suggests:

↑ old-age dependency ratio  $\Rightarrow$  ↑ demand of services  $\Rightarrow$  ↑ price stickiness  $\Rightarrow$   
 $\Rightarrow$  ↑ output responsiveness at macro-level

- *Identification problem*: Negligible **variation over time** in the U.S. demographic structures

**Micro-level evidence** suggests:

↑ old-age dependency ratio  $\Rightarrow$  ↑ demand of services  $\Rightarrow$  ↑ price stickiness  $\Rightarrow$   
 $\Rightarrow$  ↑ output responsiveness at macro-level

- *Identification problem*: Negligible **variation over time** in the U.S. demographic structures
- *Solution*: Exploit the **cross-sectional variation** among U.S. states

**Micro-level evidence** suggests:

↑ old-age dependency ratio  $\Rightarrow$  ↑ demand of services  $\Rightarrow$  ↑ price stickiness  $\Rightarrow$   
 $\Rightarrow$  ↑ output responsiveness at macro-level

- *Identification problem*: Negligible **variation over time** in the U.S. demographic structures
- *Solution*: Exploit the **cross-sectional variation** among U.S. states

Old-dependency ratio:

- ▶ 1980 - U.S. 16%; States [11%, 27%]
- ▶ 2010 - U.S. 20%; States [14%, 27%]
- ▶ Average within-state increase in old-dep. ratio is around 3pp

**Micro-level evidence** suggests:

↑ old-age dependency ratio  $\Rightarrow$  ↑ demand of services  $\Rightarrow$  ↑ price stickiness  $\Rightarrow$   
 $\Rightarrow$  ↑ output responsiveness at macro-level

- *Identification problem*: Negligible **variation over time** in the U.S. demographic structures
- *Solution*: Exploit the **cross-sectional variation** among U.S. states

Old-dependency ratio:

- ▶ 1980 - U.S. 16%; States [11%, 27%]
  - ▶ 2010 - U.S. 20%; States [14%, 27%]
  - ▶ Average within-state increase in old-dep. ratio is around 3pp
- *Prediction*: Economic activity in “*older*” U.S. states should **react more** to MP shocks

[▶ State variation](#)

[▶ Services](#)

[▶ Health](#)



## Average state level response

*Prediction:* Economic activity in “older” U.S. states should **react more** to MP shocks

Estimate the **average state level response** to MP shock with Local Projection à la [Jordà \(2005\)](#):

$$y_{i,t+h} = \alpha_{i,h} + \beta_h MP_t + \theta_{i,h} X_{i,t-1} + \gamma_h X_{t-1} + \epsilon_{i,t+h}$$

for  $h = 1, \dots, 16$

# Average state level response

*Prediction:* Economic activity in “older” U.S. states should **react more** to MP shocks

Estimate the **average state level response** to MP shock with Local Projection à la [Jordà \(2005\)](#):

$$y_{i,t+h} = \alpha_{i,h} + \beta_h MP_t + \theta_{i,h} X_{i,t-1} + \gamma_h X_{t-1} + \epsilon_{i,t+h}$$

for  $h = 1, \dots, 16$

- **Dependent variable**  $y_{i,t}$  for state  $i$  at time  $t$ :
  - ▶ Real Personal Income from the Bureau of Economic Analysis (BEA)
  - ▶ Annual inflation rate from [Hazell et al. \(2022\)](#)
  - ▶ GDP from the BEA (annual frequency)
- $MP_t$  are the [Romer and Romer \(2004\)](#) shocks

# Average state level response

*Prediction:* Economic activity in “older” U.S. states should **react more** to MP shocks

Estimate the **average state level response** to MP shock with Local Projection à la [Jordà \(2005\)](#):

$$y_{i,t+h} = \alpha_{i,h} + \beta_h MP_t + \theta_{i,h} X_{i,t-1} + \gamma_h X_{t-1} + \epsilon_{i,t+h}$$

for  $h = 1, \dots, 16$

- **Dependent variable**  $y_{i,t}$  for state  $i$  at time  $t$ :
  - ▶ Real Personal Income from the Bureau of Economic Analysis (BEA)
  - ▶ Annual inflation rate from [Hazell et al. \(2022\)](#)
  - ▶ GDP from the BEA (annual frequency)
- $MP_t$  are the [Romer and Romer \(2004\)](#) shocks
- **State controls**  $X_{i,t-1}$ : lagged dependent variable and population size
- **Aggregate controls**  $X_{t-1}$  as in [Ramey \(2016\)](#): IP, CPI, FFR, unemployment rate and commodity price index
- Standard errors are clustered at state level

## Percentile level responses

*Prediction:* Economic activity in “older” U.S. states should **react more** to MP shocks

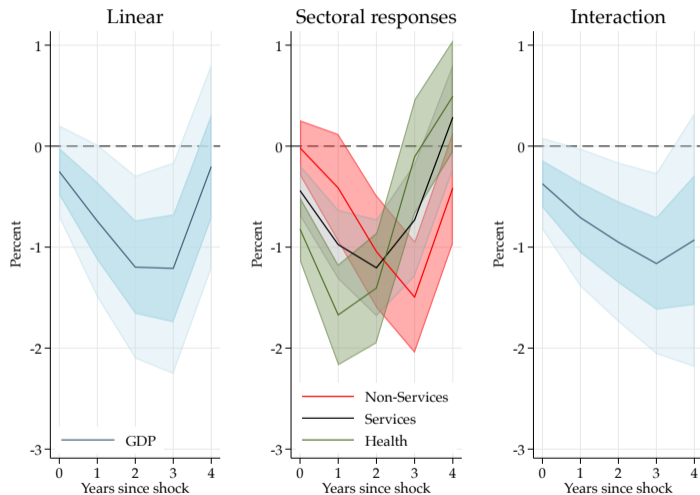
To evaluate the role of demographic structure, extend **baseline specification**:

$$y_{i,t+h} = \alpha_{i,h} + \beta_h MP_t + \theta_{i,h} X_{i,t-1} + \gamma_h X_{t-1} + \epsilon_{i,t+h}$$

with **dummy variable**  $D_{i,t}^O$  equal 1 for top quintile of the old-age dependency distribution:

$$y_{i,t+h} = \alpha_{i,h} + \delta_{t,h} + \gamma_h D_{i,t}^O + \beta_h^O D_{i,t}^O MP_t + \theta_{i,h} X_{i,t-1} + \epsilon_{i,t+h},$$

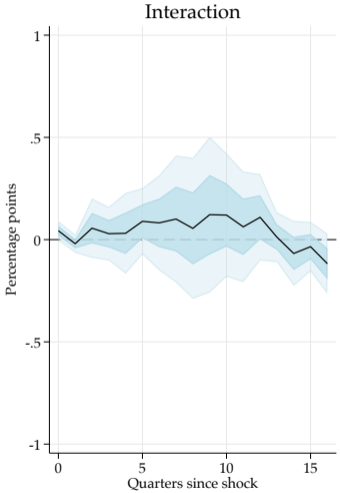
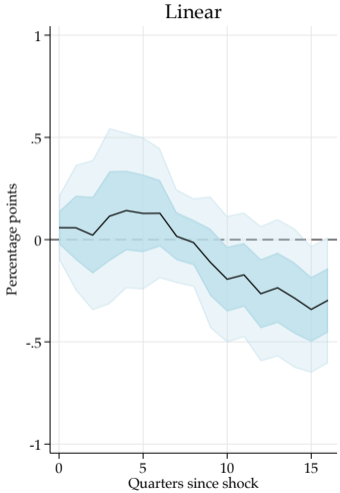
# IRF real GDP, 68% and 95% CI



Economic activity  
in “*older*” U.S. states  
is **more responsive**

▶ Service contribution

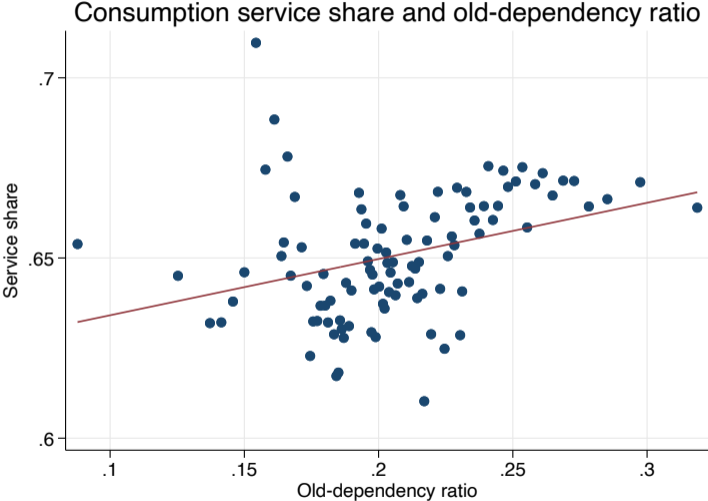
# IRF Inflation rate, 68% and 95% CI



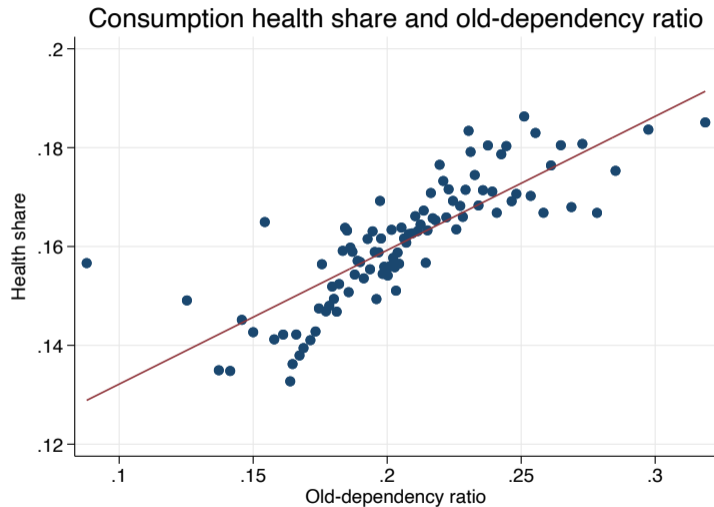
No significant differences for **inflation rate**

# Robustness checks

- Above/below median [▶ Go](#)
- Top/bottom 10 % [▶ Go](#)
- Share of working population [▶ Go](#)
- No financial crisis [▶ Go](#)
- Controlling for income [▶ Go](#)
- Excluding small states [▶ Go](#)
- High-frequency identification with IV-LP [▶ Go](#)
- Services [▶ Go](#)







The firms side has two sectors:

- **services** and **goods**
- Each sector has competitive final goods firm and a continuum of monopolistically competitive intermediate goods firms (standard NK model)
- Different frequency of price adjustment
- Only the output of the goods-sector can be used for capital investment

**Price stickiness:** Each period a fraction  $\theta^S$  of intermediate producers cannot reset their price,  $\theta^S > \theta^G$ .

▶ Market clearing

▶ Back

# Market clearing

Both aggregate labor and capital markets clear:

$$L_t = L_t^S + L_t^G = \sum_{j=1}^{jw} N_j h_j n_{t,j}, \quad K_t = K_t^S + K_t^G = \sum_{j=1}^J N_{j-1} a_{t,j}$$

$$beq_t = \sum_{j=1}^J (N_{j-1} - N_j) a_{t,j} R_t^a$$

The markets of goods and services clear:

$$Y_t^S = (K_t^S)^\alpha (L_t^S)^{1-\alpha} = C_t^S$$

$$Y_t^G = (K_t^G)^\alpha (L_t^G)^{1-\alpha} = C_t^G + I_t$$

and bonds are in zero net supply,  $B_t = 0$ .

# Investment funds

The FOCs of the representative investment fund are:

$$K_{t+1} = (1 - \delta)K_t + \left[1 - \frac{S}{2}\left(\frac{I_t}{I_{t-1}} - 1\right)^2\right] I_t$$

$$A_{t+1} = q_t(1 - \delta)K_t + I_t + p_t^d$$

$$\frac{R_t^a}{\pi_t} A_t = \left[r_t^k + q_t(1 - \delta)\right] K_t + f_t + p_t^d$$

$$R_t q_t = \mathbb{E}_t \left[ \left( r_{t+1}^k + q_{t+1}(1 - \delta) \right) \pi_{t+1} \right]$$

$$R_t p_t^d = \mathbb{E}_t \left[ \left( p_{t+1}^d + f_{t+1} \right) \pi_{t+1} \right]$$

$$1 = q_t \left[ 1 - \frac{S}{2} \left( \frac{I_t}{I_{t-1}} - 1 \right)^2 - S \left( \frac{I_t}{I_{t-1}} - 1 \right) \frac{I_t}{I_{t-1}} \right] + \mathbb{E}_t \left[ \frac{\pi_{t+1}}{R_t} q_{t+1} S \left( \frac{I_{t+1}}{I_t} - 1 \right) \left( \frac{I_{t+1}}{I_t} \right)^2 \right]$$

# Government and Monetary Authority

The government funds a **pay-as-you-go social security system**. The tax rate on labor income  $\tau_t$  is set such that the budget is balanced in each period.

$$pen_t = \bar{d}(1 - \tau_t)w_t \sum_{j=0}^{jw} N_j h_j$$

$$\tau_t w_t \sum_{j=0}^{jw} N_j h_j = pen_t \sum_{j=jw+1}^J N_j$$

with  $d_t$  the amount of pension benefit and  $\bar{d}$  the replacement rate.

The central bank follows the following simple **Taylor-type rule**:

$$\frac{R_t}{R} = \left(\frac{\Pi_t}{\Pi}\right)^{\phi_\pi} \left(\frac{Y_t}{Y}\right)^{\phi_y} e^{\nu_t^r}$$

# Phillips Curve

The **sectoral Phillips Curve**:

$$\hat{\pi}_t^S = \beta \mathbb{E}_t \hat{\pi}_{t+1}^S + \kappa^S \hat{m}c_t^S$$

$$\hat{\pi}_t^G = \beta \mathbb{E}_t \hat{\pi}_{t+1}^G + \kappa^G \hat{m}c_t^G$$

with

$$\kappa^S = \frac{(1 - \theta^S)(1 - \theta^S \beta)}{\theta^S}, \quad \kappa^G = \frac{(1 - \theta^G)(1 - \theta^G \beta)}{\theta^G}$$

Since  $\theta^S > \theta^G$ , it follows that  $\kappa^S < \kappa^G$ .

# Phillips Curve

The **sectoral Phillips Curve**:

$$\hat{\pi}_t^S = \beta \mathbb{E}_t \hat{\pi}_{t+1}^S + \kappa^S \hat{m}c_t^S$$

$$\hat{\pi}_t^G = \beta \mathbb{E}_t \hat{\pi}_{t+1}^G + \kappa^G \hat{m}c_t^G$$

with

$$\kappa^S = \frac{(1 - \theta^S)(1 - \theta^S \beta)}{\theta^S}, \quad \kappa^G = \frac{(1 - \theta^G)(1 - \theta^G \beta)}{\theta^G}$$

Since  $\theta^S > \theta^G$ , it follows that  $\kappa^S < \kappa^G$ .

It can be shown that:

$$\hat{\pi}_t = \omega \hat{\pi}_t^S + (1 - \omega) \hat{\pi}_t^G = \beta \mathbb{E}_t \hat{\pi}_{t+1} + \left[ \omega \kappa^S + (1 - \omega) \kappa^G \right] (\hat{w}_t - \alpha(\hat{k}_t - \hat{l}_t)) - \lambda \hat{z}_t$$

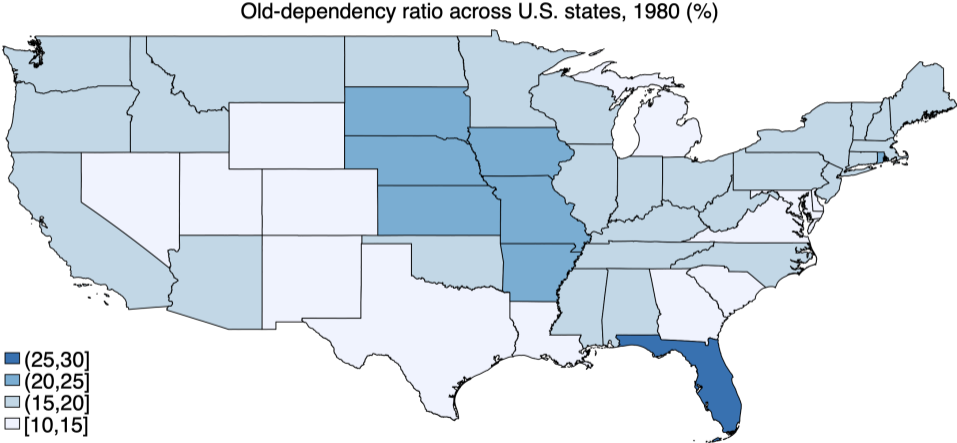
where  $\omega = \sum_j \alpha_j s_j \frac{P_j^{\eta-1}}{\sum_j s_j P_j^{\eta-1}}$ ,  $s_j = \frac{N_j P_j C_j}{\sum_j N_j P_j C_j}$  and  $\hat{z}_t = \log P_t^G - \log P_t^S$ .

## Effect of population aging on the slope of the Phillips Curve

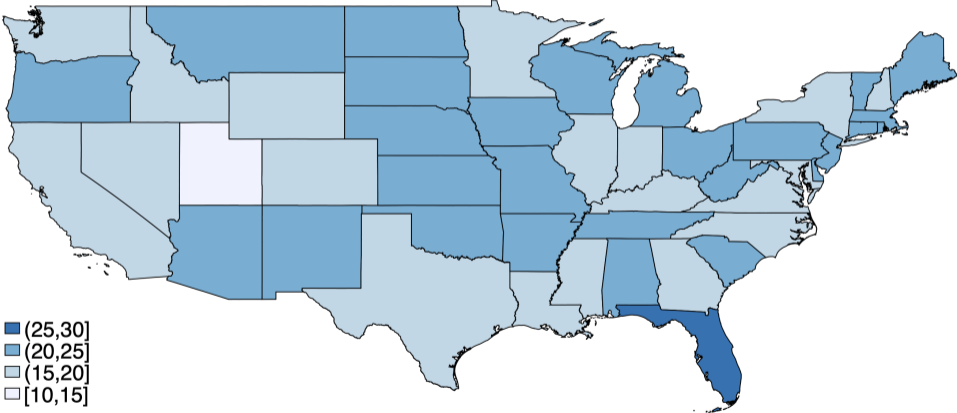
	Baseline 1980	Dem+Pref 2010	Only Dem 2010
Service weight $\omega$	0.4498	0.4953 (+10.11 %)	0.4542 (+0.97 %)
PC slope	1.2759	1.1773 (-7.72 %)	1.2665 (-0.74 %)



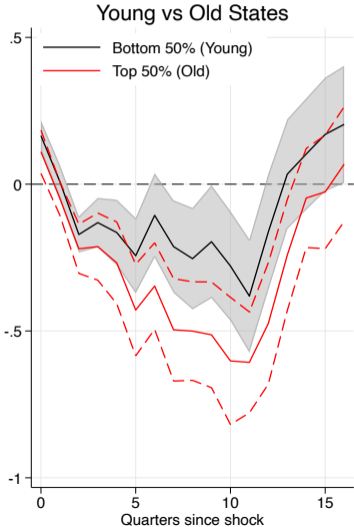
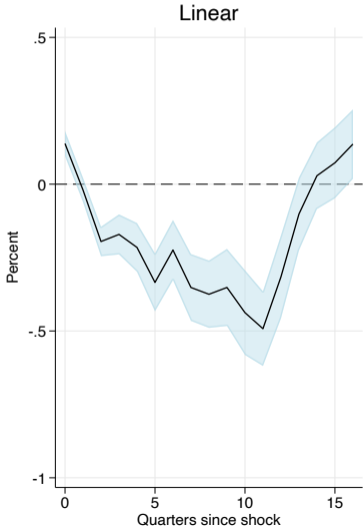
# old-age dependency ratio across states



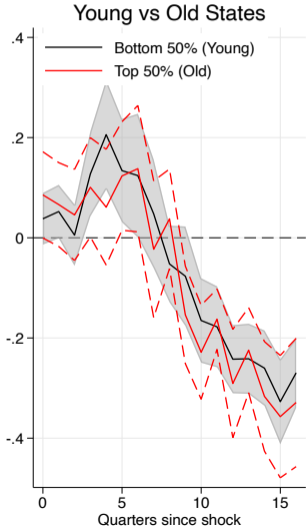
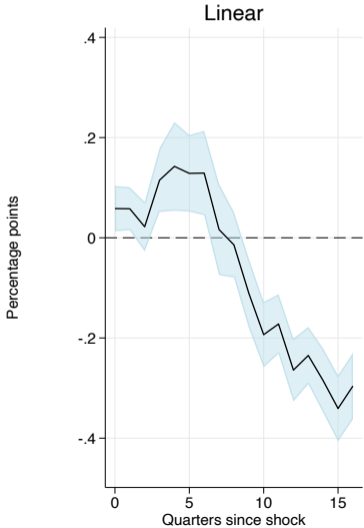
Old-dependency ratio across U.S. states, 2010 (%)

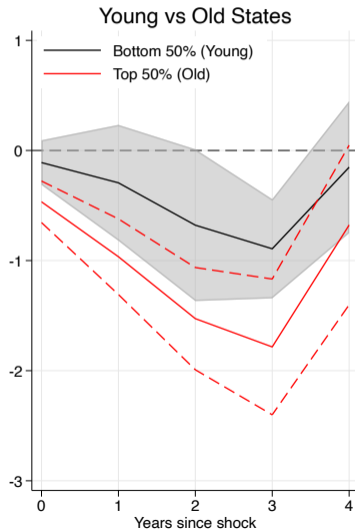
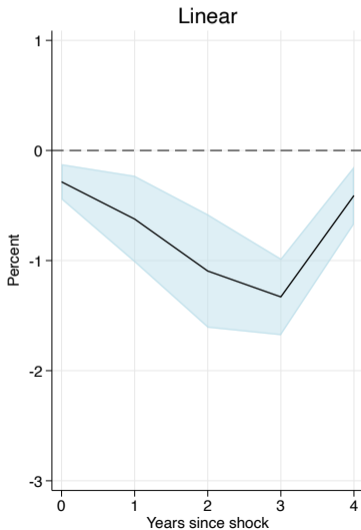


# IRF Personal Income, Above/below median

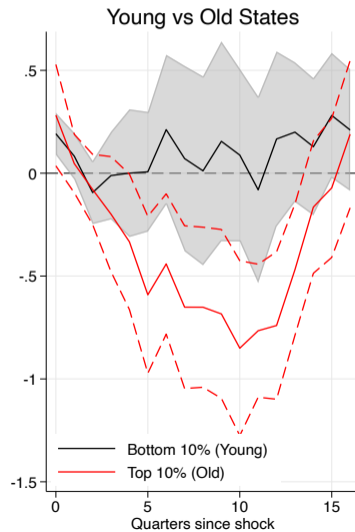
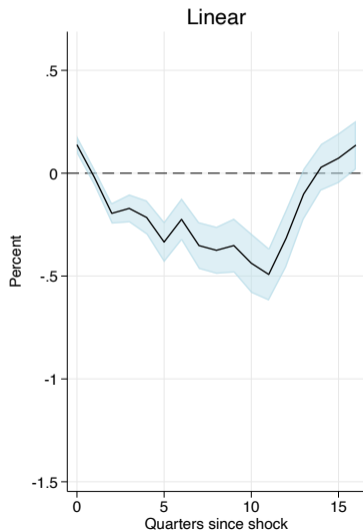


# IRF Inflation rate, Above/below median

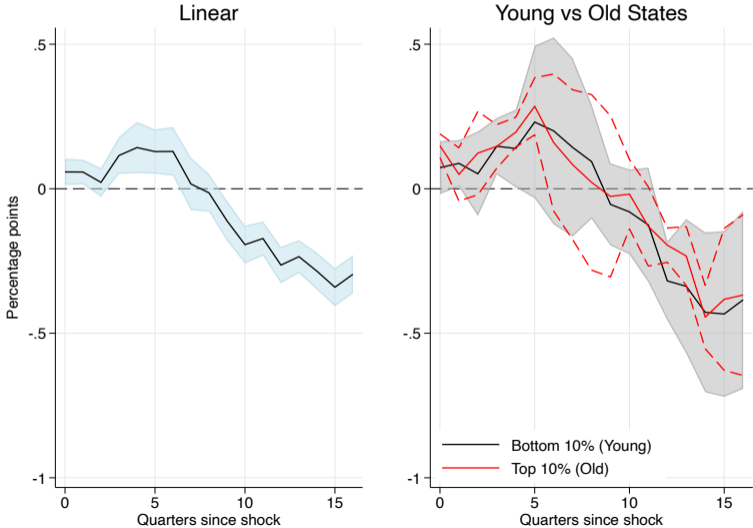


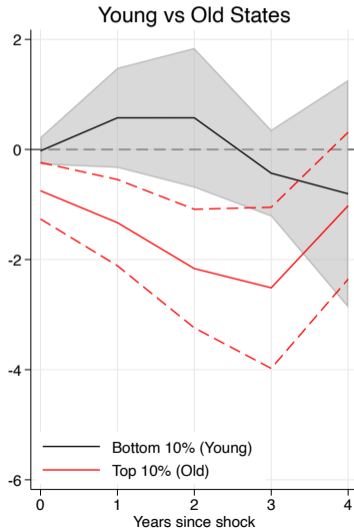
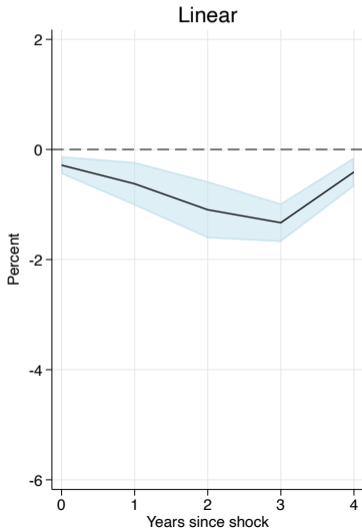


# IRF Personal Income, Top/bottom 10 %



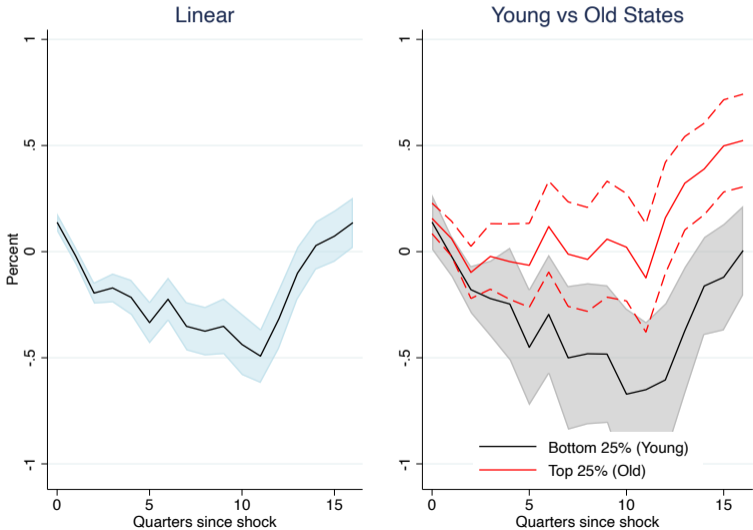
# IRF Inflation rate, Top/bottom 10 %



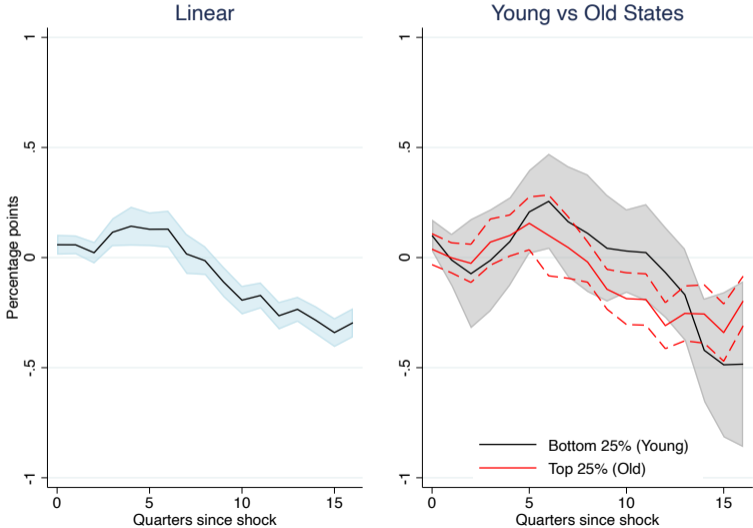


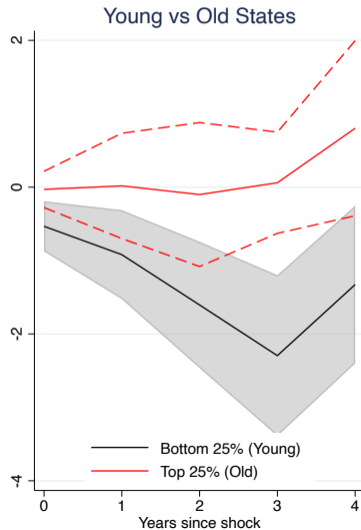
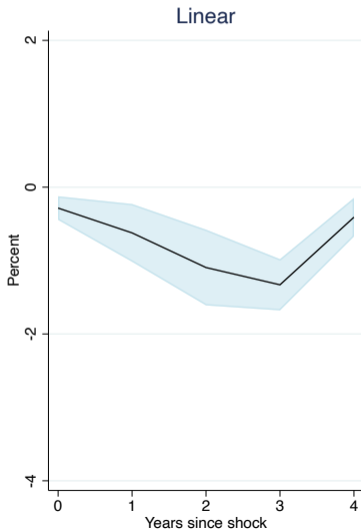


# IRF Personal Income, share working population

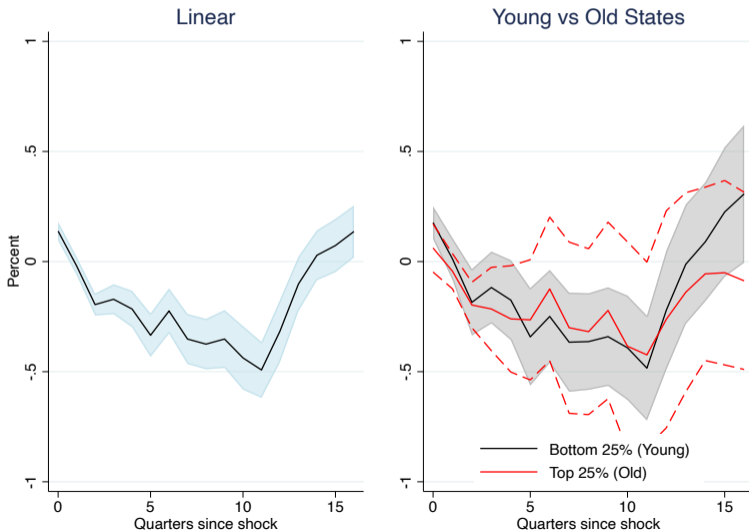


# IRF Inflation rate, share working population

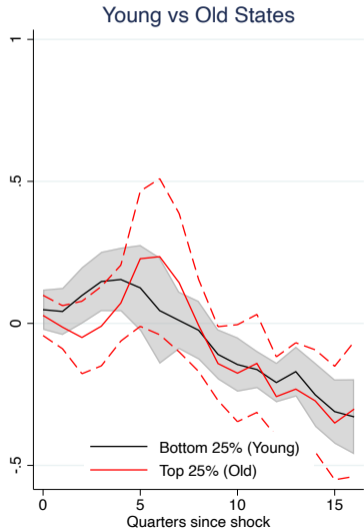
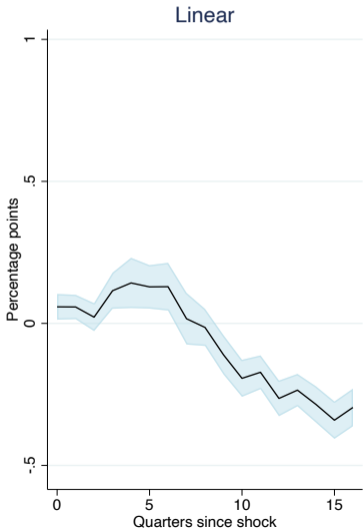


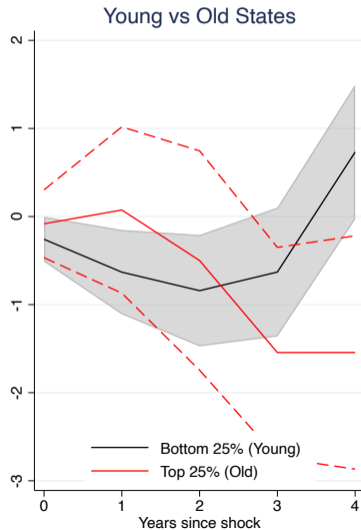
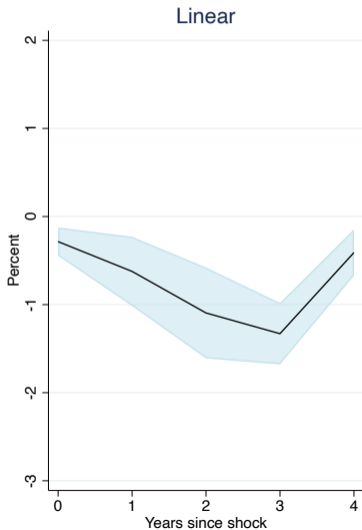


# IRF Personal Income, share young

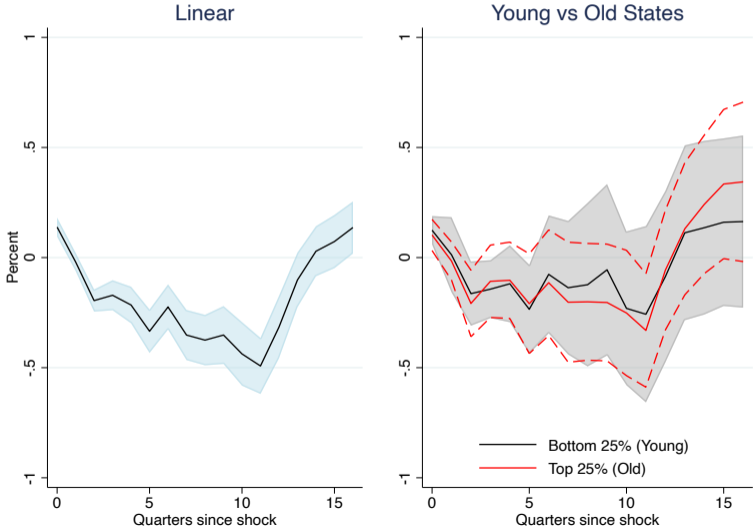


# IRF Inflation rate, share young

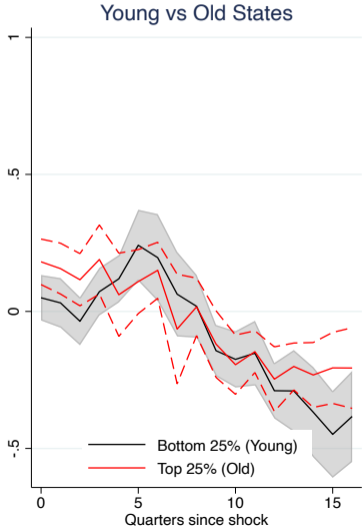
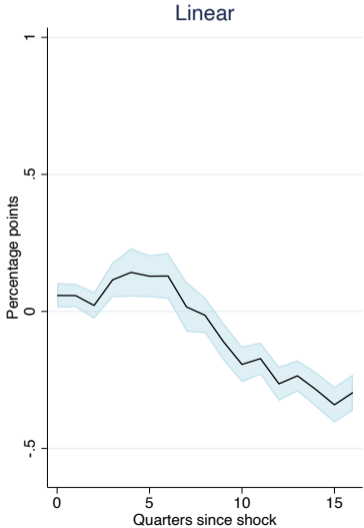




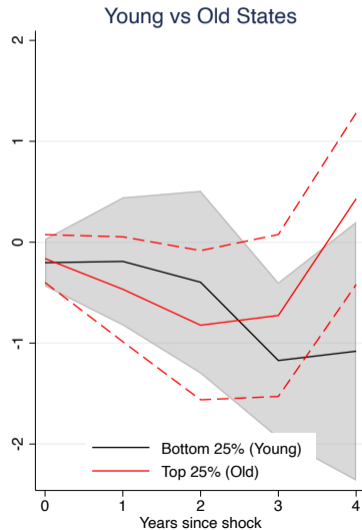
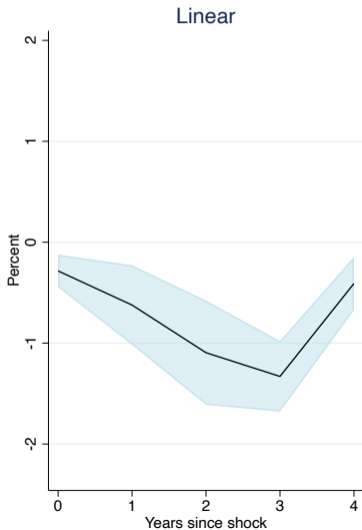
# IRF Personal Income, share old

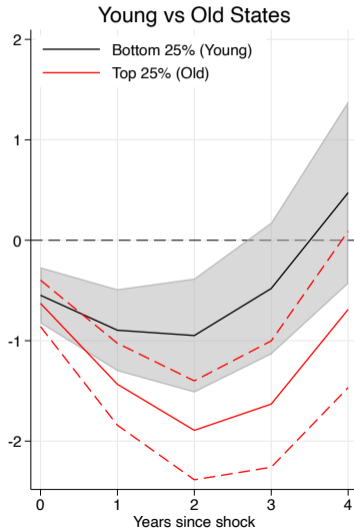
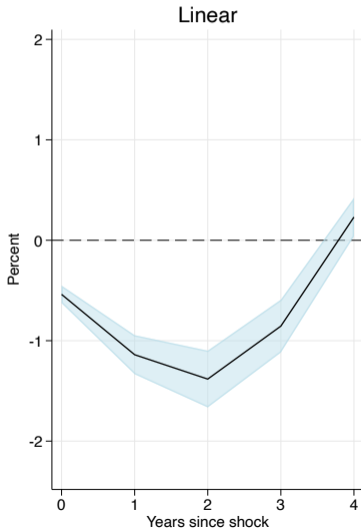


# IRF Inflation rate, share old









# Lagged birth rates as IV

Baseline regression:

$$y_{i,t+8} = \alpha_i + \beta MP_t + \tau D_{i,t} + \delta MP_t x(D_{i,t} - \bar{D}) + \theta_{i,h} X_{i,t-1} + \gamma X_{t-1} + \epsilon_{i,t}$$

- $y_{i,t+8}$  is the 2 year ahead log of Personal Income
- $D_{i,t}$  share of working population

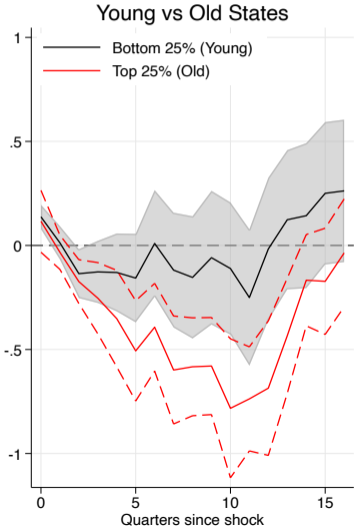
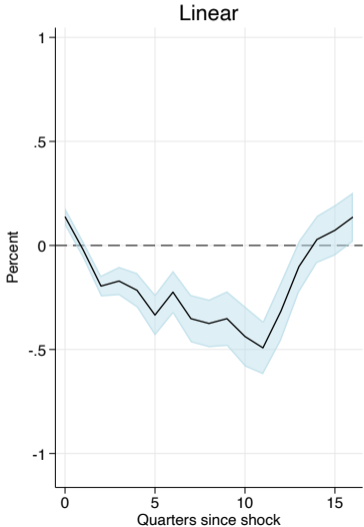
Regression table:

	(1)	(2)	(3)	(4)
	OLS	OLS	2SLS	2SLS
$MP_t$	-0.545*** (0.0905)	-0.473*** (0.0902)	-0.385 (0.252)	
$D_{i,t}$	-0.000767* (0.000434)	-0.000710* (0.000431)	-0.00747*** (0.00239)	-0.00697*** (0.00229)
$MP_t x(D_{i,t} - \bar{D})$		0.227*** (0.0232)	0.649*** (0.216)	1.024* (0.526)
Observations	7701	7701	7392	7392
Controls	YES	YES	YES	YES
State FE	YES	YES	YES	YES
Time FE	NO	NO	NO	NO
First stage F stat.			17.74	22.60

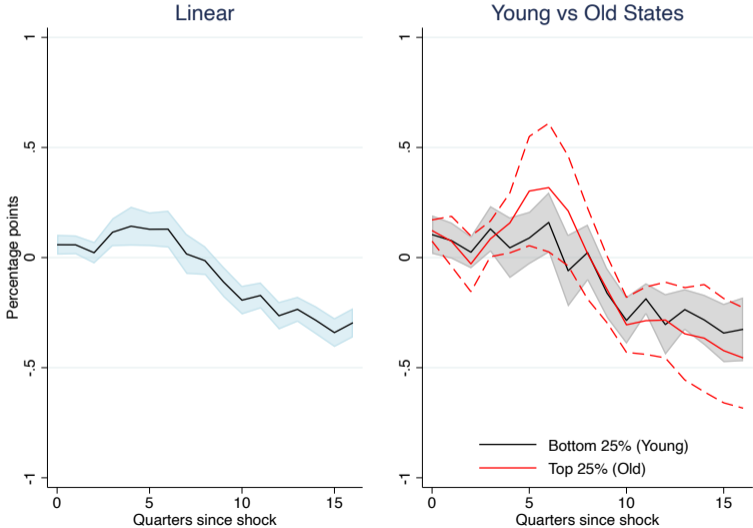
Standard errors in parentheses

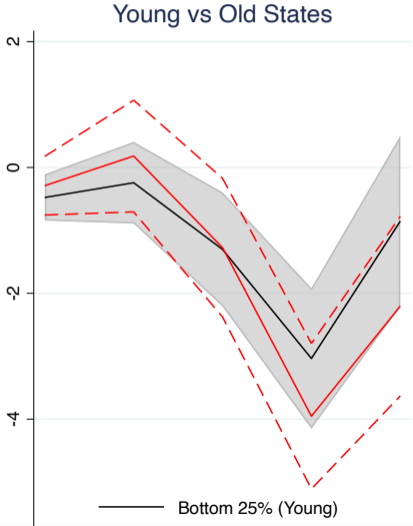
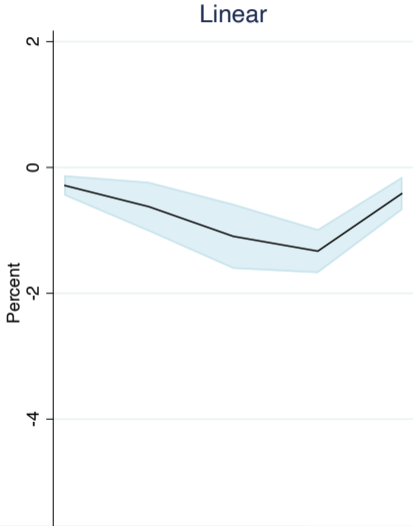
\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

# IRF Personal Income, IV

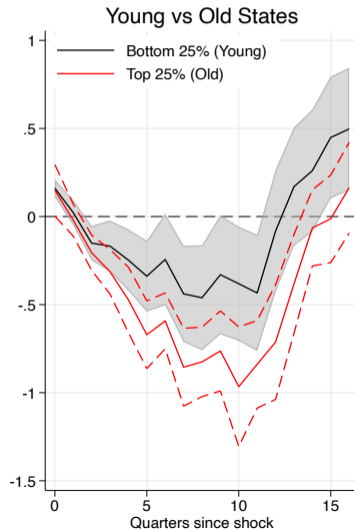
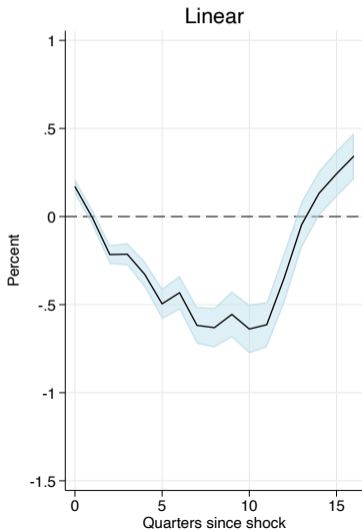


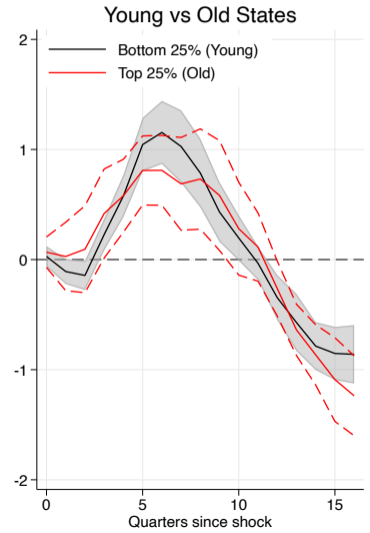
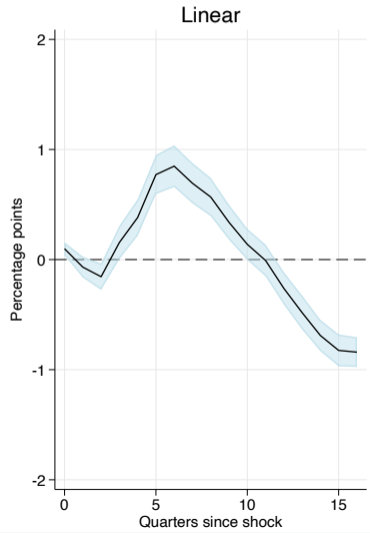
# IRF Inflation rate, IV





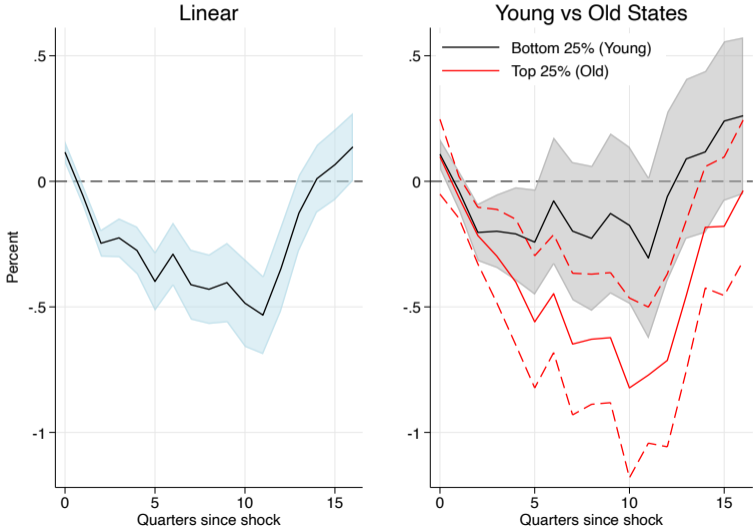
# IRF Personal Income, No financial crisis

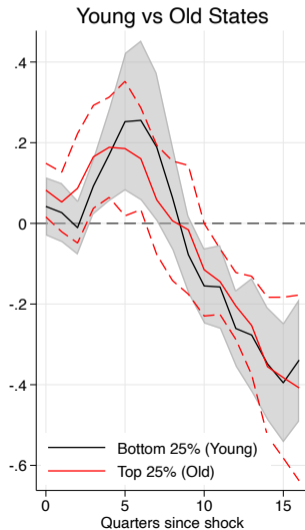
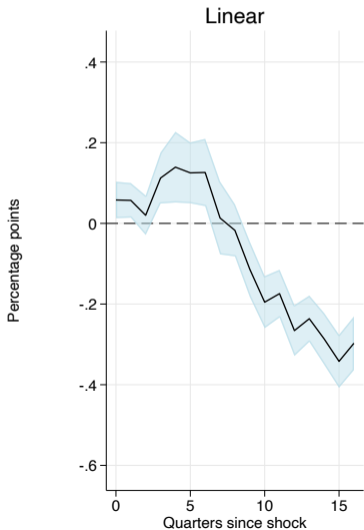




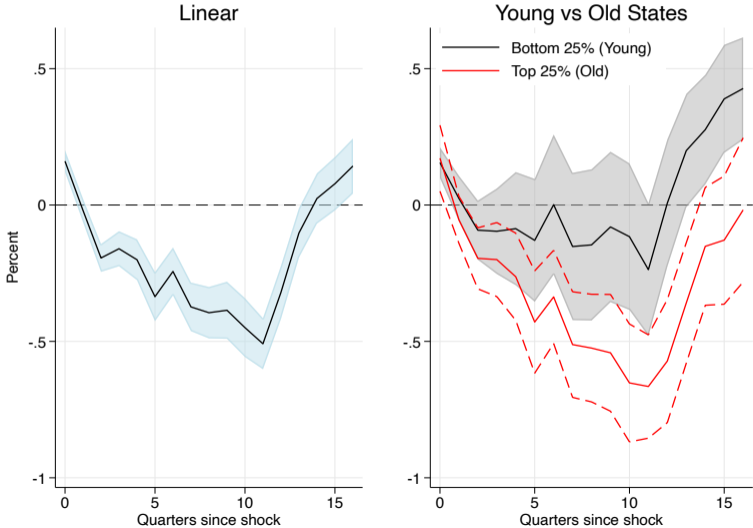


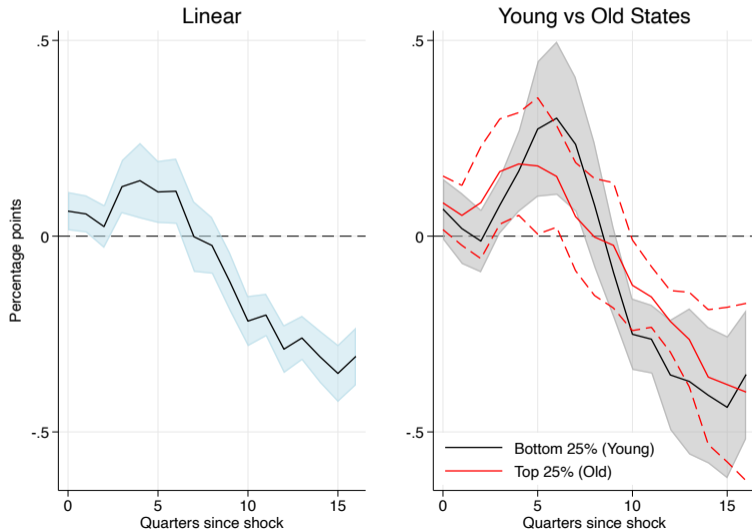
# IRF Personal Income, Controlling for income



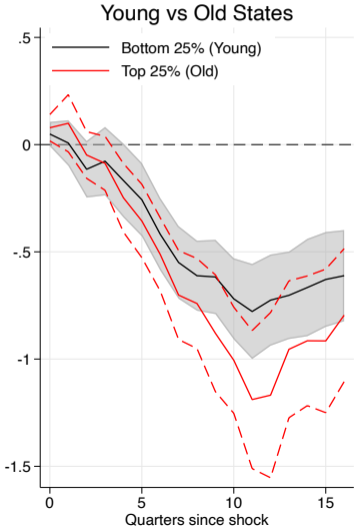
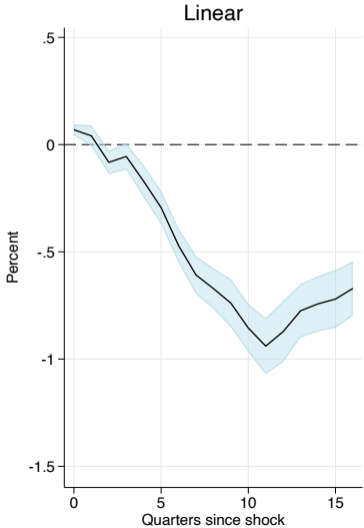


# IRF Personal Income, no small states

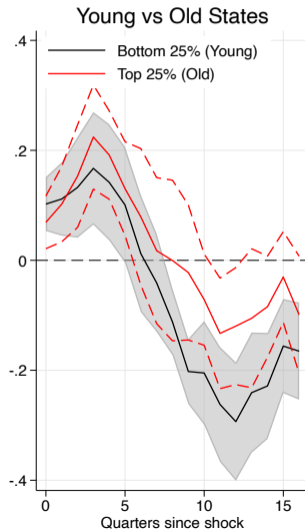
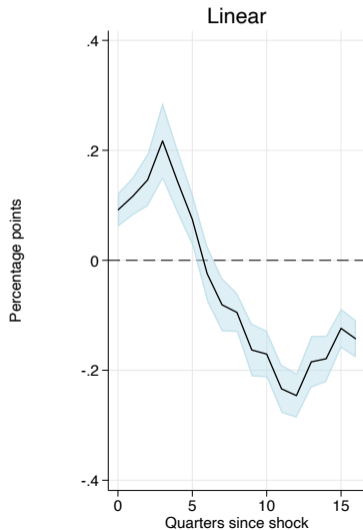


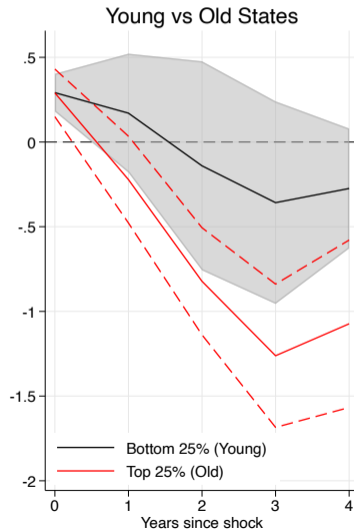
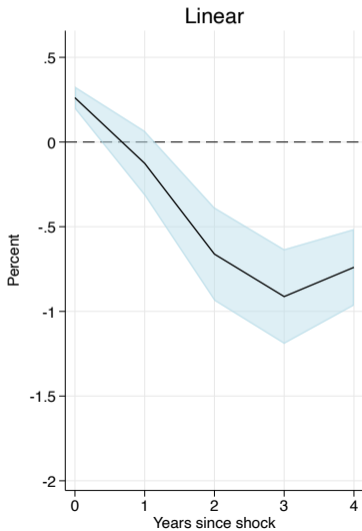


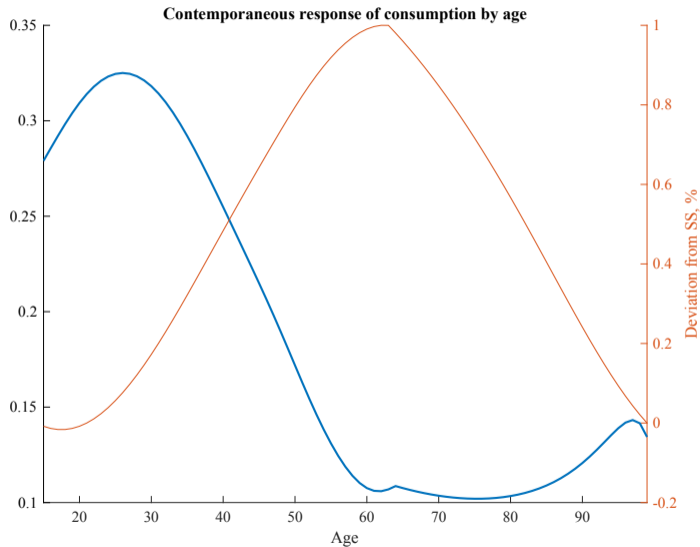
# IRF Personal Income, IV-LP



# IRF Inflation rate, IV-LP



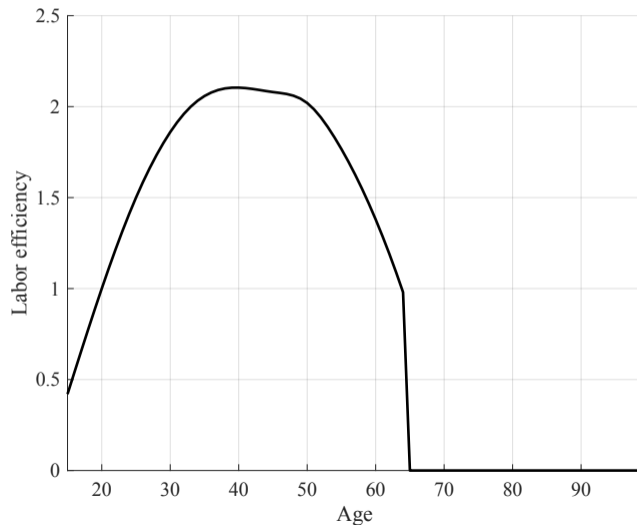






# Labor efficiency, *Source: Fullerton (1999)*

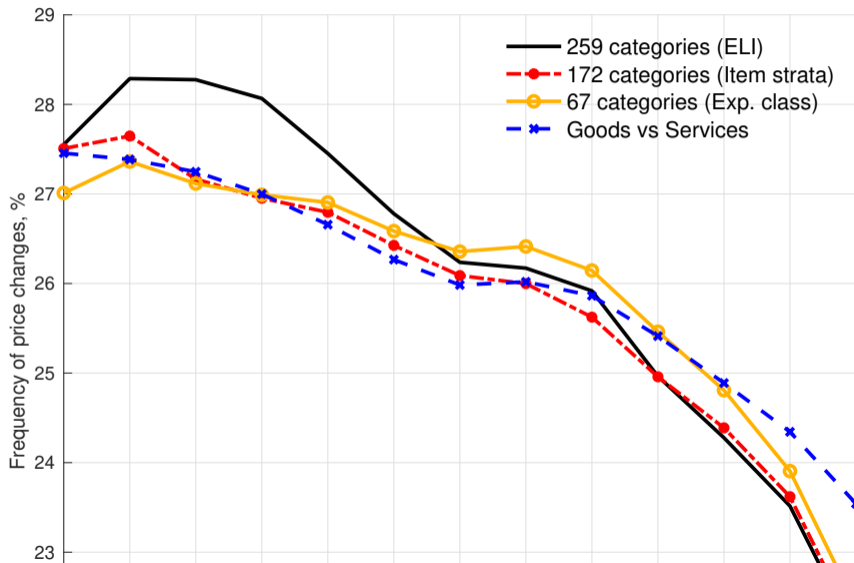
▶ Back

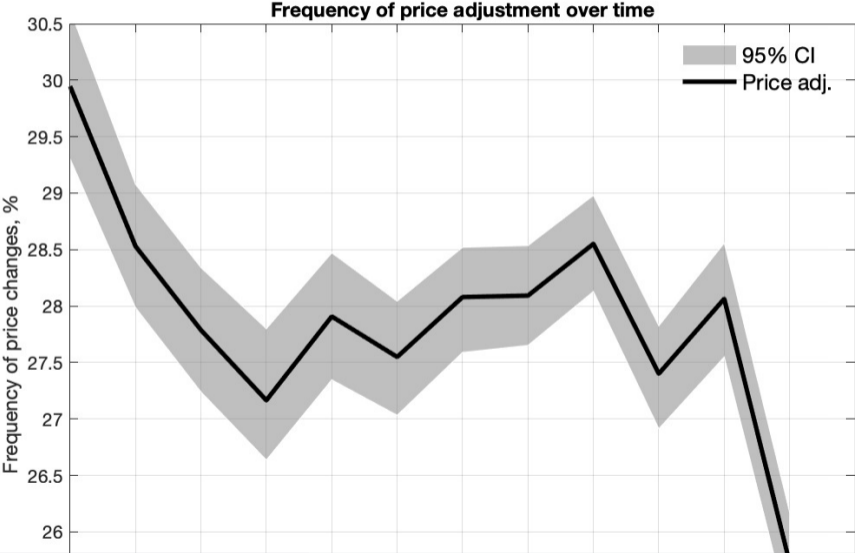


### Summary results

Parameters	1980 → 2010	Parameters ↗	
		$\pi^{IRF}$	$Output^{IRF}$
Service preference $\alpha_j$	↗	↘	↗
Survival probabilities $s_j$	↗	↗	↘
Retirement age $jw$	↗	↗	↘

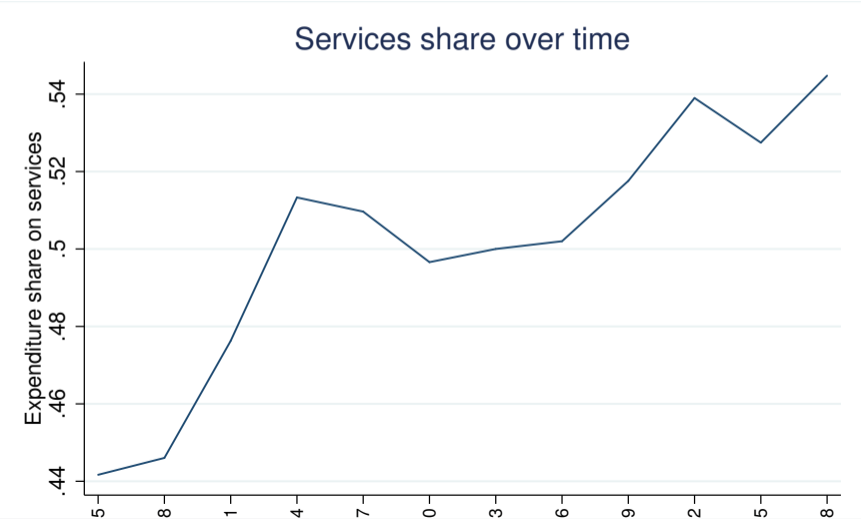
# Frequency of price adjustment across age groups



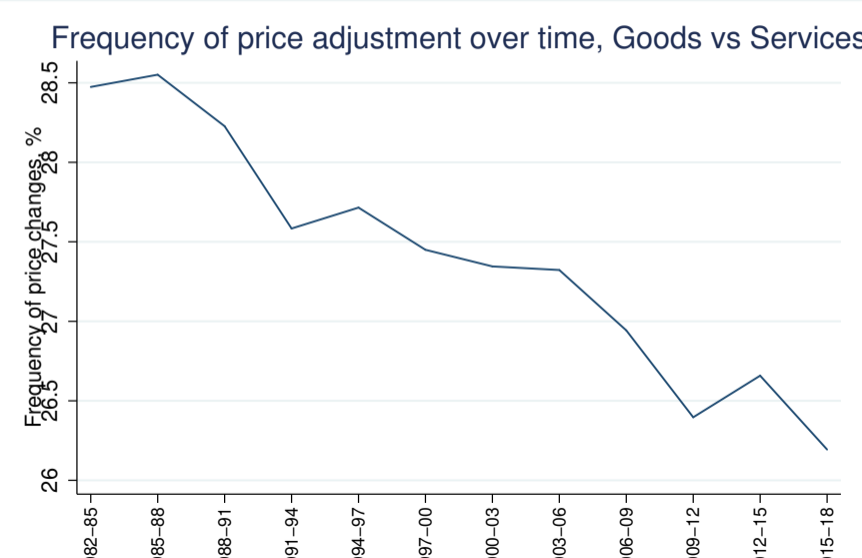


# Services vs Goods, share

$\theta_{Services}$ : 14,  $\theta_{Goods}$ : 39



# Services vs Goods, price stickiness

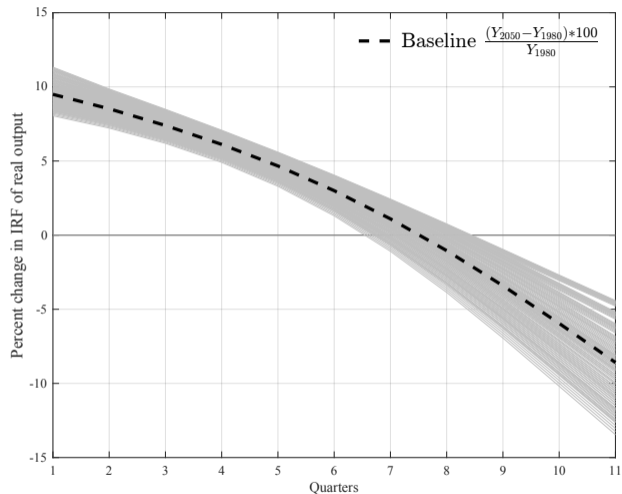


# Expenditure weights

	Age groups						
	25-	(30,35]	(40,45]	(50,55]	(60,65]	(70,75]	80+
Alcohol	2.1	1.4	1.2	1.2	1.2	1.1	0.6
Apparel	5.1	4.8	4.7	4.2	3.8	3.1	2.3
Education	6.7	1.5	2.4	3.9	1.0	0.6	0.4
Energy	3.8	5.0	5.4	5.5	6.0	6.7	7.9
Entertainment	5.9	7.0	7.5	6.9	6.8	6.0	4.4
Food Away	6.1	5.6	5.8	5.8	5.6	5.1	4.1
Food at Home	11.4	12.5	13.0	12.1	12.3	12.9	13.5
Medical	3.4	5.4	6.4	7.6	10.7	15.1	19.0
Household F&O	6.4	9.9	9.1	9.0	9.8	10.1	11.1
Other Lodging	1.2	1.0	1.4	2.0	1.8	2.0	0.9
Owned Dwellings	1.8	6.5	7.5	7.7	8.1	7.6	5.9
Other Expenses	0.9	1.1	1.3	1.4	1.6	1.8	2.4
Personal Care	1.9	1.9	2.0	1.9	1.9	2.0	2.1
Private Transportation	20.5	21.8	21.7	21.6	20.8	17.5	11.3
Public Transportation	1.2	1.3	1.4	1.5	1.8	1.7	1.1
Reading	0.3	0.4	0.4	0.5	0.6	0.7	0.7
Rented Dwellings	19.4	10.8	6.4	4.4	3.7	3.9	10.2
Tobacco	1.3	1.0	1.1	1.2	1.1	0.8	0.4
Water	0.6	1.1	1.2	1.2	1.3	1.5	1.7

▶ Back

# Change in the responsiveness of output [▶ Back](#)



Change in IRFs of output from 1980 to 2050 under different price stickiness parameters